obtaining online sprp security through an optimal inverse-free construction

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Figure : 2-round feistel encryption

Illustrated are encryption and decryption diagrams for two rounds of feistel. Here, f is an **ideal random function** which is generally implemented by a **blockcipher**.

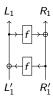


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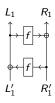


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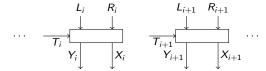
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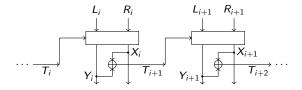
schematic view

a schematic view of OleF

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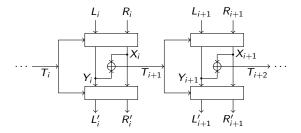


layer 1: sequential encryption, based on 2-round feistel



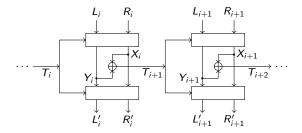
layer 2: mixing and generating tweak for next diblock

a schematic view of OleF



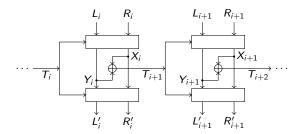
layer 3: parallel encryption, based on 2-round feistel

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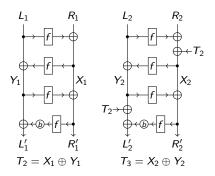
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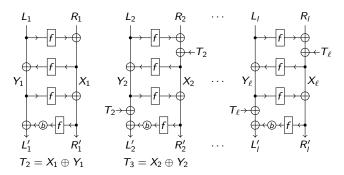
input-diblock 1 is processed to obtain output-diblock 1 and tweak T_2

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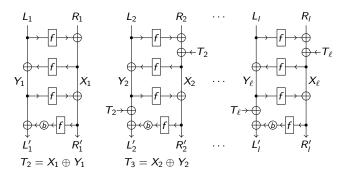
input-diblock 2 is processed using T_2 to obtain output-diblock 2 and tweak T_3

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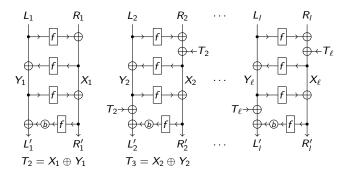
input-diblock ℓ is processed last using T_ℓ to obtain output-diblock ℓ

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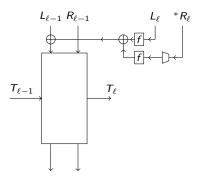
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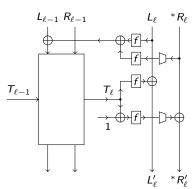
$$\xrightarrow{T_{\ell-1}}$$

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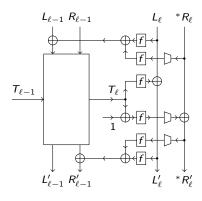
$$\frac{T_{\ell-1}}{T_{\ell-1}}$$



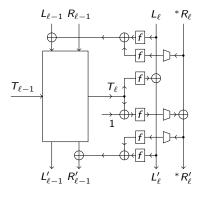
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For authenticated encryption schemes that release unverified plaintext even for invalid ciphertexts, one can desire that this released plaintext reveals nothing about the encryption function that can damage the privacy or authenticity of other encryptions. In a recent work, Huang, Krovatz and Rogaway have come up with a notion of robust authenticated encryption, which can be described by the following distinguishing game:

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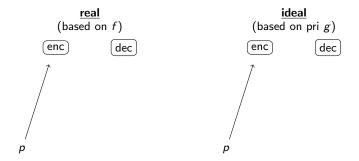
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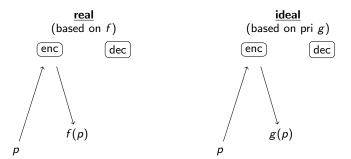
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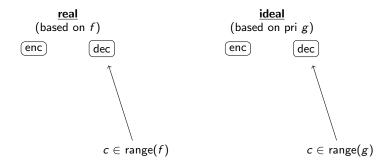
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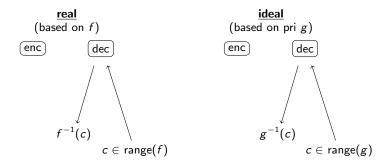
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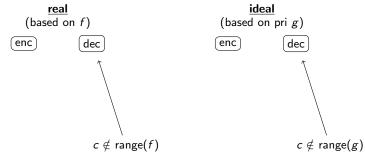
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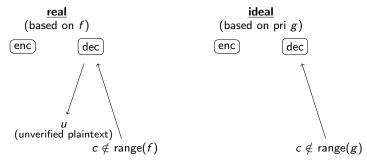


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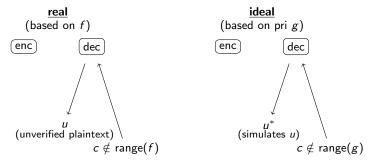
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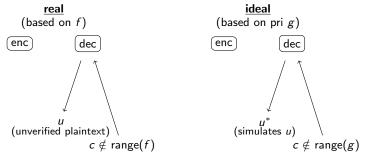
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