

We first define a flooding protocol. Given a graph $G = (V, E)$ and a seed vertex $s \in V$. Define the set of vertices F as the vertices which have already been flooded. Initially $F = \{s\}$. In each iteration all vertices in the neighborhood of F but not in F are added to F . This process continues until this neighborhood set is empty. More explicitly, in iteration t we have $F_t = (\cup_{v \in F_{t-1}} N(v)) \cup F_{t-1}$. Note that this is the same setup as the problem of firefighters on graphs.

Consider the problem of adding k edges from s to any vertex in $V \setminus \{s\}$ in order to minimize the number of iterations to the end of the process. On a grid with the seed at the center it is not sufficient to place edges from the seed to any single quadrant center. Four edges must be added, one in each quadrant, in order to decrease the flooding time. By adding all four edges the flooding time can be decreased to $1 +$ the Manhattan distance from the quadrant center to corner.