

5.1

$$\vec{a} = [1, 2, 3]$$

$$\vec{b} = [4, 0, 6]$$

$$A = \begin{vmatrix} 1 & 2 & 3 \end{vmatrix}$$

$$B = \begin{vmatrix} 4 & 0 & 6 \end{vmatrix}$$

$$A+B = \begin{vmatrix} 5 & 2 & 9 \end{vmatrix}$$

$$B-A = \begin{vmatrix} 3 & -2 & 3 \end{vmatrix}$$

$$A \cdot B = \begin{vmatrix} 4 & 0 & 18 \end{vmatrix}$$

$$A^T = \begin{vmatrix} 1 \\ 2 \\ 3 \end{vmatrix} \quad B^T = \begin{vmatrix} 4 \\ 0 \\ 6 \end{vmatrix}$$

2.

3p 7.

5.2

$$\begin{aligned} D &= \begin{vmatrix} 1 & 2 & 3 \\ 4 & 0 & 6 \\ 7 & 8 & 9 \end{vmatrix} = 1 \begin{vmatrix} 0 & 6 \\ 8 & 9 \end{vmatrix} - 2 \begin{vmatrix} 4 & 6 \\ 7 & 9 \end{vmatrix} + 3 \begin{vmatrix} 4 & 0 \\ 7 & 8 \end{vmatrix} = \\ &= 0 - 48 - 2(36 - 42) + 3(32 - 0) = \\ &= 0 - 48 - 2 \cdot (-6) + 3 \cdot 32 = \\ &= -48 + 12 + 96 = 60 \end{aligned}$$

3.

5.3) 1) $A_{11} = 1 \begin{vmatrix} 0 & 6 \\ 8 & 9 \end{vmatrix} = -48$

$A_{12} = -1 \begin{vmatrix} 4 & 6 \\ 7 & 9 \end{vmatrix} = 6$

$A_{13} = 1 \begin{vmatrix} 4 & 0 \\ 7 & 8 \end{vmatrix} = 32$

$A_{21} = - \begin{vmatrix} 2 & 3 \\ 8 & 9 \end{vmatrix} = 6$

$A_{22} = \begin{vmatrix} 1 & 3 \\ 7 & 9 \end{vmatrix} = -12$

$A_{23} = - \begin{vmatrix} 1 & 2 \\ 7 & 8 \end{vmatrix} = 6$

$A_{31} = \begin{vmatrix} 2 & 3 \\ 0 & 6 \end{vmatrix} = 12$

$A_{32} = - \begin{vmatrix} 1 & 3 \\ 4 & 6 \end{vmatrix} = 6$

$A_{33} = \begin{vmatrix} 1 & 2 \\ 4 & 0 \end{vmatrix} = -8$

$A^{-1} = \frac{1}{60} \begin{vmatrix} -48 & 6 & 12 \\ 6 & -12 & 6 \\ 12 & 6 & -8 \end{vmatrix} = \begin{vmatrix} -0,8 & 0,1 & 0,2 \\ 0,1 & -0,2 & 0,1 \\ 0,2 & 0,1 & -0,13 \end{vmatrix}$

2) $A = \begin{vmatrix} 1 & 1 & 1 \\ 2 & 2 & 2 \\ 3 & 3 & 3 \end{vmatrix}$

$M_1 = \begin{vmatrix} 1 & 1 \\ 2 & 2 \end{vmatrix} = 2 - 2 = 0$

$M_2 = \begin{vmatrix} 2 & 2 \\ 3 & 3 \end{vmatrix} = 6 - 6 = 0$

$M_3 = \begin{vmatrix} 1 & 1 \\ 3 & 3 \end{vmatrix} = 3 - 3 = 0$

$\text{rang}(A) = 1$

4, 5

5.4 $(1, 5) ; (2, 8)$

$$\vec{a} \cdot \vec{b} = 1 \cdot 2 + 5 \cdot 8 = 42$$

5.5 $\vec{a} = [1, 5, 0]$

$$\vec{b} = [2, 8, 7]$$

$$\vec{c} = [7, 15, 3]$$

$$\vec{a} \vec{b} \vec{c} = \begin{vmatrix} 1 & 5 & 0 \\ 2 & 8 & 7 \\ 7 & 15 & 3 \end{vmatrix} = 1 \cdot \begin{vmatrix} 8 & 7 \\ 15 & 3 \end{vmatrix} - 5 \cdot \begin{vmatrix} 2 & 7 \\ 7 & 3 \end{vmatrix} =$$

$$= 24 - 10 \cdot 5 - 5 \cdot (-43) = \underline{\underline{229.5}}$$