

ABOUT THE % OPERATOR: CALLED MODULUS

- ***THIS OPERATOR RETURNS THE REMAINDER OF TWO NUMBERS.***

FOR INSTANCE $10 \% 3$ IS 1

BECAUSE 10 DIVIDED BY 3 LEAVES A REMAINDER OF 1

YOU MAY REMEMBER WHEN WE FIRST LEARNED ABOUT DIVISION,
WE WORKED WITH INTEGERS AND REMAINDERS,
NOT DECIMAL FRACTIONS.

THE MODULUS OPERATOR % SYMBOLIZES INTEGER DIVISION, BUT RETURNS THE
REMAINDER, NOT THE QUOTIENT.

BELOW SHOWS 4 IS THE QUOTIENT, 2 IS THE REMAINDER, SO THAT:

$14 \% 3 = 2$ (WITH 2 BEING THE REMAINDER OF THE DIVISION)

WHY USING IT?

MODULUS IS USEFUL IN ALL KINDS OF SCENARIOS, ONE OF WHICH IS DETERMINING
DIVISIBILITY.

- ***IF $A \% B == 0$ THEN A IS EVENLY DIVISIBLE BY B.***
- ***IT IS ALSO USEFUL FOR OPEN-ENDED COUNTING***
- ***WHERE WE REPEAT A PATTERN EVERY SO MANY TICKS.***

NOTE THE FOLLOWING:

$14 / 3 = 4.666... \Rightarrow 4 + 0.666...$

$0.666... * 3$ APPROACHES TO 2

$14 - (4 * 3) = 2$

- ***FORTUNATELY, WE DON'T HAVE TO FUSS WITH DECIMAL VALUES, ONLY INTEGER REMAINDERS.***
- ***DIVIDEND MINUS QUOTIENT TIMES MODULUS EQUALS MODULO***
- ***THE DIVISOR IN A MODULAR EXPRESSION IS THE MODULUS.***
- ***THE REMAINDER IN A MODULAR EXPRESSION IS THE MODULO.***

WHY DOES $2 \bmod 4 = 2$?

REMAINDER OF INTEGER DIVISION

BECAUSE $2 = 0 * 4 + 2$

- *IN X/Y RESULTS CONSISTS OF AN INTEGER PART AND A FRACTION PART.*
- *IF YOU MULTIPLY THE FRACTION PART WITH THE DIVISOR, YOU GET THE REMAINDER.*
AND $X = \text{INTEGER PARTY} + \text{REMAINDER (I.E. FRACTION PARTY)}$.
- *IN THIS CASE INTEGER PART IS 0, AND THE REMAINDER IS 2.*

IMPORTANT NOTES:

$2 \% 5 = 2$ ITSELF (REMAINDER OF INTEGER DIVISION)
DO THE DIVISION $2/5 = 0.4$
THEN $2 - [0 * (\text{RESULT}) * 5 \text{ (THE MODULUS)}] = 2$

$2 \% 2 = 0$ ANY NUMBER MODULUS ITSELF IS ZERO
DO THE DIVISION $2/2 = 1$
THEN $2 - (1 * 2) = 0$

$2 \% 1 = 0$ ANY NUMBER MODULUS 1 IS ZERO
DO THE DIVISION $2/1 = 2$
THEN $2 - (2 * 1) = 0$

EXAMPLE:

- SO, $54 \% 23$ MEANS SUBTRACT 23 FROM 54 YOU GET 31.
- THEN 31 IS GREATER
- THAN 23 WE CONTINUE TO SUBTRACT 23 FROM 31 AGAIN
- SUBTRACT $31 - 23$ AND RESULT IS NOW 8. SO 8 IS LESS THAN 24 AND WE STOP.
- HENCE, 8 IS THE REMAINDER.