

HW8-8

$$\textcircled{1} P = P_0 e^{kt}$$

$$\text{half life} = 1590$$

$$t = 3000 \text{ yr}$$

$$\text{sample} = 200 \text{ mg}$$

$$\frac{1}{2} = e^{k(1590)}$$

$$k = \ln(1/2)/1590$$

$$P = 200 e^{k(3000)}$$

$$\text{then } P = 54.082$$

$$\textcircled{4} P = P_0 e^{rt}$$

$$P_0 = 900; t = 2; P = 1800$$

$$P = 900 e^{r(2)} = 1800$$

$$r = \ln(2)/2$$

$$P(t) = 900 e^{rt}$$

$$P(5) = 5091.168825$$

$$P(t) = 2790; t = ?$$

$$3.1 = e^{kt}; t = 3.2645 \text{ hours}$$

$$\textcircled{3} \frac{dT}{dt} = k(T - T_a)$$

$$T(0) = 295$$

$$T(0.7) = 190$$

$$\int \frac{1}{T - T_a} dT = \int k dt$$

$$\ln(T - T_a) = kt + C$$

$$C = \ln(216)$$

$$k = \frac{10}{7} \ln(111/216)$$

using substitution

then:

$$\ln(T - T_a) = \frac{50}{7} \ln\left(\frac{111}{216}\right) +$$

$$\ln(216) + 5 \text{ hours}$$

$$T = 80.8588 \text{ hrs}$$

$$\textcircled{2} P = P_0 e^{kt}$$

$$\text{where } 0.94 : \text{half} = 5720$$

$$\frac{1}{2} = e^{k(5720)}; k = \ln(1/2)/5720$$

$$\text{full life} = 5720 \times 2 = 11460$$

$$\frac{94}{100} = e^{kt}; \ln\left(\frac{94}{100}\right)/k = t$$

then the value of $t \approx 511.501$ years ago

$$\textcircled{5} P = P_0 e^{rt}; r = 0.0132$$

$$\text{available land} = 13,500,000 \times 640$$

$$\text{max people} = 17.28 \text{ B}$$

$$\text{Current people} = 6.06 \text{ B}$$

$$\frac{17.28}{6.06} = e^{rt}; \frac{\ln\left(\frac{17.28}{6.06}\right)}{0.0132} \approx 79$$

then we gonna die at 2079