

CS 219 – Assignment #5

Purpose: Become familiar with the MIPS architecture instruction formats, floating point data representation issues, and multiplication algorithms

Points: 100

Assignment:

- 1) According to the text (Ch 2), what are the three (3) underlying design principals? [8 pts]

The first of three underlying principles of hardware design is Simplicity favors regularity. The second principle is Smaller is faster. The final hardware design principle is Good design demands good compromises.

- 2) List the two architectural models and describe the key difference each. Include which is the most commonly used. *Note*, not in text. [5 pts]

The two architectural models are the Von Neumann architecture and the Harvard architecture. Von Neumann uses the same memory for instructions and data with a typical memory layout of program/data/stack. Harvard uses different memory for instructions and data. The most commonly used is the Von Neumann architecture.

- 3) List the six possible fields (include the name and meaning) in a MIPS instruction? [8 pts]

The six possible fields in a MIPS instruction are:

- op → operation / op field
- rs → 1st register source
- rd → 2nd register source
- rd → destination register
- shamt → shift amount (for logicals)
- funct → function (variant in op field)

- 4) What are the three basic instruction formats? Show the layout/fields for each. [3 pts]

R format:

- field: op / rs / rt / rd / shamt / funct
- bits: 6 / 5 / 5 / 5 / 5 / 6

I format:

- field: op / rs / rd / address/constant
- bits: 6 / 5 / 5 / 16

J format:

- field: op / address

- 5) Referring to `mips.s` program from assignment #3

Hex: 020d8020

R-format

rs: 10000 \rightarrow 16 \rightarrow register \$16 \rightarrow \$s0

rd: 10000 \rightarrow 16 \rightarrow register \$16 \rightarrow \$s0

funct: 100000 \rightarrow add (20_{hex})

rd: 10000₂ , 16₁₀ , register \$s0

000000/00100/10101/01000/00000/100000

rs: 00100 \rightarrow 4 \rightarrow register \$4 \rightarrow \$a0

rd: 01000 \rightarrow 8 \rightarrow register \$8 \rightarrow \$t0

funct: 100000 \rightarrow add (20_{hex})

7) Given that $x = 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0101\ 1011$, and

a) $x + y$

0000 0000 0000 0000 0000 0000 0101 1011 → 91₁₀

+ 0000 0000 0000 0000 0000 0000 0000 1101 → +13₁₀

0000 0000 0000 0000 0000 0000 0110 1000 $\rightarrow 104_{10}$

b) $x - y \rightarrow (x + (-y))$

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y: 0000 0000 0000 0000 0000 0000 0000 1101

→ decimal: $8+4+1=13_{10}$

→ negative 2's complement:

$$\begin{array}{r} (y): \quad 1111 \ 1111 \ 1111 \ 1111 \ 1111 \ 1111 \ 1111 \ 0010 \\ + \quad 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0001 \\ \hline \end{array}$$

$$(-y): \quad 1111 \ 1111 \ 1111 \ 1111 \ 1111 \ 1111 \ 1111 \ 0011$$

$$\begin{array}{r} (x): \quad 11111 \ 1111 \ 1111 \ 1111 \ 1111 \ 1111 \ 111 \ 11 \\ \quad 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0101 \ 1011 \rightarrow 94_{10} \\ + \quad 1111 \ 1111 \ 1111 \ 1111 \ 1111 \ 1111 \ 1111 \ 0011 \rightarrow -13_{10} \quad :(-y) \\ \hline \quad 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0100 \ 1110 \rightarrow 78_{10} \end{array}$$

- 8) Given that $x = 1111 \ 1111 \ 1111 \ 1111 \ 1001 \ 1011 \ 0011 \ 1110_2$ and $y = 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0110 \ 0010 \ 0101_2$ representing two's complement signed integers, perform the following operations showing all work. [3 pts each]

a) $x + y$

$$\begin{array}{r} \quad \quad \quad 11 \ 11 \quad 111 \ 1 \\ 1111 \ 1111 \ 1111 \ 1111 \ 1001 \ 1011 \ 0011 \ 1110 \rightarrow -25794_{10} \\ + \quad 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0110 \ 0010 \ 0101 \rightarrow +1573_{10} \\ \hline 1111 \ 1111 \ 1111 \ 1111 \ 1010 \ 0001 \ 0110 \ 0011 \rightarrow -24221_{10} \end{array}$$

b) $x - y \rightarrow (x + (-y))$

$$\begin{array}{l} y: 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0110 \ 0010 \ 0101 \\ \rightarrow \text{decimal: } 1+4+32+512+1024=1573_{10} \end{array}$$

→ negative 2's complement:

$$\begin{array}{r} (y): \quad 1111 \ 1111 \ 1111 \ 1111 \ 1111 \ 1001 \ 1101 \ 1010 \\ + \quad 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0001 \\ \hline \end{array}$$

$$(-y): \quad 1111 \ 1111 \ 1111 \ 1111 \ 1111 \ 1001 \ 1101 \ 1011$$

$$\begin{array}{r} (x): \quad 11111 \ 1111 \ 1111 \ 1111 \ 1111 \ 111 \ 1111 \ 11 \\ \quad 1111 \ 1111 \ 1111 \ 1111 \ 1001 \ 1011 \ 0011 \ 1110 \rightarrow -25794_{10} \\ + \quad 1111 \ 1111 \ 1111 \ 1111 \ 1111 \ 1001 \ 1101 \ 1011 \rightarrow +(-1573_{10}) :(-y) \\ \hline \quad 1111 \ 1111 \ 1111 \ 1111 \ 1001 \ 0101 \ 0001 \ 1001 \rightarrow -27367_{10} \end{array}$$

9) Briefly describe what is meant by overflow and underflow conditions that might be produced after a floating point operation (for the exponent). [4 pts]

After shifting the smaller number to the right until its exponent matches the larger exponent, adding the significands, and normalizing the sum by either shifting right and incrementing the exponent or shifting left and decrementing the exponent, we must check for overflow or underflow. This means we make sure that the exponent still fits in its field, such as $127 \geq \text{exponent} \geq -126$.

10) What are the basic elements/steps required for floating point addition? *Note*, answer with a short paraphrased description of each step. [4 pts]

1. Compare the exponents of the two numbers; shift the smaller number to the right until its exponent would match the larger exponent.
2. Add the significands
3. Normalize the sum by either shifting right and incrementing the exponent or shifting left and decrementing the exponent., checking for overflow or underflow.
4. Round the significand to the appropriate number of bits, normalize again if necessary.

11) What are the basic elements/steps required for floating point multiplication? *Note*, answer with a short paraphrased description of each step. [4 pts]

1. Add the biased exponents of the two numbers, subtracting the bias from the sum to get the new biased exponent.
2. Multiply the significands
3. Normalize the product if necessary, shifting it right and incrementing the exponent, and check for overflow or underflow.
4. Round the significand to the appropriate number of bits, normalize again if necessary.
5. Set the sign of the product to positive if the signs of the original operands are the same; if they differ make the sign negative.

12) Given the below data declarations (which are in a provided main):

```
.data
# ----
# Single precision

fval1: .float 9.75
fval2: .float 5.5
fval3: .float 12.25
fval4: .float 3.6

fans1: .float 0.0
fans2: .float 0.0
```

```
fval: .float 0.001
fsum: .float 0.0

# -----
# Double precision

dval1: .double 9.75
dval2: .double 5.5
dval3: .double 12.25
dval4: .double 3.6

dans1: .double 0.0
dans2: .double 0.0

dval: .double 0.001
dsum: .double 0.0
```

Write a simple MIPS program to compute the following floating point formulas:

```
# fans1 = fval1 + fval2
# fans2 = fval3 + fval4
# fsum = 0.0
# do 1000 times
# fsum = fsum + fval

# dans1 = dval1 + dval2
# dans2 = dval3 + dval4
# dsum = 0.0
# do 1000 times
# dsum = dsum + dval
```

Show the displayed results of the program (i.e., console output) and explain. [10 pts]

For this question:

- 1) Submit a copy of the console output (from the log file).
 - a) It is **not** necessary to include the program source or text segment information in the log file.
 - 2) Submit a copy of the source file.
- 13) Perform the following multiplication problems using Booths algorithm (see handout). Assume an 8-bit machine. [8 pts each]

- a) 5×10
- b) 6×7
- c) 17×-6
- d) -14×4