

SCHNORR IDS

We have two parties - P:V which denotes prover and verifier.
Protocol is successful if correctness ~~equation~~ condition is fulfilled.
We start with initialization.

ParamGen() \rightarrow params

KeyGen(params) \rightarrow SK, PK where SK - secret key
PK - public key

Having SK and PK we can start a protocol, which, if ~~accepts~~ ~~is correct~~, ~~fulfills the following equation~~ accepts honest P. ~~is correct~~

$$\Pr \left[\pi(P(SK, PK), V(PK)) \rightarrow 1 \right] = 1$$
~~$$\Pr \left[\pi(\text{KeyGen}() \rightarrow (SK, PK)) \right] = 1$$~~

$$P(SK, PK) \text{ with } \frac{1}{p\text{-ty}}$$

$$H(PK, \text{View}), V(PK)$$

Schnorr IDS is secure if $\text{adv}(it) = \Pr[P[\pi(\cdot) \rightarrow 1]]$ is negligible, where $\text{View} = \{t_1, t_2, \dots, t_m\}$

How protocol works:

We have a dLP (discrete logarithm problem) to break:

$$P(\text{SK}, A = g^a)$$

$$DL_{gA} = a$$

$$V(A)$$

Adversary is trying to guess a

$$X \leftarrow_R \mathbb{Z}_q$$

$$X = g^x$$

$$c \leftarrow_R \mathbb{Z}_q$$

$$s = x + ac$$

$$\leftarrow c$$

$$\rightarrow s$$

$$\text{if } g^s = X A^c$$

true
else false

1 The prover needs to simulate transcription

$$\begin{array}{c} \xrightarrow{X} \\ \xleftarrow{c} \\ \hline s = x + ac \\ c = \frac{s - x}{a} \\ X = \frac{g^s}{A^c} \end{array}$$

And now, we assume that adversary can rewind to X. Now ~~he sends the same X~~ ~~to verifier~~ but gets ~~is received~~

modified C changes and so does $s(s')$ and $C' \neq C, s \neq s'$

P

X

\checkmark

C'

$C' \in \mathbb{Z}_q$

$$s = X + aC$$

s'

Now, by solving the equations we can guess a , what results in breaking DLP?

$$s = aX + X$$

$$s' = aC' + X$$

$$s - s' = a(C - C')$$

$$a = \frac{s - s'}{C - C'}$$

Conclusion:

While ~~adversary~~ cannot rewind to the same X , he cannot obtain such s' and C' which will be ~~adversary~~ cannot learn anything from observing transcripts that he could not compute himself. The key idea is ~~that~~ order of generating transcripts doesn't matter. Schnorr IDS is secure against eavesdropping.

2) Security property

Let's define a game G_0 :

2 parties $P(sk, pk)$ $V(pk)$

Firstly the View ~~of~~ consisting
several transcripts is created
Parameters of keygen

$$V \left\{ \begin{array}{l} \pi(P(sk, pk), V(pk)) \rightsquigarrow T_1 \\ \pi(\quad \quad \quad) \rightsquigarrow T_2 \end{array} \right.$$

udaje, zem mam
sk, a kurwa nie mam

Secondly a malicious adversary
tries to impersonate the prover

$$(*) \pi(P(View, PK), V(pk))$$

Protocol is secure if

$$P((*) \rightarrow 1) \leq \text{negl}(\lambda)$$