Parallel Programming

Overview of Parallel and Distributed Programming

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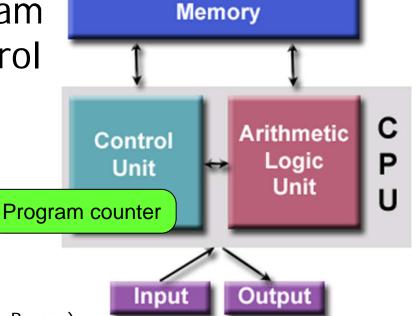
Outline

- The What and Why of Parallel Computing
- The Why and How of Parallel Programming
- Parallel Programming Models
- Performance Evaluation



Sequential Computing

- von Neumann arch. with Program Counter (PC) dictates sequential execution
- Traditional programming thus follows a single thread of control
 - The sequence of program points reached as control flows through the program



(Introduction to Parallel Computing, Blaise Barney)

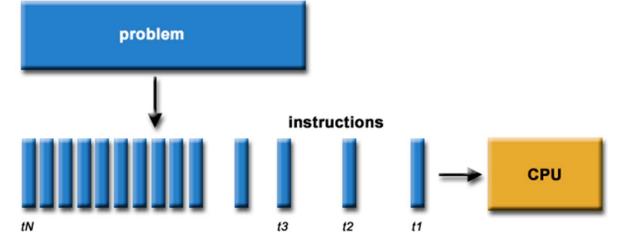


Sequential Computing (Cont'd)

- Traditionally, software has been written for serial computing:
 - To be run on a single computer having a single CPU
 - A problem is broken into a discrete series of instructions
 - Instructions are executed one after another

Only one instruction may execute at any moment in

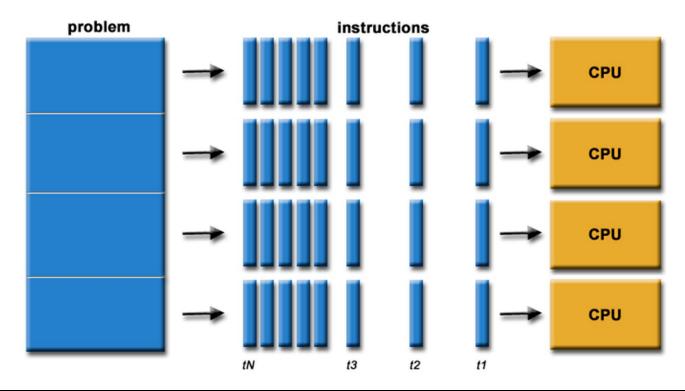
time





What is Parallel Computing?

In the simplest sense, parallel computing is the simultaneous use of multiple compute resources to solve a computational problem





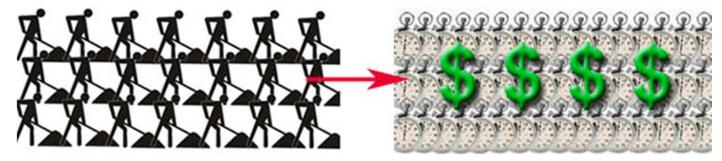
Concurrent, Parallel, and Distributed Computing

- Although there isn't complete agreement on the distinction between these terms, many authors make the following distinctions:
 - Concurrent computing: A program is one in which multiple tasks can be in progress at any instant
 - Parallel computing: A program is one in which multiple tasks cooperate closely to solve a problem
 - Distributed computing: A program may need to cooperate with other programs to solve a problem



Why Use Parallel Computing? (1/3)

- Save time and/or money
 - In theory, throwing more resources at a task will shorten its time to completion, with potential cost savings
 - Parallel computers can be built from cheap, commodity components



- Time to brute force a 56-bit DES key has evolved from
 - 1998, 56 hours, \$250,000
 - 2006, 6.4 hours, \$10,000





Why Use Parallel Computing? (2/3)

- Solve larger problems (applications demand it!)
 - Many problems are so large and/or complex that it is impractical or impossible to solve them on a single computer, especially given limited computer memory
 - Largest direct numerical solutions have evolved from meshes of 10243 to 80963 in the last ten years!
 - E.g., climate modeling, drug discovery, energy research, data analysis
 - Big data drivers





More Devices

New & Better

Information

Big Data Phenomenon

"Data are becoming the new raw material of business: an economic input almost on a par with capital and labor."

—The Economist, 2010

"Information will be the oil of the 21st century"

-Gartner, 2010

1.8ZB in 2011 2 Days > the dawn of

civilization to 2003



750 Million

Photos uploaded to Facebook in 2 days



966PB Stored in US manufacturing (2009)



209 Billion

RFID tags sale in 2021: from 12 million in 2011



200+TB
A boy's 240'000 hours by a MIT Media Lab geek



200PB Storage of a Smart City project in China



\$800B

in personal location data within 10 years



\$300B /year
US healthcare saving from Big Data



\$32+B
Acquisitions by 4 big players since 2010





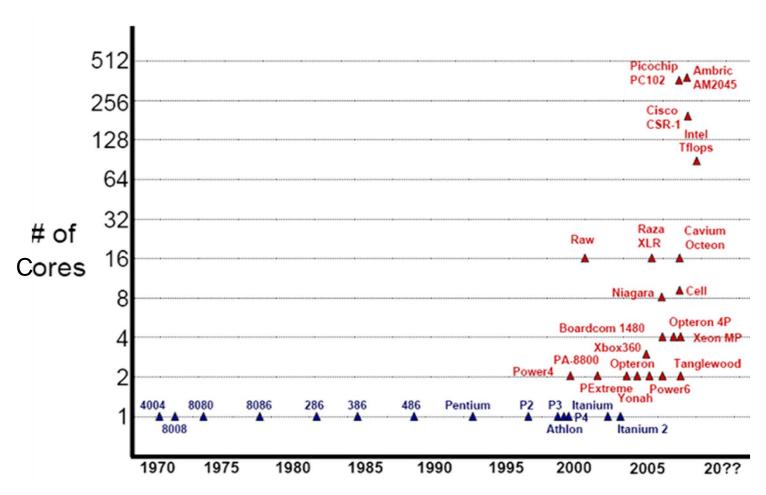
Source: IDF2012

Why Use Parallel Computing? (3/3)

- Architectures demand it!
 - The free lunch is over
 - Clock speed increase is no longer an option
 - Multiple/many cores are future trend
 - Simply adding more processors will not magically improve the performance of the vast majority of serial programs



Multicore Trends



(Source) MIT Course 6.189, "Multi-core Programming Primer: Learn and Compete in Programming the PLAYSTATION®3 Cell Processor."

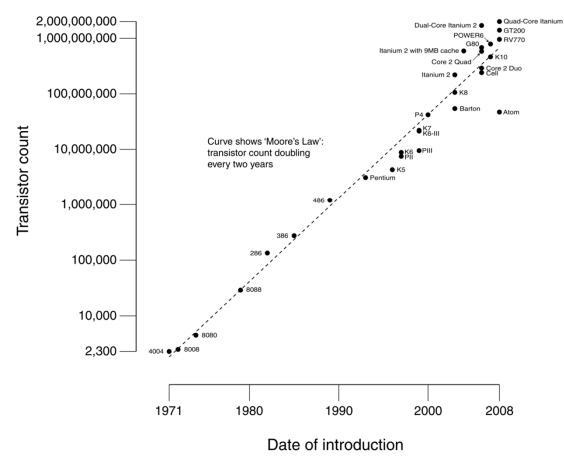


Moore's Law



- Describes a trend in the history of computer hardware that the number of transistors can be inexpensively placed on an integrated circuit is increasing exponentially
 - Doubling every 18 month (Moore's original predication)
 - Doubling approximately every two years (actual growth of processors)

CPU Transistor Counts 1971-2008 & Moore's Law

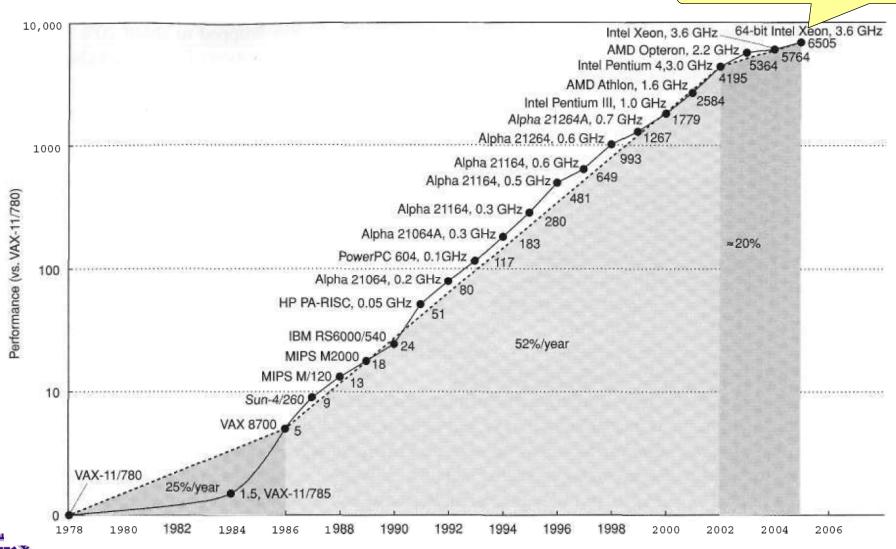






Semiconductor Trends

Curve gets flatten

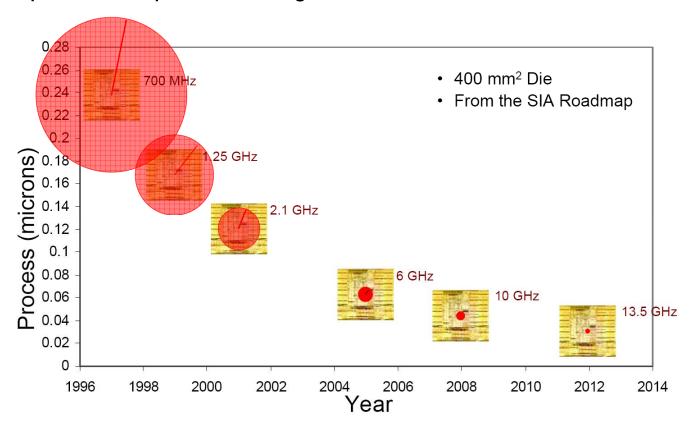




(Source) Hennessy & Patterson, Computer Architecture: A Quantitative Approach, 4th edition, Oct., 2006

Challenges: Wire Delay becomes issue when clock rate raised

- The signal delay for a wire increases in proportion to the product of its resistance and capacitance (R*C)
 - Feature size shrinks → shorter wires → higher resistance and capacitance per unit length

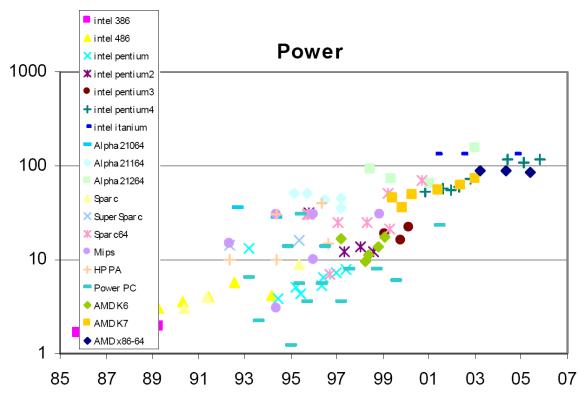




(Source) MIT Course 6.189, "Multi-core Programming Primer: Learn and Compete in Programming the PLAYSTATION®3 Cell Processor."

Challenges: Power Consumption

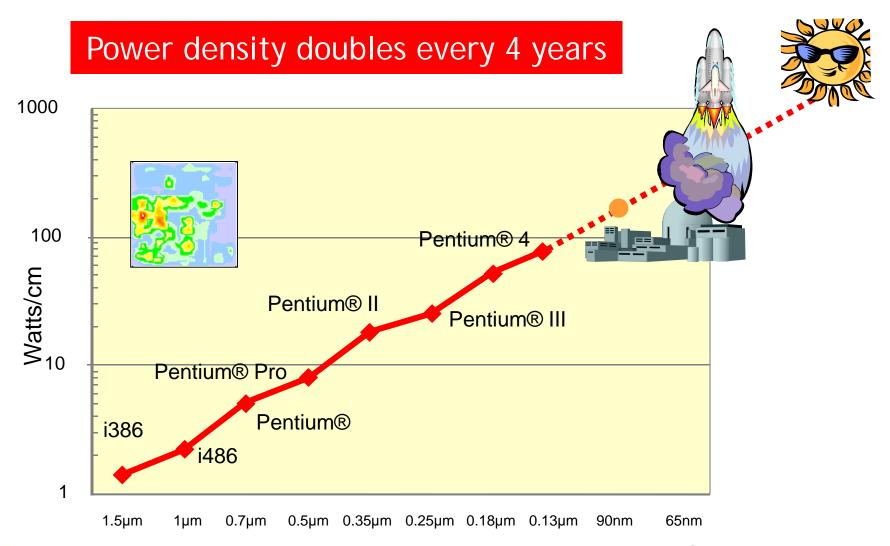
- Power consumption becomes a problem:
 - Operation energy of transistors (cost, environment)
 - Heat dissipation reaching its limitation (cooling, space, cost)





(Source) MIT Course 6.189, "Multi-core Programming Primer: Learn and Compete in Programming the PLAYSTATION®3 Cell Processor."

Power Density Trend





Source: Intel

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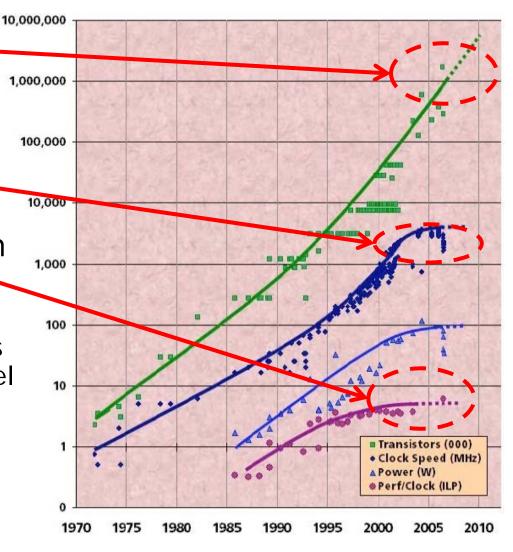


Why We Need to Write Parallel Programs?

- Most programs that have been written for single-core systems cannot exploit the presence of multiple cores
- The bad news is that researchers have had very limited success writing programs that convert serial programs in languages such as C and C++ into parallel programs

Limiting Forces: Clock Speed and ILP

- Chip density is continuing increase ~2x every 2 years
 - # processors/chip (cores) may double instead
- Clock speed is not
- There is little or no more instruction-level parallelism (ILP) to be found
 - Can no longer allow programmer to think in terms of a serial programming model
- Conclusion:
 - Parallelism must be exposed to software!





Source: Intel, Microsoft (Sutter) and Stanford (Olukotun, Hammond)

Parallelizing A Program: An Example

- As an example, suppose that we need to compute n values and add them together
- We know that this can be done with the following serial code:

```
sum = 0;
for (i = 0; i < n; i++) {
    x = Compute_next_value(. . .);
    sum += x;
}</pre>
```



Partitioning Step

Now suppose we also have p cores and p is much smaller than n. Then each core can form a partial sum of approximately n=p values:

```
my_sum = 0;
my_first_i = . . .;
my_last_i = . . .;
for (my_i = my_first_i; my_i < my_last_i; my_i++) {
    my_sum += my_x;
}
my_n = n/p;
my_first_i = my_n * my_rank;
my_last_i = my_first_i + my_n;
my_last_i; my_i++) {
    my_sum += my_x;
}
```

Here the prefix my indicates that each core is using its own, private variables, and each core can execute this block of code independently of the other cores

An Example

For example, if there are eight cores, n = 24, and the 24 calls to Compute next value return the values

1,4,3, 9,2,8, 5,1,1, 6,2,7, 2,5,0, 4,1,8, 6,5,1, 2,3,9,

Then the values stored in my sum might be

Core	0	1	2	3	4	5	6	7
my_sum	8	19	7	15	7	13	12	14

When the cores are done computing their values of my_sum, they can form a global sum by sending their results to a designated "master" core, which can add their results



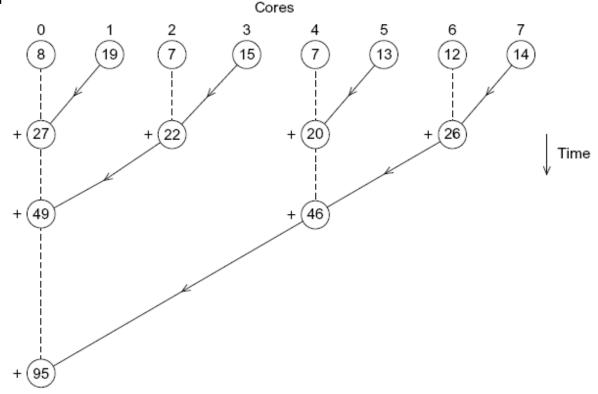
Aggregation Step

If the master core is core 0, it would add the values 8+19+7+15+7+13+12+14 = 95

```
if (I'm the master core) {
    sum = my_x;
    for each core other than myself {
        receive value from core;
        sum += value;
    }
} else {
    send my_x to the master;
}
```

A Better Aggregation

Instead of making the master core do all the work of computing the final sum, we can pair the cores so that while core 0 adds in the result of core 1, core 2 can add in the result of core 3, core 4 can add in the result of core 5 and so on



Comparison between Two Aggregation Methods

- With eight cores, the master will carry out seven receives and adds using the first method, while with the second method it will only carry out three
- The difference becomes much more dramatic with large numbers of cores
 - With 1000 cores, the first method will require 999 receives and adds, while the second will only require 10, an improvement of almost a factor of 100!

Writing Parallel Software to Exploit Parallelism

- The point here is that it's unlikely that a translation program would "discover" the second global sum
- We cannot simply continue to write serial programs
- We must write parallel programs that exploit the power of multiple processors

How Do We Write Parallel Programs?

- There are two widely used approaches:
 - Task-parallelism
 - We partition the various tasks carried out in solving the problem among the cores
 - 2) Data-parallelism
 - We partition the data used in solving the problem among the cores, and each core carries out more or less similar operations on its part of the data
- The theme of the course focuses on data parallelism, which mostly exists within loops



How Do We Write Parallel Programs?

- Currently, the most powerful parallel programs are written using explicit parallel constructs
- They are written using extensions to languages such as C and C++
 - These programs include explicit instructions for parallelism

Coordination

In both global sum examples, the coordination involves three types:

1) Communication

One or more cores send their current partial sums to another core

Load Balancing

We want the cores all to be assigned roughly the same number of values to compute

3) Synchronization

Sometimes we want that each core will wait until all the cores have entered a given point



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Parallel Programming Models

 Programming model is made up of the languages and libraries that create an abstract view of the machine

Control

- How is parallelism created?
- What orderings exist between operations?

Data

- What data are private vs. shared?
- How is logically shared data accessed or communicated?

Synchronization

- What operations can be used to coordinate parallelism?
- What are the atomic (indivisible) operations?

Cost

How do we account for the cost of each of the above?



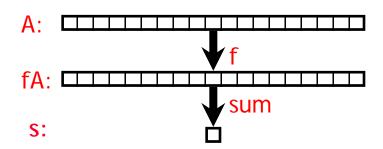
Simple Example of Data Parallelism

Consider applying a function f to the elements of an array A and then computing its sum:

$$\sum_{i=0}^{n-1} f(A[i])$$

Questions:

- Where does A live? All in single memory? Partitioned?
- What work will be done by each processors?
- They need to coordinate to get a single result, how?





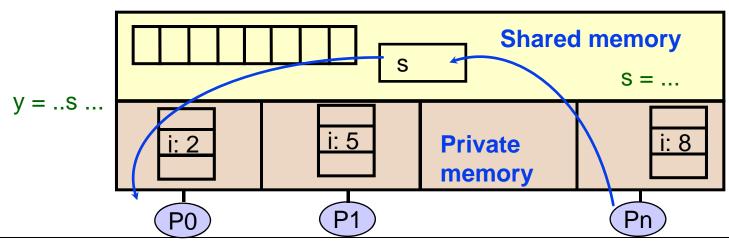
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Programming Model 1: Shared Memory

- Program is a collection of threads of control
 - Can be created dynamically, mid-execution, in some languages
- Each thread has a set of private variables, e.g., local stack variables
- Also a set of shared variables, e.g., static variables, shared common blocks, or global heap
 - Threads communicate implicitly by writing and reading shared variables
 - Threads coordinate by synchronizing on shared variables





Simple Example of Data Parallelism

- Shared memory strategy:
 - small number p << n=size(A) processors</p>
 - attached to single memory

 $\sum_{i=0}^{n-1} f(A[i])$

- Parallel decomposition:
 - Each evaluation and each partial sum is a task
- Assign n/p numbers to each of p procs
 - Each computes independent "private" results and partial sum
 - Collect the p partial sums and compute a global sum

Two Classes of Data:

- Logically Shared
 - The original n numbers, the global sum
- Logically Private
 - The individual function evaluations
 - What about the individual partial sums?



Shared Memory "Code" for Computing a Sum

```
fork(sum,a[0:n/2-1]);
sum(a[n/2,n-1]);
```

static int s = 0;

Thread 1

for
$$i = 0$$
, $n/2-1$
 $s = s + f(A[i])$

Thread 2

for
$$i = n/2, n-1$$

 $s = s + f(A[i])$

- What is the problem with this program?
- A race condition or data race occurs when:
 - Two processors (or two threads) access the same variable, and at least one does a write
 - The accesses are concurrent (not synchronized) so they could happen simultaneously



An Example of Race Condition

A=
$$\begin{bmatrix} 3 & 5 \end{bmatrix}$$
 f (x) = x² static int s = 0;

```
Thread 1
                                          Thread 2
                                     9
                                                                              25
 compute f([A[i]) and put in reg0
                                           compute f([A[i]) and put in reg0
 reg1 = s
                                           reg1 = s
                                     0
 reg1 = reg1 + reg0
                                           reg1 = reg1 + reg0
                                                                              25
 s = reg1
                                           s = reg1
                                     9
                                                                              25
```

- Assume A = [3,5], $f(x) = x^2$, and s=0 initially
- For this program to work, s should be $3^2 + 5^2 = 34$ at the end
 - but it may be 34, 9, or 25
- The atomic operations are reads and writes
 - Never see ½ of one number, but += operation is not atomic
 - All computations happen in (private) register



Improved Code for Computing a Sum

```
static int s = 0;
static lock lk;
```

Why not do lock inside loop?

```
Interest 1

local_s1= 0

for i = 0, n/2-1

local_s1 = local_s1 + f(A[i])

lock(lk);

s = s + local_s1

unlock(lk);
```

```
Thread 2

local_s2 = 0
for i = n/2, n-1
    local_s2 = local_s2 + f(A[i])
lock(lk);
s = s +local_s2
unlock(lk);
```

- Since addition is associative, it's OK to rearrange order
- Most computation is on private variables
 - Sharing frequency is also reduced, which might improve speed
 - But there is still a race condition on the update of shared s
 - The race condition can be fixed by adding locks (only one thread can hold a lock at a time; others wait for it)



POSIX Threads

- POSIX: Portable Operating System Interface for UNIX
 - Interface to Operating System utilities
- Pthreads: The POSIX threading interface
 - System calls to create and synchronize threads
 - Should be relatively uniform across UNIX-like OS platforms
 - Originally IEEE POSIX 1003.1c
- Pthreads contain support for
 - Creating parallelism
 - Synchronizing
 - No explicit support for communication, because shared memory is implicit; a pointer to shared data is passed to a thread
 - Only for static variables and HEAP! Stacks not shared



Pthreads Example: Hello World

```
void* SayHello(void *foo) {
    printf( "Hello, world!\n" );
    return NULL;
int main() {
    pthread t threads[16];
    int tn;
    for(tn=0; tn<16; tn++) {
        pthread create(&threads[tn], NULL, SayHello, NULL);
    for(tn=0; tn<16; tn++) {
        pthread join(threads[tn], NULL);
    return 0;
```



Shared Data and Threads

- Variables declared outside of main are shared
- Objects allocated on the heap may be shared (if pointer is passed)
- Variables on the stack are private: passing pointer to these around to other threads can cause problems
- Often done by creating a large "thread data" struct, which is passed into all threads as argument



OpenMP

C\$OMP FLUSH

#pragma omp critical

OpenMP: An API for Writing Multithreaded

CSOMP Applications

C\$OMP

A set of compiler directives and library routines for parallel application programmers

C\$OM

Makes writing multi-threaded applications in Fortran, C and C++ as easy as we can make it

C\$C

Standardizes last 20 years of SMP practice

#pra

C\$OMP PARALLEL COPYIN(/blk/)

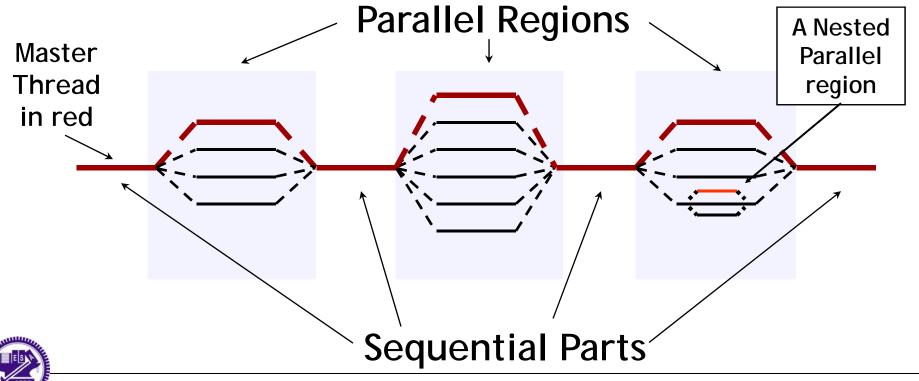
C\$OMP DO lastprivate(XX)



ED

OpenMP Execution Model:

- Fork-Join Parallelism:
 - Master thread spawns a team of threads as needed
 - Parallelism added incrementally until performance are met: i.e. the sequential program evolves into a parallel program



OpenMP Example: Hello World

Write a multithreaded program where each thread prints "hello world"

```
void main() {
    printf(" hello(%d) ", ID);
    printf(" world(%d) \n", ID);
```



OpenMP Example: Hello World

Tell the compiler to pack code into a function, fork the threads, and join when done ...

```
#include "omp.h"
void main() {
#pragma omp parallel
     int ID = omp get thread num();
     printf(" hello(%d) ", ID);
    printf(" world(%d) \n", ID);
                                     Sample Output:
                                     hello(1) hello(0) world(1)
                                     world(0)
                                     hello(3) hello(2) world(3)
                                     world(2)
```



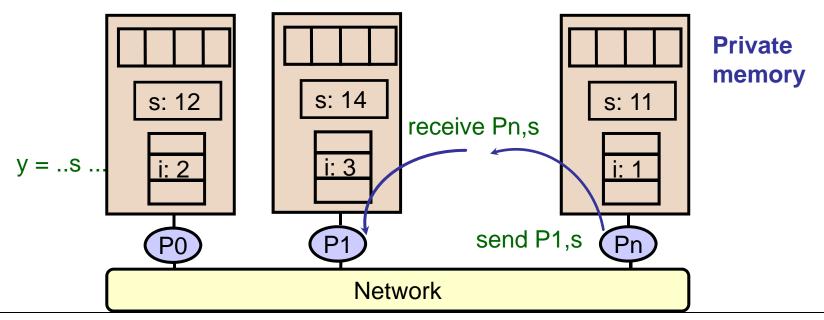
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Programming Model 2: Message Passing

- Program consists of a collection of named processes
 - Usually fixed at program startup time
 - Thread of control plus local address space -- NO shared data
 - Logically shared data is partitioned over local processes
- Processes communicate by explicit send/receive pairs
 - Coordination is implicit in every communication event
 - MPI (Message Passing Interface) is the most commonly used SW



Computing s = f(A[1])+f(A[2]) on each processor

° First possible solution - what could go wrong?

```
Processor 1
xlocal = f(A[1])
send xlocal, proc2
receive xremote, proc2
s = xlocal + xremote
```

```
Processor 2
xlocal = f(A[2])
send xlocal, proc1
receive xremote, proc1
s = xlocal + xremote
```

- ° If send/receive acts like the telephone system? The post office?
- Second possible solution

```
Processor 1
xlocal = f(A[1])
send xlocal, proc2
receive xremote, proc2
s = xlocal + xremote
```

Processor 2
 xlocal = f(A[2])
 receive xremote, proc1
 send xlocal, proc1
 s = xlocal + xremote

MPI - the de facto standard

- MPI has become the de facto standard for parallel computing using message passing
- Example:

```
for (i=1;i<numprocs;i++) {
    sprintf(buff, "Hello %d! ", i);
    MPI_Send(buff, BUFSIZE, MPI_CHAR, i, TAG, MPI_COMM_WORLD);
}
for(i=1;i<numprocs;i++) {
    MPI_Recv(buff, BUFSIZE, MPI_CHAR, i, TAG, MPI_COMM_WORLD, &stat);
    printf("%d: %s\n", myid, buff);
}</pre>
```

- Pros and Cons of standards
 - MPI created finally a standard for applications development in the HPC community portability
 - The MPI standard is a least common denominator building on mid-80s technology, so may discourage innovation



Which is better? SM or MP?

- Which is better, Shared Memory or Message Passing?
 - Depends on the program!
 - Both are "communication Turing complete"
 - i.e. can build Shared Memory with Message Passing and vice-versa
- Advantages of Shared Memory
 - Implicit communication (loads/stores)
 - Low overhead when cached
- Disadvantages of Shared Memory
 - Complex to build in way that scales well
 - Requires synchronization operations
 - Hard to control data placement within caching system
- Advantages of Message Passing
 - Explicit Communication (sending/receiving of messages)
 - Easier to control data placement (no automatic caching)
- Disadvantages of Message Passing
 - Message passing overhead can be quite high
 - More complex to program
 - Introduces question of reception technique (interrupts/polling)



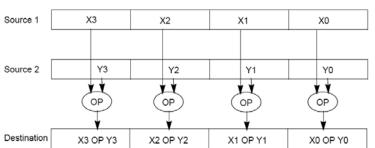
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Programming Model 3: Data Parallel

- Single thread of control consisting of parallel operations
 - A = B + C could mean adding two arrays in parallel
- Parallel operations applied to all (or a defined subset) of a data structure, usually an array
 - Communication is implicit in parallel operators
 - Elegant and easy to understand and reason about
 - Coordination is implicit statements executed synchronously
 - Similar to Matlab language for array operations
- Drawbacks:
 - Not all problems fit this model
 - Difficult to map onto coarse-grained machines



Vector/SIMD operations



What about GPU and Cloud?

- GPU's big performance opportunity is data parallelism
 - Most programs have a mixture of highly parallel operations, and some not so parallel
 - GPUs provide a threaded programming model (CUDA) for data parallelism to accommodate both
 - Current research attempting to generalize programming model to other architectures, for portability (OpenCL)

- Cloud computing allows large numbers of people easily share O(105) machines
 - MapReduce was first programming model: data parallel on distributed memory
 - More flexible models (Hadoop...) invented since then

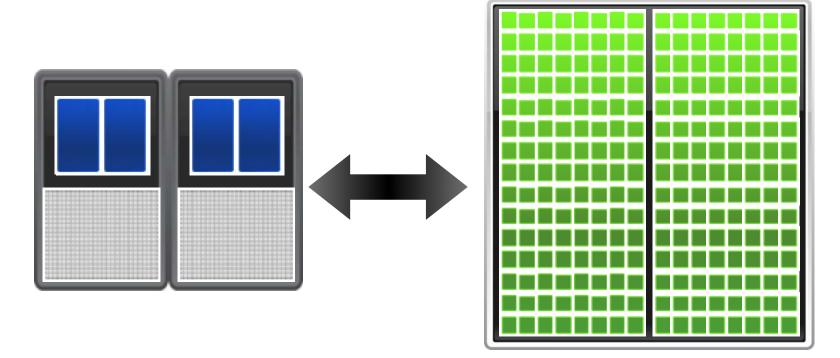


O NVIDIA



OpenCL

CPU-GPU: Heterogeneous Parallel Computing



Latencyoptimized CPU

Fast serial processing

Throughputoptimized GPU

Scalable parallel processing



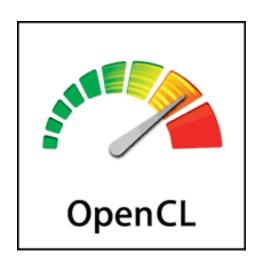
CUDA (Compute Unified Device Architecture)

- Data-parallel programming interface to GPU
 - Data to be operated on is discretized into independent partition of memory
 - Each thread performs roughly same computation to different partition of data
- Programmer expresses
 - Thread programs to be launched on GPU, and how to launch
 - Data organization and movement between host and GPU
 - Synchronization, memory management, ...
- CUDA is one of first to support heterogeneous architectures (more later in the semester)



OpenCL

- Open Computing Language
- A framework for writing programs that execute across heterogeneous platforms consisting of CPUs, GPUs and other processors



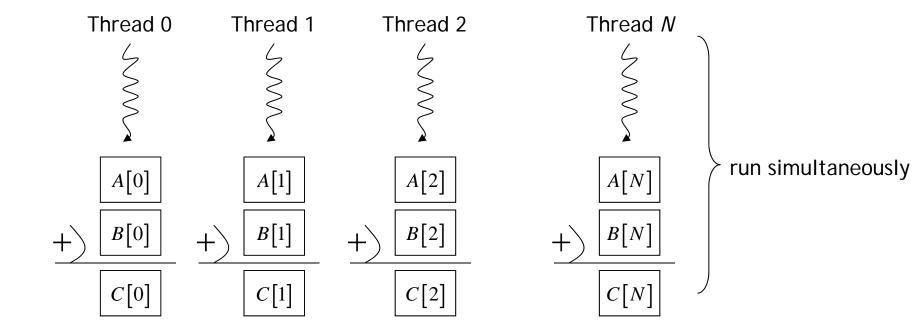
CUDA Example: Vector Add

```
int main() {
 int A[] = {...};
  int B[] = \{...\};
                                    Sequential version
 for (i = 0; i < N; i++) {
   C[i] = A[i] + B[i];
global void vecAdd(int A[], int B[], int C[]) {
  int i = threadIdx.x;
 C[i] = A[i] + B[i];
int main() {
  int hA[] = {...};
  int hB[] = \{...\};
                                                            Parallel version
  cudaMemcpy(dA, hA, sizeof(hA), HostToDevice);
  cudaMemcpy(dB, hB, sizeof(hB), HostToDevice);
 vecAdd<<<1, N>>>(dA, dB, dC);
  cudaMemcpy(dA, hA, sizeof(hA), DeviceToHost);
```



CUDA Example: Vector Add

```
__global__ void vecAdd(int A[], int B[], int C[]) {
  int i = threadIdx.x;
  C[i] = A[i] + B[i];
}
```





MapReduce

- MapReduce is a programming model for processing large data sets with a parallel, distributed algorithm on a cluster
- The model is inspired by the map and reduce functions commonly used in functional programming

Map and Reduce

Map

- The master node takes the input, divides it into smaller subproblems, and distributes them to worker nodes
- The worker node processes the smaller problem, and passes the answer back to its master node

Map function:

$$(K_{in'}, V_{in}) \rightarrow list < (K_{inter'}, V_{inter}) >$$

Reduce

The master node then collects the answers to all the subproblems and combines them in some way to form the output, the answer to the problem it was originally trying to solve

Reduce function:

$$(K_{inter'} list < V_{inter} >) \rightarrow list < (K_{out'} V_{out}) >$$

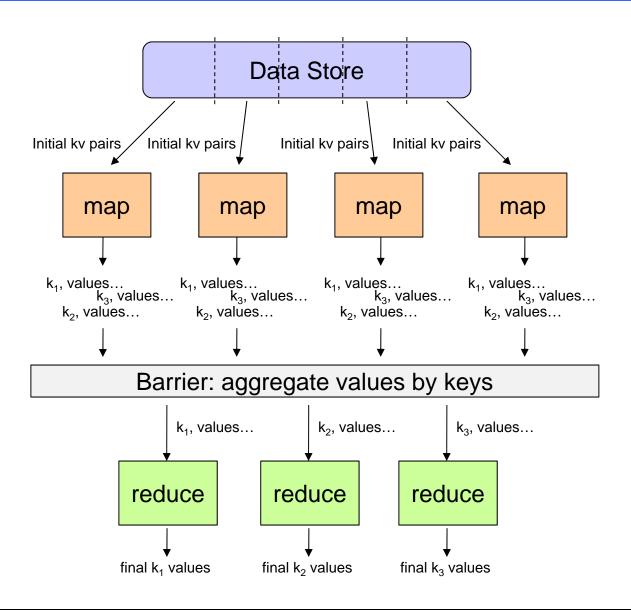


Typical Problem

- Iterate over a large number of records
- Map: extract something of interest from each
- Shuffle and sort intermediate results
- Reduce: aggregate intermediate results
- Generate final output

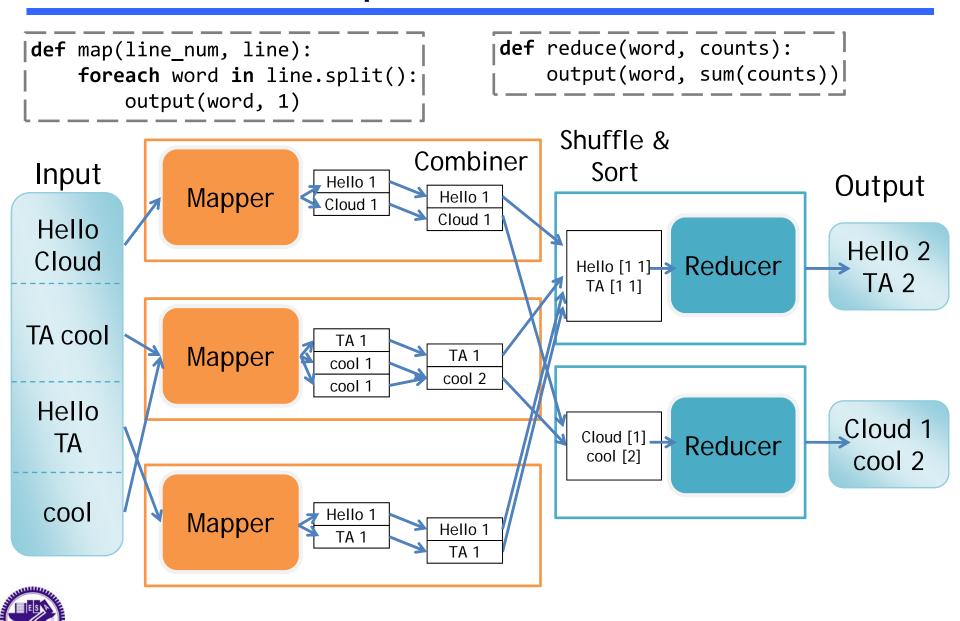
Key idea: provide an abstraction at the point of these two operations

It's just divide and conquer!





Example: Word Count



Hadoop

- Hadoop (High-availability distributed objectoriented platform)
- An open-source software framework that supports data-intensive distributed applications
- Distributed File System (HDFS)
 - Runs on same machines
 - Replicates data 3x for fault-tolerance
- It supports the running of applications on large clusters of commodity hardware





Hadoop

- Hadoop was derived from Google's MapReduce and Google File System (GFS) papers
- Hadoop is written in the Java programming language

Remark

- Three basic conceptual models
 - Shared memory
 - Distributed memory
 - Data parallel and hybrids of these models
- All of these models rely on dividing up work into parts that are:
 - Mostly independent (little synchronization)
 - About same size (load balanced)
 - Have good locality (little communication)



Outline

- The What and Why of Parallel Computing
- The Why and How of Parallel Programming
- Parallel Programming Models
- Performance Evaluation



Performance

- Of course our main purpose in writing parallel programs is usually increased performance
- So what can we expect? And how can we evaluate our programs?
 - Speedup
 - Efficiency
 - Scalability



Speedup

- We run our program with p cores, one thread or process on each core, then our parallel program will run p times faster than the serial program
- When this happens, we say that our parallel program has linear speedup

Speedup

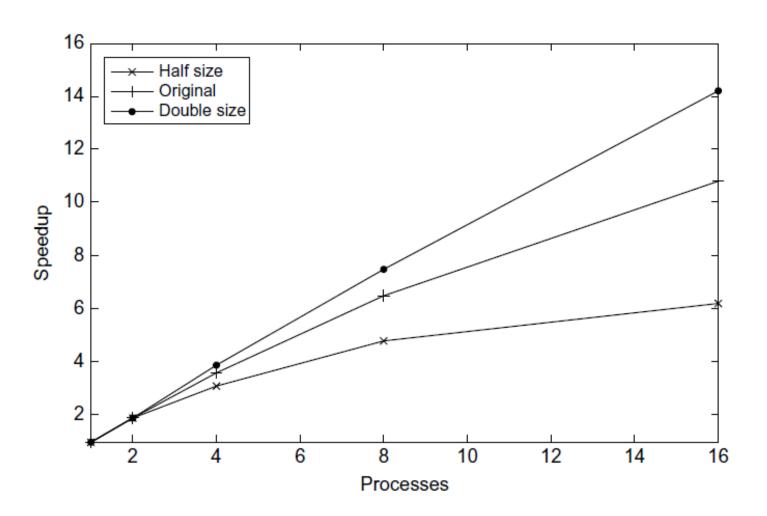
- In practice, we're unlikely to get linear speedup because the use of multiple processes almost invariably introduces some overhead
- We define the speedup of a parallel program to be:

$$S = \frac{T_{\text{serial}}}{T_{\text{parallel}}}$$

Then linear speedup has S = p



Speedup



Speedups of parallel program on different problem sizes

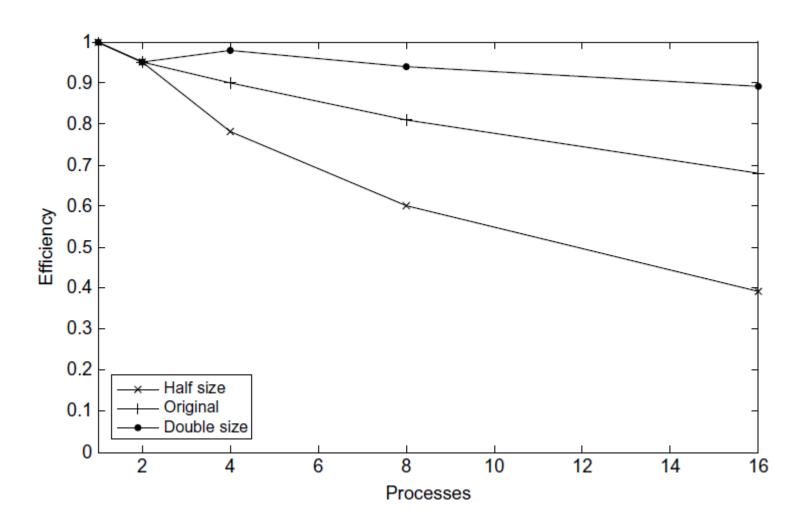


Efficiency

S/p, is sometimes called the efficiency of the parallel program

$$E = \frac{S}{p} = \frac{\left(\frac{T_{\text{serial}}}{T_{\text{parallel}}}\right)}{p} = \frac{T_{\text{serial}}}{p \cdot T_{\text{parallel}}}$$

Efficiency



Efficiencies of parallel program on different problem sizes



Scalability

If we increase the problem size at the same rate that we increase the number of processes/threads, then the efficiency will be unchanged, and our program is scalable



AUTO'SCALE'



Grows without requiring developers to re-architect their algorithms/applications

Strongly Scalable and Weakly Scalable

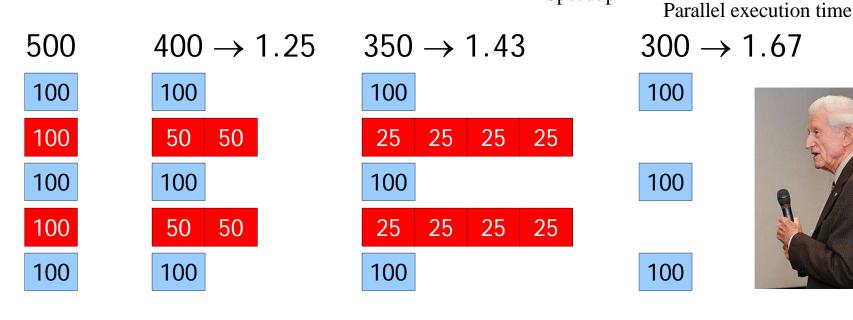
- There are a couple of cases that have special names:
 - 1) Strongly scalable
 - When we increase the number of processes/threads, we can keep the efficiency fixed without increasing the problem size
 - 2) Weakly scalable
 - We can keep the efficiency fixed by increasing the problem size at the same rate as we increase the number of processes/threads

A Word of Warning

- Every parallel program contains at least one serial program
- Since we almost always need to coordinate the actions of multiple cores, writing parallel programs is almost always more complex than writing a serial program that solves the same problem

Amdahl's Law

The speedup of a program using multiple processors in parallel computing is limited by the time needed for the sequential fraction of the program Sequential execution time Speedup =



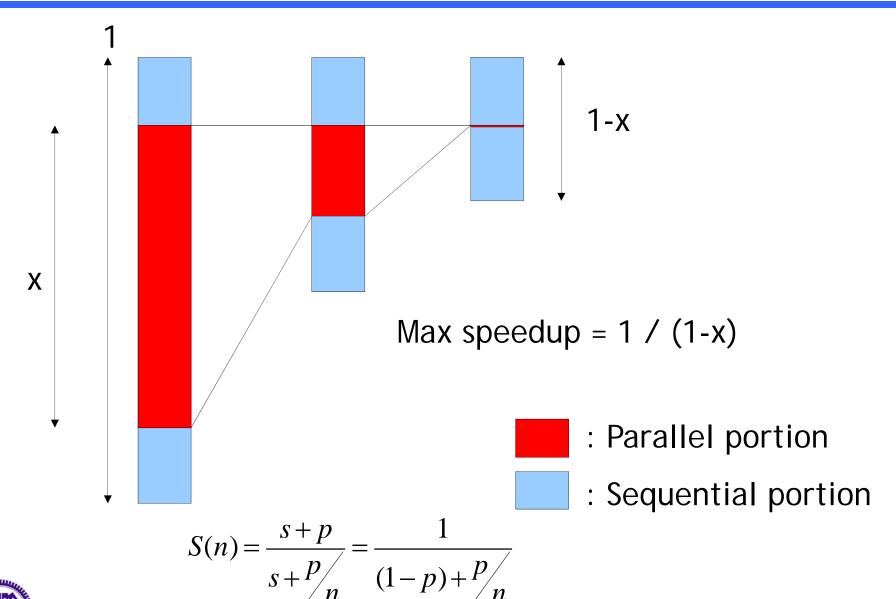


: Parallel portion

: Sequential portion

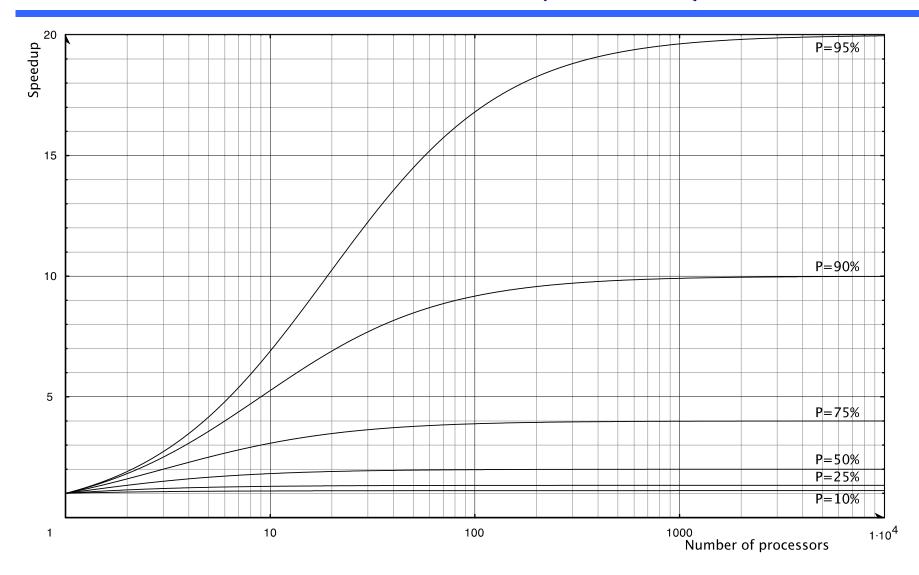


Amdahl's Law (Cont'd)



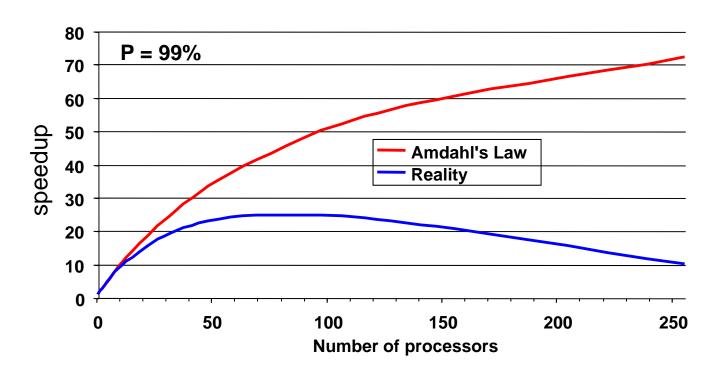


Amdahl's Law (Cont'd)





Amdahl's Law vs Reality



- Amdahl's Law provides a theoretical upper limit on parallel speedup assuming that there are no costs for communications
 - In reality, communications will result in a further degradation of performance



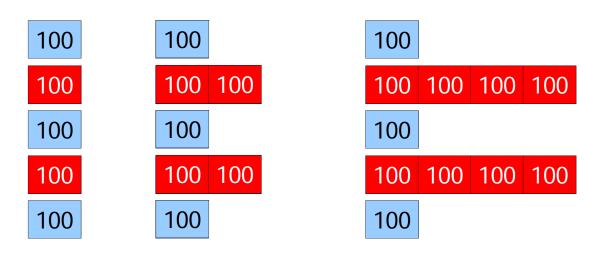
More on Amdahl's Law

- Amdahl's Law works on a fixed problem size
 - This is reasonable if your only goal is to solve a problem faster
 - What if you also want to solve a larger problem?
- Gustafson's Law:
 - The proportion of the computations that are sequential normally decreases as the problem size increases



Gustafson's Law

- Rather than assume that the problem size is fixed, assume that the parallel execution time is fixed
 - In increasing the problem size, Gustafson also makes the case that the serial section of the code does not increase as the problem size





Scaled speedup

$$S_s(n) = \frac{s+np}{s+p} = s+np = (1-p)+np = 1+(n-1)p$$



Example of Gustafson's Law

- Suppose a parallel section of 95% and 20 processors; the speedup according to the formula is 19.05 instead of 10.26 according to Amdahl's law
 - Note, however, the different assumptions

$$S(n) = \frac{1}{(1-p) + \frac{p}{n}} = \frac{1}{0.05 + 0.95/20} \approx 10.26$$

$$S_s(n) = 1 + (n-1)p = 1 + (20-1)*0.95 = 19.05$$

Summary

- In order to increase the power of processors, chipmakers have turned to multicore integrated circuits
- Ordinary serial programs usually cannot exploit the presence of multiple cores

Summary

- When we write parallel programs, we usually need to coordinate the work of the cores. This can involve communication among the cores, load balancing, and synchronization of the cores
- Parallel programs are usually very complex. So it's even more important to use good program development techniques with parallel programs

References

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