# 1 E.A.5.3

# 1.1 Modellazione (Cards)

#### 1.1.1 Variabili e domini

Dati i parametri  $k,n\in\mathbb{N}$  t.c.  $k\geq 2,n>0$ 

$$\mathrm{CSP}(k \ge 2, n > 0) : (X, D, C)$$

- $X = X_C \cup X_P$  t.c.
  - $X_C = \{C_i \mid i \in \{1, ..., kn\}\}$
  - $X_P = \{P_i \mid i \in \{1, ..., kn\}\}$
- $D = D_C \cup D_P$  t.c.
  - $D_C = \left\{ D_{C_i} \mid \exists C_i \in X_C \land D_{C_i} = \{1, ..., kn\} \right\}$   $D_P = \left\{ D_{P_i} \mid \exists P_i \in X_P \land D_{P_i} = \{1, ..., n\} \right\}$
- $C = C_{\text{cards}} \cup C_{\text{pos}} \cup \text{alldifferent}(P_1, ..., P_n) \text{ t.c.}$   $C_{\text{cards}} = \{ \langle \{C_i\}, R \rangle \mid \exists i, j \}$ 

  - $C_{\rm pos} = \{\langle \{\}, R \rangle \}$

#### 1.1.2 Vincoli

#### 1.2 Istanziazione

### 1.2.1 Variabili e domini

Dati k = 2, n = 4

- $\bullet \ \ X = \{\overset{\cdot}{C_1}, \overset{\cdot}{C_2}, \overset{\cdot}{C_3}, \overset{\cdot}{C_4}, \overset{\cdot}{C_5}, \overset{\cdot}{C_6}, \overset{\cdot}{C_7}, \overset{\cdot}{C_8}, \overset{\cdot}{P_1}, \overset{\cdot}{P_2}, \overset{\cdot}{P_3}, \overset{\cdot}{P_4}, \overset{\cdot}{P_5}, \overset{\cdot}{P_6}, \overset{\cdot}{P_7}, \overset{\cdot}{P_8}\}$
- $D = \{D_{C_1}, D_{C_2}, D_{C_3}, D_{C_4}, D_{C_5}, D_{C_6}, D_{C_7}, D_{C_8}, \}$

### 1.2.2 Vincoli

- $\begin{array}{l} \bullet \quad C = C_{\mathrm{diff}} \cup C_{\mathrm{col}} \cup C_{\mathrm{pos}} \\ \bullet \quad C_{\mathrm{diff}} = \mathrm{alldifferent}(P_1, P_2, P_3, P_4, P_5, P_6, P_7, P_8) \end{array}$
- $\begin{array}{ll} \bullet & C_{\mathrm{col}} = \{\} \\ \bullet & C_{\mathrm{pos}} = \{\} \end{array}$

## 1.3 Codifica in MiniZinc

```
include "alldifferent.mzn";
int: k = 3;
int: n = 10;

array[1..k * n] of var 1..n: cards;
array[1..k * n] of var 1..k * n: positions;

constraint forall(i in 1..n, j in 1..k)(
    cards[(i - 1) * k + j] == i
);

constraint forall(i in 0..n - 1, j in 2..k)(
    positions[i * k + j] ==
        positions[i * k + j - 1] + cards[i * k + j] + 1
);

constraint alldifferent(positions);
```