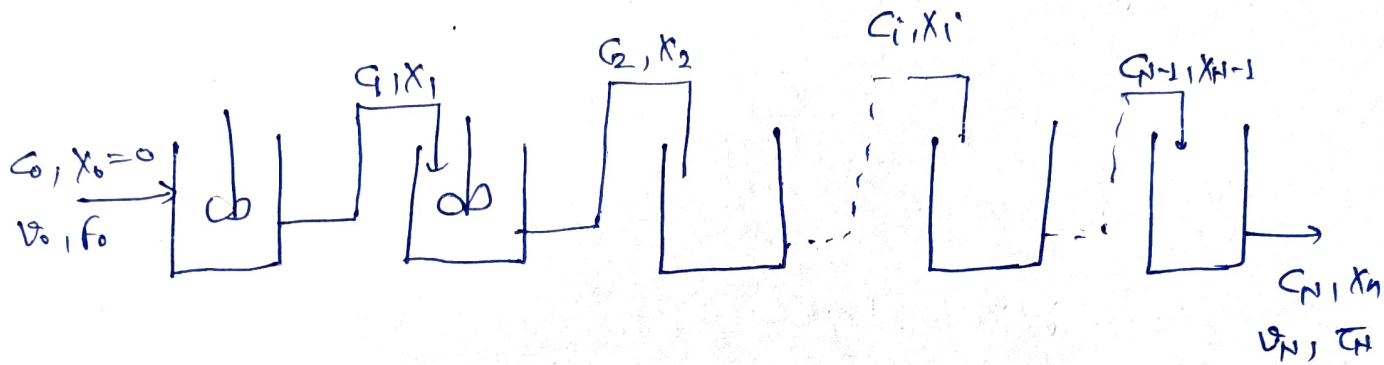


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CL208 CCRE)

Quiz

Ans-1



~~Ass~~ equal size

$$\Rightarrow V_1 = V_2 = V_i = V_N = V$$

$$\text{also } \tau_1 = \tau_2 = \tau_i = \tau_N = \tau$$

Material balance

input = output + disappearance + accumulation \rightarrow (steady state)

$$F_0(1 - x_{i-1}) = F_0(1 - x_i) + (-r_{Ai})V_i$$

$$\Rightarrow F_0(x_i - x_{i-1}) = (-r_{Ai})V_i$$

$$\Rightarrow \frac{V_i}{F_0} = \frac{x_i - x_{i-1}}{-r_{Ai}}$$

$$\Rightarrow \tau_i = \frac{C_0 V_i}{F_0} = \frac{V_i}{V} = \frac{C_0 (x_i - x_{i-1})}{-r_{Ai}}$$

$$\begin{aligned} \therefore \tau_i &= \frac{C_0 \left[\left(1 - \frac{q_i}{C_0}\right) - \left(1 - \frac{q_{i-1}}{C_0}\right) \right]}{-r_{Ai}} \\ &= \frac{C_i - C_{i-1}}{-r_{Ai}} \end{aligned}$$

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(2)

$$\tau_i = \frac{C_{i-1} - C_i}{-r_{Ai}}$$

$$\tau_i = \frac{C_0 \left[\left(1 - \frac{C_i}{C_0}\right) - \left(1 - \frac{C_{i-1}}{C_0}\right) \right]}{-r_{Ai}}$$

$$\tau_i = \frac{C_{i-1} - C_i}{-r_{Ai}}$$

for 1st order

$$-r_{Ai} = kC_i$$

$$\tau_i = \frac{C_{i-1} - C_i}{kC_i}$$

$$\Rightarrow \frac{C_{i-1}}{C_i} = 1 + k\tau_i$$

for reactor 1: $\frac{C_0}{C_1} = 1 + k\tau_1$

for reactor 2: $\frac{C_1}{C_2} = 1 + k\tau_2$

Similarly

$$\frac{C_0}{C_1} \times \frac{C_1}{C_2} \times \dots \times \frac{C_{N-1}}{C_N} = (1 + k\tau_1)(1 + k\tau_2) \dots (1 + k\tau_N)$$

$$\therefore \tau_1 = \tau_2 = \dots = \tau$$

$$\Rightarrow \frac{C_0}{C_N} = (1 + k\tau)^N$$

$$1 + k\tau = \left(\frac{C_0}{C_N}\right)^{\frac{1}{N}}$$

$$\Rightarrow \tau = \frac{1}{k} \left[\left(\frac{C_0}{C_N}\right)^{\frac{1}{N}} - 1 \right]$$

①

$$\tau_{N, \text{real}} = H \tau_i$$

$$= -\frac{N}{R} \left[\left(\frac{C_0}{C_N} \right)^{\frac{1}{N}} - 1 \right] \quad \text{--- (2)}$$

when $N \rightarrow \infty$

$$\left(\frac{C_0}{C_N} \right)^{\frac{1}{N}} = 1 + \frac{1}{N} \log \frac{C_0}{C_N} + \left(\frac{1}{N} \right)^2 \frac{1}{2!} \ln \left(\frac{C_0}{C_N} \right)^2 \dots$$

neglecting higher order terms

$$\left(\frac{C_0}{C_N} \right)^{\frac{1}{N}} = 1 + \frac{1}{N} \ln \frac{C_0}{C_N}$$

$$\left(\frac{C_0}{C_N} \right)^{\frac{1}{N}} - 1 = \frac{1}{N} \ln \frac{C_0}{C_N} \quad \text{--- (3)}$$

putting eqn (3) in eq (2)

$$\tau_{N, \text{real}} = \frac{H}{R} \left[\frac{1}{N} \ln \frac{C_0}{C_N} \right]$$

$$\tau_{N, \text{real}} = \frac{1}{R} \ln \frac{C_0}{C_N} \quad \text{--- (4)}$$

for $N \rightarrow \infty$ it behaves like PFR

$$\tau_p = \frac{1}{R} \ln \frac{C_0}{C}$$

~~at~~

Ans-2

(i) Batch Reactor: ^{Let us} If we filled batch reactor with a microfluid. ~~conversion~~ Each ~~reactor~~ aggregate or packet of microfluid acts as its own little batch reactor, conversion will be same in all aggregate as every aggregate acts as its own little batch reactor. Therefore degree of segregation does not affect conversion.

(ii) Plug flow reactor: All the microfluid and macrofluid flow alike and flow is visualised as a flow of small batch reactors. Therefore degree of segregation does not influence conversion.

(iii) Mixed flow reactor - Macrofluid: When a macrofluid enters in a mixed flow reactor, a reactant concⁿ in an aggregate does not drop immediately to a low value but decreases in the same way as it would in a batch reactor. Thus a molecule in a macrofluid does not lose its identity, its past history is not unknown and its age can be estimated by examining its neighboring molecules.

Performance eqn for a microfluid in MFR

$$1 - \bar{X}_A = \frac{\bar{C}_A}{C_{A0}} = \int_0^{\infty} \left(\frac{C_A}{C_{A0}} \right)_{\text{batch}} E dt$$

where $E dt = \frac{v}{V} e^{-\frac{vt}{V}} dt$
 $= e^{-\frac{t}{\tau}} dt$

from above eqn

$$1 - \bar{X}_A = \frac{\bar{C}_A}{C_{A0}} = \int_0^{\infty} \left(\frac{C_A}{C_{A0}} \right)_{\text{batch}} \frac{e^{-\frac{t}{\tau}}}{\tau} dt \quad (1)$$

for first order

$$\frac{C_A}{C_{A0}} = e^{-kt} \quad (2)$$

putting eqn (2) in eqn (1)

$$\frac{\bar{C}_A}{C_{A0}} = \frac{1}{\tau} \int_0^{\infty} e^{-kt} \cdot e^{-\frac{t}{\tau}} dt$$

solving above eqn

$$\frac{\bar{C}_A}{C_{A0}} = \frac{1}{1 + k\tau}$$

This eqn is identical to that obtained for a microfluid.

$$kt = \frac{C_{A0} - C_A}{C_A}$$

$$kt C_A = C_{A0} - C_A$$

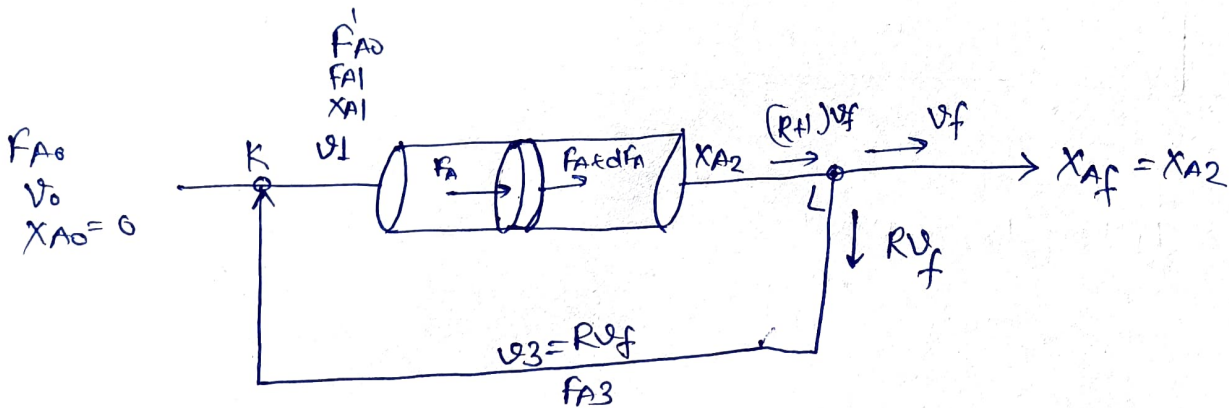
$$\Rightarrow \frac{C_A}{C_{A0}} = \frac{1}{1 + kt}$$

Thus we conclude that degree of segregation has no effect on conversion for first order reaction.

Ans-3

Recycle ratio, $R = \frac{\text{Volume of fluid returned to the reactor entrance}}{\text{volume of leaving the system}}$

$$0 \leq R < \infty$$



Material balance:

Input = Output + disappearance + accumulation
(steady state)

$$F_A' = (F_A + dF_A) + (-r_A)dV$$

$$dF_A = 0 = (-r_A)dV$$

$$d[F_A'(1-X_A)] = (-r_A)dV$$

$$\Rightarrow F_A' dX_A = (-r_A)dV$$

$$\Rightarrow \frac{dV}{F_A'} = \int_{X_{A1}}^{X_{A2}=X_{Af}} \frac{dX_A}{-r_A}$$

$$\Rightarrow \boxed{\frac{V}{F_A'} = \int_{X_{A1}}^{X_{Af}} \frac{dX_A}{-r_A}} \quad \text{--- (1)}$$

Also,

The flow entering the reactor includes both fresh feed and recycle stream.

$$\Rightarrow F_{A0}' = \text{fresh feed} + \text{unconverted recycle stream} \\ = F_{A0} + R F_{A0}$$

$$F_{A0}' = F_{A0}(R+1) \quad \text{--- (2)}$$

$$\text{Also} \quad X_{A1} = \frac{1 - \frac{C_{A1}}{C_{A0}}}{1 + E_A \frac{C_{A1}}{C_{A0}}} \quad \text{--- (3)}$$

$$\therefore \frac{F_{A0}'}{X_{A1}} = \frac{F_{A0}}{X_{A1}} \quad \text{--- (4)}$$

$$\therefore C_{A1} = \frac{F_{A1}}{V_1} = \frac{F_{A0} + F_{A3}}{V_0 + R V_f} \quad (\text{material balance at point K})$$

$$= \frac{F_{A0} + R F_{A0}(1 - X_{Af})}{V_0 + R V_0 (1 + E_A X_{Af})} \\ = C_{A0} \frac{(1 + R - R X_{Af})}{1 + R + R E_A X_{Af}} \quad \text{--- (4)}$$

from above eqn (3) & (4)

$$X_{A1} = \left(\frac{R}{R+1} \right) X_{Af} \quad \text{--- (5)}$$

Putting eqn (5) in eqn (1)

$$\boxed{\frac{V}{F_{A0}} = (R+1) \int_{\left(\frac{R}{R+1} \right) X_{Af}}^{X_{Af}} \frac{dX_A}{-r_A}}$$

for $\varepsilon = 0$

$$\boxed{Z = \frac{C_{A0}V}{F_{A0}} = -(R+1) \int_{C_{A0}}^{C_{Af}} \frac{dC_A}{C_{A0} + R C_{Af}} \quad \text{acts like PFR}}$$

for $R = 0$

$$\boxed{\frac{V}{F_{A0}} = \int_A^{X_{Af}} \frac{dX_A}{-r_A}} \quad \text{acts like PFR}$$

for $R = \infty$

it behaves like MFR

$\Rightarrow (-r_A)$ will be constant

$$\begin{aligned} \Rightarrow \frac{V}{F_{A0}} &= \frac{R+1}{(-r_A)} \int_0^{X_{Af}} \frac{dX_A}{\left(\frac{R}{R+1}\right) X_{Af}} \\ &= \frac{R+1}{(-r_A)} \left[X_A \right]_0^{X_{Af}} \frac{R}{R+1} \\ &= \frac{R+1}{(-r_A)} \left(X_{Af} - \frac{R}{R+1} X_{Af} \right) \end{aligned}$$

$$\Rightarrow \boxed{\frac{V}{F} = \frac{X_{Af}}{-r_A}} \quad \text{acts like MFR}$$

for $\varepsilon = 0$, 1st order kinetics

$$\boxed{\frac{kZ}{R+1} = \ln \left[\frac{C_{A0} + R C_{Af}}{(R+1) C_{Af}} \right]}$$