$$V(k_0) = \sum_{t=0}^{\infty} \left[\beta^t \ln(1 - \alpha \beta) + \beta^t \alpha \ln k_t \right]$$

$$= \frac{1}{1 - \alpha \beta} \sum_{t=0}^{\infty} \left[\frac{1 - (\alpha \beta)^t}{1 - \alpha \beta} \ln \alpha \beta + \alpha^t \ln k_0 \right]$$

$$= \frac{\alpha}{1 - \alpha \beta} \sum_{t=0}^{\infty} \left[\frac{\beta^t}{1 - \alpha} - \frac{(\alpha \beta)^t}{1 - \alpha} \right]$$

$$= \frac{\alpha}{1 - \alpha} \ln k_0 + \frac{\ln(1 - \alpha \beta)}{1 - \alpha} + \frac{\alpha \beta}{(1 - \alpha)(1 - \alpha)} \ln(\alpha \beta)$$

左边 =
$$V(k) = \frac{\alpha}{1 - \alpha\beta} \ln k + \frac{\ln(1 - \alpha\beta)}{1 - \beta} + \frac{\alpha\beta}{(1 - \beta)(1 - \alpha\beta)} \ln(\alpha\beta)$$

$$\stackrel{\triangle}{=} \frac{\alpha}{1 - \alpha\beta} \ln k + A$$

右边 = $\max \left\{ \sqrt{f(t)} \sqrt{y} + \beta V(y) \right\}$

利用 FOC 和包络条件求解得到 $y = \beta k^{\alpha}$, $\uparrow \lambda$ 求右边

$$f$$
 起 = $\max_{\alpha} \left\{ u(f(k) - g(k)) + \beta V(y) \right\}$ = $u(f(k) - g(k)) + \beta \left[\frac{\alpha}{1 - \alpha \beta} \ln g(k) + A \right]$ Victory won't come to us unless we go to it. $= \ln(1 - \alpha \beta) + \alpha \ln k + \beta \left[\frac{\alpha}{1 - \alpha \beta} \left[\ln \alpha \beta + \alpha \ln k \right] + k \right]$ = $\alpha \ln k + \frac{\alpha \beta}{1 - \alpha \beta} \alpha \ln k + \ln(1 - \alpha \beta) + \frac{\alpha \beta}{1 - \alpha \beta} \ln \alpha \beta + \beta A$ = $\frac{\alpha}{1 - \alpha \beta} \ln k + \ln(1 - \alpha \beta) + \frac{\alpha \beta}{1 - \alpha \beta} \ln \alpha \beta + \beta A$ 整理: 陈传升 整理时间: December 10, 2018

Email: sheng_ccs@@163.com

所以, 左边 = 右边, 证毕。

Version: 1.00

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