8. sympy

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1 sympy para cálculos simbólicos

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In [1]: from sympy import *
   Para crear variables que son objetos simbólicos:
In [7]: x = symbols("x")
        # Crea un nombre 'x' que se refiere al simbolo con la representacion visual 'x'
In [3]: x
Out[3]: x
In [4]: y
    NameError
                                                 Traceback (most recent call last)
        <ipython-input-4-009520053b00> in <module>()
    ----> 1 y
        NameError: name 'y' is not defined
   Para que se vean bonitos:
In [5]: init_printing()
In [6]: x
Out[6]:
                                               \boldsymbol{x}
In [8]: 2 * x
Out[8]:
                                               2x
In [9]: x * x
```

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Out[9]:
                                                x^2
In [11]: expr = 2*x + 3*x**2
In [12]: diff(expr, x)
Out[12]:
                                               6x + 2
In [13]: integrate(expr, x)
Out[13]:
                                              x^3 + x^2
In [14]: integrate(_, x)
Out[14]:
                                             \frac{x^4}{4} + \frac{x^3}{3}
In [15]: diff(_, x)
Out[15]:
                                              x^3 + x^2
In [16]: s = sin(x)
In [17]: s
Out[17]:
                                               \sin(x)
In [18]: diff(s, x)
Out[18]:
                                              \cos(x)
In [20]: y = symbols("y")
In [21]: diff(s, y)
Out[21]:
                                                 0
In [22]: p = x*y
In [23]: diff(p, x)
Out[23]:
                                                 y
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In [24]: diff(p, y)
Out[24]:
                                                    \boldsymbol{x}
In [27]: s
Out[27]:
                                                 \sin(x)
In [28]: s * s
Out[28]:
                                                 \sin^2(x)
In [29]: s * expr
Out[29]:
                                            \left(3x^2 + 2x\right)\sin\left(x\right)
In [36]: r = series(s, x, n=10)
In [41]: r.coeff(x, 5)
Out[41]:
                                                    1
                                                   \overline{120}
In [42]: M = Matrix([x, x**2, x**3, x**4])
In [43]: M
Out[43]:
In [48]: M = Matrix([x, x**2, x**3, x**5]).reshape(2,2)
In [49]: M
Out[49]:
In [50]: M.det()
Out[50]:
                                                 x^6 - x^5
```

```
In [51]: M.inv()
Out[51]:
                                                                                                                                                                                                                             \begin{bmatrix} \frac{1}{x} + \frac{1}{x(x-1)} & -\frac{1}{x^3(x-1)} \\ -\frac{1}{x^2(x-1)} & \frac{1}{x^4(x-1)} \end{bmatrix}
In [55]: M.inv().subs(x,10)
Out [55]:
                                                                                                                                                                                                                                                        \begin{bmatrix} \frac{1}{9} & -\frac{1}{9000} \\ -\frac{1}{900} & \frac{1}{90000} \end{bmatrix}
In [56]: M.subs(\{x:10, y:3\})
Out [56]:
                                                                                                                                                                                                                                                        \begin{bmatrix} 10 & 100 \\ 1000 & 100000 \end{bmatrix}
In [57]: M
Out[57]:
                                                                                                                                                                                                                                                                        \begin{bmatrix} x & x^2 \\ x^3 & x^5 \end{bmatrix}
In [63]: M.eigenvals()
Out[63]:
                                        \left\{ \frac{x}{2} \left( x^4 + 1 \right) - \frac{1}{2} \sqrt{x^2 \left( x^8 - 2x^4 + 4x^3 + 1 \right)} : 1, \quad \frac{x}{2} \left( x^4 + 1 \right) + \frac{1}{2} \sqrt{x^2 \left( x^8 - 2x^4 + 4x^3 + 1 \right)} : 1 \right\}
In [64]: expr = x**4 - x**2 + 1
In [65]: solve(expr, x)
Out[65]:
                                                                                                                                                                            \left[ -\frac{\sqrt{3}}{2} - \frac{i}{2}, -\frac{\sqrt{3}}{2} + \frac{i}{2}, \frac{\sqrt{3}}{2} - \frac{i}{2}, \frac{\sqrt{3}}{2} + \frac{i}{2} \right]
In [68]: expr = x**5 + 2*x**4 - x**2 + 1
In [69]: solve(expr, x)
Out[69]:
\left[ \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 0 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 1 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - x^2 + 1, 2 \right), \quad \text{RootOf}\left( x^5 + 2x^4 - 
In [72]: import sympy
In [73]: theta = symbols("theta")
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In [74]: theta