(ROC - curve (

Example I - Logistic Regression for linearly separable test dataset!

In LR, we wodel P(Y=11x) using a signal function such that:

 $P(\hat{y}=1|x)=O(f(x))=\frac{1}{1+e^{-f(x)}}$ 

In linear logistic regression:

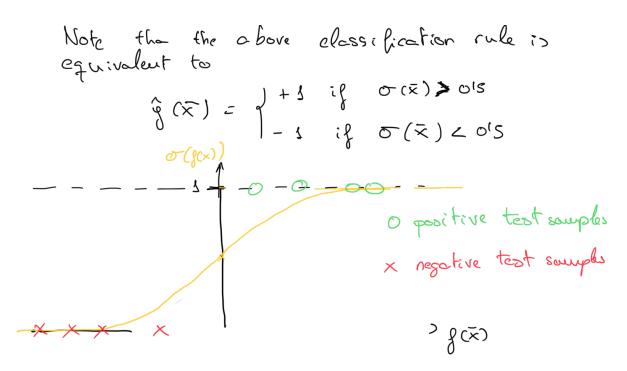
$$\begin{cases}
R^{\frac{1}{4}} & \rightarrow R \\
\bar{\times} & \rightarrow \bar{\times}, \bar{\times}
\end{cases}$$

Using training logistic segression:

Using trainin defeaset  $D_n = (\bar{x}_i, y_i)_{i,i}$ , we find the weight vector with that minimizes the logistic loss, or equivalently, waximizes the likelihood evaluated on the training defa. (Lecture 6).

## - > Evaluating the performance of a classifier!

- We assume that we have trained a LR classifier, which is fully defined by the function  $f(\bar{x}) = \langle \bar{w}^{*}, \bar{x} \rangle$
- We further assume access to a test obtaset  $D_{Test} = (\bar{x}_i, y_i)_{i=1}^{w}$ , which contains mile samples of the measure P over  $X \times Y$ .
- So for, we assumed the we dessify as:  $\hat{y}(\bar{x}) = sign f(x)$



Assuming a classification threshold &=0 (ie. y=signfx we obtain that Error =0 =) Dtest is linearly separable

Question: How do we get the ROC-curve?

top 1 - random classifier

- LR

For D=D => fpr=0 l tpr=1