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[Centre Inria d'Université Côte d'Azur](#)  
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## EDUCATION

<b>Vanderbilt University</b>	Nashville, TN, USA
Ph.D. in Mathematics	
Dissertation: <i>A Measure Theoretical approach to Geomnetical Inverse Problems</i>	May 2019
<b>Universidad Autónoma de San Luis Potosí</b>	San Luis Potosí, SLP, México
Bachelor's in mathematics	2012
Thesis: <i>Algebras de Lie Reductivas sobre campos de característica cero (Reductive Lie Algebras over fields of characteristic zero.)</i>	

## RESEARCH EXPERIENCE

<b>Centre Inria d'Université Côte d'Azur</b>	December 2021 – Present
Postdoctoral position under the supervision of Laurent Baratchart.	
<b>CMAP École Polytechnique</b>	October 2020 – November 2021
Postdoctoral position under the supervision of Houssem Haddar and with funding from the postdoctoral fellowship “Labex Mathématiques Hadamard” in Mathematics in Computational Science and Engineering.	
<b>Vanderbilt University</b>	August 2014 – May 2019
Dissertation directed by Douglas P. Hardin, Ph.D.	
Worked as part of the <a href="#">Impinge</a> “Associate Inria team”.	
This was a collaboration between Vanderbilt University, the department of Earth, Atmospheric and Planetary Sciences of the MIT, and the research group FACTAS (formerly APICS) from the inria Inria center at Sophia Antipolis.	
<b>Universidad Autónoma de San Luis Potosí</b>	
- Thesis under the supervision of Dr. Gil Salgado González.	August 2010 – March 2012
- Summer research for Dr. Gelasio Salazar Anaya together with Dr. Mario Cetina.	Summer 2008

## REFERENCES

<b>Laurent Baratchart, Inria (France)</b>	<a href="mailto:laurent.baratchart@inria.fr">laurent.baratchart@inria.fr</a>	+33 492 387 874
<b>Eduardo Andrade Lima, MIT (USA)</b>	<a href="mailto:limaea@mit.edu">limaea@mit.edu</a>	+1 617 324 2829
<b>Juliette Leblond, Inria (France)</b>	<a href="mailto:juliette.leblond@inria.fr">juliette.leblond@inria.fr</a>	+33 492 387 858
<b>Houssem Haddar, Inria (France)</b>	<a href="mailto:houssem.haddar@inria.fr">houssem.haddar@inria.fr</a>	+33 181 872 110
<b>Douglas P. Hardin, Vanderbilt (USA)</b>	<a href="mailto:doug.hardin@vanderbilt.edu">doug.hardin@vanderbilt.edu</a>	+1 615 322 6662

## MANUSCRIPTS

- L. Baratchart, H. Haddar, **C. Villalobos Guillén**, Silent surface sources for the Helmholtz equation and decomposition of  $L^2$  vector fields.
- L. Baratchart, D. P. Hardin, **C. Villalobos Guillén**, Numerical setting for the solution of TV-norm regularized inverse problems.
- L. Baratchart, D. P. Hardin, **C. Villalobos Guillén**, Uniqueness result for TV-norm regularized inverse problems with source term in divergence form.

## PUBLICATIONS

- L. Baratchart, **C. Villalobos Guillén**, D. P. Hardin, Inverse potential problems in divergence form for measures in the plane. ESAIM: COCV, 27 (2021) 87 DOI: <https://doi.org/10.1051/cocv/2021082>
- L. Baratchart, **C. Villalobos Guillén**, D. P. Hardin, M. C. Northington, and E. B. Saff. Inverse potential problems for divergence of measures with total variation regularization. Foundations of Computational Mathematics, Nov 2019.
- Laurent Baratchart, **Cristobal Villalobos-Guillen**, Douglas Hardin and Juliette Leblond, Sparse recovery for inverse potential problems in divergence form, to be published in the Proceedings at the 9th International Conference on New Computational Methods for Inverse Problems, May 24, 2019
- G. SALGADO, **C. Villalobos-Guillen**, Algebras de Lie reductivas y semisimples; nuevas caracterizaciones, Aportaciones (Reductive and semisimple Lie Algebras, new characterizations) Mat. Comun. Vol. 52, pags. 3-12, (2017)
- M. Cetina, C. Hernández-Vélez, J. Leños, **C. Villalobos**, Point sets that minimize ( $\leq k$ )-edges, 3-decomposable drawings, and the rectilinear crossing number of  $K_{30}$ , Discrete Mathematics, Volume 311, Issue 16, 28 August 2011, Pages 1646-1657, ISSN 0012-365X, 10.1016/j.disc.2011.03.030.

## PRESENTATIONS

- [Inverse problem for the Helmholtz equation and singular sources in the divergence form](#), at the 2022 WAVES conference held in July 2022  
Discussed an inverse problem where the underlying model is related to sources generated by currents on an anisotropic layer. This problem is a generalization of another motivated by the recovering of magnetization distribution in a rock sample from outer measurements of the generated static magnetic field. The original problem can be formulated as inverse source problem for the Laplace equation with sources being the divergence of the magnetization whereas the generalization comes from taking the Helmholtz equation. Either inverse problem is non uniquely solvable with a kernel of infinite dimension. Presented a decomposition of the space of sources that will allow us to discuss constraints that may restore uniqueness and propose regularization schemes adapted to these assumptions.
- [Some measure-theoretic aspects of planar magnetization reconstruction](#), at the 10th International Conference Inverse Problems: Modeling and Simulation held on May 2022.  
When modeling magnetizations by  $\mathbb{R}^3$ -valued Borel measures, the kernel of the forward operator, mapping magnetizations supported on the plane  $\{z = 0\}$  to the restriction of the magnetic fields they induce to a sufficiently dense subset of an analytic surface, consist of divergence free measures whose 3rd component is zero. Using this fact as a motivation, showed how any divergence free  $\mathbb{R}^3$ -valued Borel measure on  $\mathbb{R}^2$  can be decomposed into line integrals over Jordan curves. This result has two important implications for the recovery of planar magnetizations. First, that any magnetization supported on sufficiently separated straight lines has minimal total variation, in the measure-theoretic sense, among all other planar magnetizations that induce the same field. Second, that the group LASSO regularization problem in this context, which amounts to total variation regularization, has a unique solution for any value of the regularization parameter.
- [Inverse Problem for Singular Sources in the Divergence Form](#), at the 2022 SIAM Conference on Imaging Science held in March 2022.

Discussed an inverse problem motivated by the recovering of magnetization distribution in a rock sample from outer measurements of the generated static magnetic field. It can be formulated as inverse source problem for the Laplace equation with sources being the divergence of the magnetization. It can also be generalized to the Helmholtz equation where the underlying model is related to sources generated by currents on an anisotropic layer.

This was a collaborative work with L. Baratchart, H. Haddar and D. P. Hardin.

- ["El número de cruce rectilíneo y pseudolineal de  \$K\_{30}\$  es 9726"](#) (The lineal and pseudo-lineal crossing number of  $K_{30}$  is 9726), at the XLI National Congress of the Mexican Mathematical Society (SMM) held in October 2008.

This was a collaborative work with M. Cetina. Based on the work of J. Leños, we were able to show that the rectilinear crossing number of  $K_{30}$  (that is, the minimal number of edge crossing for the drawing on the plane of a complete graph with 30 vertices where each of the 435 edges is a line segment) actually reached its current upper bound, 9726 .

## POSTERS

- [The Magnetization Inverse Problem on 2-D sources](#), at the [Conference: 30 ans de mathématiques pour l'imagerie optique](#).

Marseille, France from the 25<sup>th</sup> to the 27<sup>th</sup> of September 2023

This work is concerned with inverse potential problems with source term in divergence form.

Such issues typically arise in source identification from field measurements for Maxwell's equations, in the quasi-static regime. They occur for instance in geomagnetism and paleomagnetism, as well as in several non-destructive testing problems. A model problem of our particular interest and which we will take as focus in this poster, is inverse scanning magnetic microscopy, to recover magnetization distributions of thin rock samples. However the considerations here are of a more general and abstract nature.

## SUMMER SCHOOLS

- [Scientific Machine Learning](#)  
CIRM, Marseille, France from the 17<sup>th</sup> to the 21<sup>st</sup> of July 2023
- [Deep Learning: a hands-on introduction](#) and [Computer Vision Crash Course](#)  
Genoa, Italy, from the 12<sup>th</sup> to the 20<sup>th</sup> of July 2022
- ["Escuela Matemática de América Latina y el Caribe 2010"](#)  
(Mathematical School of Latin America and the Caribbean)  
Villahermosa, México, from the 2<sup>nd</sup> to the 13<sup>th</sup> of August 2010.

## OTHER EXPERIENCE

### Technical proofreader

January 2019 – March 2019

Department of Mathematics, Vanderbilt University

Proofread preliminary versions of the book: Borodachov, S. V., Hardin, D. P., and Saff, E. B. (2019). Discrete energy on rectifiable sets. New York, NY: Springer.

### Teaching assistant

August 2013 – December 2018

Department of Mathematics, Vanderbilt University

- Directed weekly lab on the 2017 Fall term on the basis of Data science with R
- Graded homework and exams
- Directed discussion sessions
- Held office hours to tutored students

### Problem Judge of the 25th Mexican Mathematical Olympics ([OMM](#))

13th – 19th of November  
of 2011

San Luis Potosí, México

This is a contest between highschool and middleschool students where they solve proof-based mathematical problems.

