Table of Contents

Introductionii			
Chapter 1	Family of Numbers Family of Numbers Important Divisibility Rules. Prime Factorization. The Rats! Rational Numbers Important Factors Chapter Review	1 5 6 10	
Chapter 2	Working With Integers Addition of Integers Absolute Value. Adding Positive and Negative Integers Subtraction of Integers Multiplication and Division of Integers Working With Exponents Chapter Review The Cowboy Story	15 16 21 26 28	
Chapter 3	Working With Rational Numbers	32 36 42 45	
Chapter 4	Ratio, Proportion, and Percent Converting Fractions to Decimals and Terminating Decimals to Fractions. Common Fractions/Decimals How to Tell if a Fraction Terminates or Repeats Ratio, Rate, and Unit Rate. Proportions Scale Drawings Understanding Percent. Working With Percent Chapter Review	49 53 54 59 63	

Chapter 5	Percent Applications	77-86
	Going Shopping- Tax and Tips	77
	Percent Increase and Decrease	81
	Understanding Simple Interest vs Compound Interest	82
	Chapter Review	
Chapter 6	Algebraic Expressions	. 87-116
Citapte: 0	Expression vs Equations	
	Evaluating Expressions	
	Translating Expressions	
	Understanding "Less," "Less Than," and "From"	
	Polynomials	
	Understanding "Like Terms"	
	Subtracting Polynomials	
	Multiplication of Monomials - Exploring Exponent Rules	
	Thinking More About Monomials	
	Powers	
	Division of Monomials	
	Understanding Negative Powers	
	Scientific Notation	
	Using Scientific Notation to Simplify	
	Chapter Review	
Chapter 7	Equations and Solving Word Problems	117-152
	Properties of Real Numbers (Part 1)	
	Properties of Real Numbers (Part 2)	
	Properties of Equality	
	Solving Algebra Equations	126
	Step 4: Using the Additive Inverse	
	Step 5: Using the Multiplicative Inverse	
	Solving Two Step Equations	
	Solving Word Problems Using Equations	
	Steps 3, 4, and 5: Moving Variable Terms to the Same Side	
	Steps 2-5: Combining Like Terms on Each Side	
	Steps 1-5: Using All the Steps to Solve Equations	
	Consecutive Integer Problems	
	Thinking More About Equations	
	Chapter Review	
Chapter 8	Inequalities and Applications	153-171
Chapter 6	Graphing Inequalities	
	Solving Inequalities	
	How to Tell an Equation From an Inequality in Word Problems.	
	Understanding Compound Inequalities	
	Graphing Compound Inequalities	
	Chapter Review	
	5ap 55. 1.641644 11111111111111111111111111111	

Chapter 9	Understanding Square Roots and Irrational Numbers	172-195
	Repeating Decimals Cannot Be Irrational Numbers	
	Squaring and Square Roots	174
	Cube Roots and Other Roots	
	Simplifying Square Roots	
	A Look at Irrational PI	
	The Pythagorean Theorem	
	Chinese Proof of the Pythagorean Theorem	190
	Chapter Review	191
Chapter 10	Two Dimensional Geometry	196-234
	Naming Angles	
	Parallel Lines and Transversals	200
	Perimeter	
	Polygons	
	Angles of Triangles and Polygons	
	Types of Triangles	
	Areas of Parallelograms, Triangles, and Trapezoids	
	Area of Parallelograms	
	Area of Triangles	
	Area of Trapezoids	
	Using Algebra to Solve Geometry Problems	
	Finding the Circumference and Area of a Circle	
	Chapter Review	
Chapter 11	Understanding Volume and Surface Area	236-251
Chapter 11	Volume of Prisms	
	Volume of Pyramids	
	Volume of Cylinders and Cones	
	Surface Area	
	Surface Area of a Cone	
	Volume and Surface Area of a Sphere	
	Chapter Review	
Chapter 12	Graphing on the Coordinate Plane	
	Graphing Linear Equations	
	Special Graphs	
	Using Slope and Y-Intercept to Graph Linear Equations	
	Types of Slopes	258
	Finding Slope Given Two Points	
	Writing an Equation Given Two Points	
	Graphs of Proportional Relationships	
	Systems of Equations	
	Chapter Review	

Transformations and Congruency	276-302
Translations	276
Reflections	280
Rotations	283
Understanding Triangle Congruency (SSS, SAS, ASA)	286
Chapter Review	
•	
Understanding Functions	303-322
Understanding Functions	303
Quadratic Functions	
Understanding Exponential Functions	309
Probability and Statistics	323-358
_	
•	
· ·	
Chapter Review	
nation	250_267
IIauoII	339-307
	369-373
	300-3/2
Sheet	272
лісеt	
uare Roots 1-120	374
uui C 1.00t3 1 120	
i .	Reflections Rotations Understanding Triangle Congruency (SSS, SAS, ASA) How to Prove Triangles Are Congruent Dilations Similarity Chapter Review Understanding Functions Understanding Functions Understanding Exponential Functions Exponential Growth and Decay Absolute Value Functions Linear, Exponential, and Quadratic Functions Review. Chapter Review

Chapter 4

Ratio, Proportion, and Percent

Fractions, decimals, and percents are different ways of representing the same quantities. For some situations, you'll know whether it's better to represent a quantity by a fraction, a decimal, or a percent. Let's review how to change fractions to decimals and terminating decimals to fractions.

Remember from Chapter 1 that any fraction can be changed to a terminating (a decimal that stops) or to a repeating decimal.

Converting Fractions to Decimals and Terminating Decimals to Fractions

Example 1: Change $\frac{3}{8}$ to a decimal.

The fraction bar means "divide." You're dividing 3 by 8. You can think of the 3 sitting on a chair and falling into the box. Since 8 cannot go into 3, put a decimal point after the 3 and add a few zeros. Then start dividing and keep dividing until the decimal terminates or repeats.

Example 2: Change .375 to a fraction.

The 5 sits on the thousandths place, so write 375 as the numerator and 1,000 as the denominator and reduce. Then divide the fraction by 5. If the GCF (which is 125) was found, the fraction could have been reduced in one step.

$$\frac{375}{1,000} = \frac{75}{200} = \frac{15}{40} = \frac{3}{8}$$

Example 3: Change $-5\frac{2}{3}$ to a decimal.

Since -5 is an integer, you just need to find out what $\frac{2}{3}$ is as a decimal. Again, drop the 2 into the box and divide.

You can see that the 6 will repeat, so the answer is $-5.\overline{6}$. The bar on top of the 6 indicates that the 6 repeats. And yes, you can write your answer as $-5.\overline{66}$.

Common Fractions/Decimals

You can always use the above methods to covert fractions to decimals and terminating decimals to fractions. However, there are 10 common fractions/decimals that appear in many real life situations, as well as in many standardized tests that you might take in the future. It is a great advantage to memorize these. Making flashcards may be useful. Make sure you do not memorize these unless you understand the concept.

$$\frac{1}{2} = .5$$

$$\frac{3}{8} = .375$$

$$\frac{1}{4} = .25$$

$$\frac{5}{8} = .625$$

$$\frac{3}{4} = .75$$

$$\frac{7}{8} = .875$$

$$\frac{1}{5} = .2$$

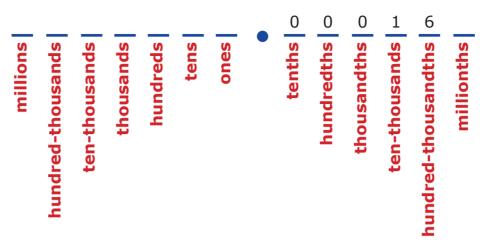
$$\frac{1}{3} = .\overline{3}$$

$$\frac{1}{8} = .125$$

$$\frac{2}{3} = .\overline{6}$$

 $\frac{1}{5}$ = .2. What are the decimals for $\frac{2}{5}$, $\frac{3}{5}$, and $\frac{4}{5}$. Why?

PLACE VALUE CHART



Practice

Change the following decimals to fractions. Make sure to simplify each fraction. If you memorized the "Common Fractions/Decimals," you do not need to show work.

1. .08

6. .00016 (see chart)

2. .004

7. -6.008

3. -5.025

8. 26.75

4. .375

9. -9.248

5. -9.875

10. .00065

Change the following fractions to decimals. Remember to reduce the fraction first. If you memorized the "Common Fractions/Decimals," then you do not need to show work.

11. $\frac{7}{100}$

17. $-10\frac{1}{3}$

12. $\frac{3}{24}$

18. $-9\frac{27}{72}$

13. $\frac{2}{5}$

19. $\frac{125}{100}$

14. $\frac{5}{8}$

20. $\frac{18}{24}$

15. $-8\frac{3}{10,000}$

21. $-\frac{5}{32}$

16. $\frac{3}{16}$

22. $\frac{22}{7}$

- 23. a. Change $\frac{1}{9}$ to a decimal.
 - b. Change $\frac{2}{9}$ to a decimal.

Finish the pattern.

c.
$$\frac{3}{9} =$$
______, $\frac{4}{9} =$ ______, $\frac{5}{9} =$ ______, $\frac{6}{9} =$ ______, $\frac{7}{9} =$ _______, $\frac{8}{9} =$ ______

d. So $\frac{9}{9} =$ _____. But isn't $\frac{9}{9}$ the same as 1 whole?

Explain your thinking.

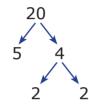
How to Tell if a Fraction Terminates or Repeats

When changing a fraction to a decimal, it helps to know ahead of time if the decimal will terminate or repeat. To figure this out, follow these steps.

Example 1: Does the fraction $\frac{6}{40}$ terminate or repeat when changed to decimal?

- Step 1: Reduce the fraction first! It becomes $\frac{3}{20}$.
- Step 2: Do a prime factorization of the denominator. Do not worry about the numerator.

The prime factorization of 20 is: $2 \cdot 2 \cdot 5$ or $2^2 \cdot 5$.



- Step 3: If you have only factors of 2, or only factors of 5, or both, but no other primes such as 3, 7, 11, etc. in the prime factorization of the denominator, then the fraction will terminate when changed to a decimal.
- Example 2: Does the fraction $\frac{3}{70}$ terminate or repeat when changed to a decimal?

The fraction is already reduced. The prime factorization of 70 is $2 \bullet 5 \bullet 7$. Therefore the prime number 7 will make this fraction repeat when changed to a decimal repeat.

Practice

1. Why do you think having only the primes 2 and/or 5 and no other primes will make the fraction terminate when changed to a decimal? Explain your thinking.

2. Do these fractions terminate (T) or repeat (R) when changed to a decimal?

Use an extra sheet of paper if needed. Don't forget to reduce each fraction first.

a.
$$\frac{1}{20} =$$

b.
$$\frac{3}{30} =$$

c.
$$\frac{22}{14} =$$

d.
$$\frac{1}{64} =$$

e.
$$\frac{9}{54} =$$

f.
$$\frac{8}{41} =$$

Ratio, Rate, and Unit Rate

A ratio is the relationship between two quantities.

Example 1: In a classroom there are 15 girls to 7 boys. What is the ratio of girls to boys?

You can write the answer as 15 to 7, 15:7, or $\frac{15}{7}$.

Since the question reads "girls" to "boys," then the number that matches with girls goes first. If you write the ratio as a fraction, you can reduce.

Example 2: In the problem above, what is the ratio of boys to the total number of students in the classroom?

The answer is 7 to 22, 7:22, or $\frac{7}{22}$.

Example 3: At a dance the principal of a school wants to have the ratio of chaperones to students to be 2 chaperones for every 9 students. If the total number of chaperones plus students was 110, how many chaperones were there?

2 chaperones + 9 students = 11 people. $\frac{2}{11}$ is the ratio of chaperones to total people.

So $\frac{2}{11}$ of 110 must be chaperones. $\frac{2}{11} \cdot 110 = 20$. There are 20 chaperones.

Example 4: Dana drove 200 miles using 5 gallons of gas. Simplify the ratio of miles to gallons.

 $\frac{200 \text{ miles}}{5 \text{ gallons}} = \frac{40 \text{ miles}}{1 \text{ gallon}}$ You can say Dana's car gets 40 miles per gallon or 40 mj/gal or 40 mpg (miles per gallon).

 $\frac{200}{5}$ is called a <u>rate</u> (a special type of ratio used to compare measurements with different units) and $\frac{40}{1}$ is called a <u>unit rate</u>.

A unit rate is a rate with a denominator of 1.

Practice

Find the answer to these problems using these bathroom tiles. Be sure to reduce if possible. Use a separate sheet of paper if needed.



1.	What is the ratio of yellow shapes to squares?	
2.	What is the ratio of red triangles to total triangles?	
3.	What is the ratio of green triangles to green squares?	
	3 3 1	

- 4. What is the ratio of triangles to squares?5. What is the ratio of triangles to total shapes?
- 6. If the design above has to be repeated multiple times on a bathroom wall to make a border and the final design has 104 total shapes (squares plus triangles), how many triangles are there on the banner? Show your work.
- 7. Dan drove his car for 250 miles and used 10 gallons of gas. Elsie drove her truck for 300 miles and used 20 gallons of gas. DJ drove his motorcycle 120 miles and used up 3 gallons of gas. You can also use the abbreviation "mpg" for miles per gallon. Complete the table below.

Vehicle	Rate	Unit Rate

- 8. If gas costs \$2.30 per gallon, how much did each trip in problem 7 cost? Show your work.
 - a. Dan's trip _____
 - b. Elsie's trip _____
 - c. DJ's trip _____
- 9. A banana bread recipe calls for 1 cup of sugar for every 2 cups of flour. Finish the following table.

Flour (Cups)	Sugar(Cups	Flour and Sugar (Cups)
2	1	3
3		
6		
		12
	5	
		$16\frac{1}{2}$

10. The same recipe above calls for $\frac{1}{4}$ tsp of salt for every 2 cups of flour. If Mr. Baker used $1\frac{1}{2}$ tsp salt, how many cups of flour should he use? Show your work.

- 11. Find each unit rate.
 - a. The average human walks 9 miles in 3 hours.

b. Michael Phelps swims 3 miles in a $\frac{1}{2}$ hour.

c. Katie Ledecky swims 800 meters in about 8 minutes.

d. A gray wolf runs 70 miles in 2 hours.



e. Usain Bolt runs 55 miles in 2 hours.

f. A cheetah runs 245 miles in $3\frac{1}{2}$ hours.



12. Fill in the table below.

Two 8" pizza pies for \$21.90.



Number of Pizza Pies	Cost
1	
2	\$21.90
3	
16	



13. In problem 12, the dependent variable is the "cost" and the independent variable is the "number of pizzas." What do you think is meant by those terms? Explain your thinking. Hint: Think of independent as free to choose what you want. A variable is something that changes.