

Software Engineering

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The latest version of the .pdf and the referenced material can be found at the following link: <https://github.com/CuriousCI/software-engineering>

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1 Software models

Software projects require **design choices** that often can't be driven by experience or reasoning alone. That's why a **model** of the project is needed to compare different solutions.

1.1 The “Amazon Prime Video” article

If you were tasked with designing the software architecture for Amazon Prime Video, which choices would you make? What if you had the to keep the costs minimal? Would you use a distributed architecture or a monolith application?

More often than not, monolith applications are considered more costly and less scalable than the counterpart, due to an inefficient usage of resources. But, in a recent article, a Senior SDE at Prime Video describes how they “*reduced the cost of the audio/video monitoring infrastructure by 90%*” [1] by using a monolith architecture.

There isn't a definitive way to answer these type of questions, but one way to go about it is building a model of the system to compare the solutions. In the case of Prime Video, “*the audio/video monitoring service consists of three major components:*” [1]

- the *media converter* converts input audio/video streams
- the *defect detectors* analyze frames and audio buffers in real-time
- the *orchestrator* controls the flow in the service

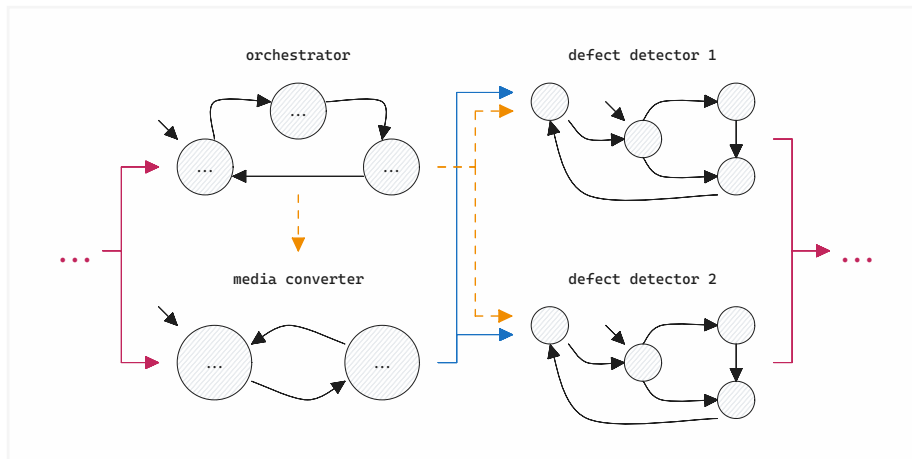


Figure 1: audio/video monitoring system process

To answer questions about the system, it can be simulated by modeling its components as **Markov decision processes**.

1.2 Models

1.2.1 Markov chain

In simple terms, a Markov chain M is described by a set of **states** S and the **transition probability** $p : S \times S \rightarrow [0, 1]$ such that $p(s'|s)$ is the probability to transition from s to s' . The transition probability p is constrained by Equation 1

$$\forall s \in S \quad \sum_{s' \in S} p(s'|s) = 1 \quad (1)$$

A Markov chain (or Markov process) is characterized by memorylessness (called the Markov property), meaning that predictions can be made solely on its present state, and aren't influenced by its history.

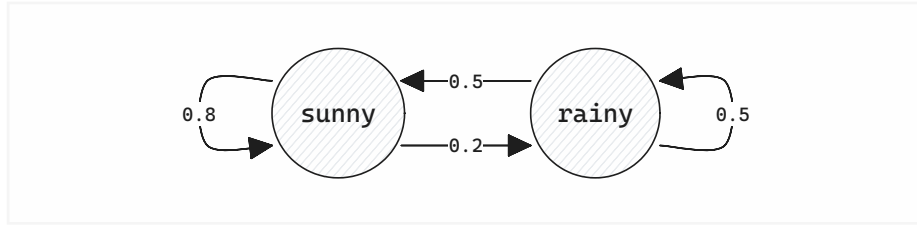


Figure 2: Example Markov chain with $S = \{\text{rainy}, \text{sunny}\}$

	sunny	rainy
sunny	0.8	0.2
rainy	0.5	0.5

Table 1: Transition probability of Figure 2

If a Markov chain M transitions at **discrete time** steps (i.e. the time steps t_0, t_1, t_2, \dots are a countable) and the **state space** is countable, then it's called a DTMC (discrete-time Markov chain). There are other classifications for continuous state space and continuous-time.

The Markov process is characterized by a **transition matrix** which describes the probability of certain transitions, like the one in Table 1. Later in the guide it will be shown that implementing transition matrices in C++ is really simple when using the `<random>` library.

1.2.2 Markov decision process

A Markov decision process (MDP), despite sharing the name, is **different** from a Markov chain, because it interacts with an **external environment**. A MDP M is a tuple (U, X, Y, p, g) s.t.

- U is the set of **input values**
- X is the set of **states**
- Y is the set of **output values**

- $p : X \times X \times U \rightarrow [0, 1]$ is such that $p(x'|x, u)$ is the probability to **transition** from state x to state x' when the **input value** is u
- $g : X \rightarrow Y$ is the **output function**
- $x_0 \in X$ is the **initial state**

The same constrain in Equation 1 holds for MDPs, with an important difference: **for each input value**, the sum of the transition probabilities for **that input value** must be 1.

$$\forall x \in X \quad \forall u \in U \quad \sum_{x' \in X} p(x'|x, u) = 1 \quad (2)$$

1.2.2.1 MDP example

The development process of a company can be modeled as a MDP

$M = (U, X, Y, p, g)$ s.t.

- $U = \{\varepsilon\}^1$, $X = \{0, 1, 2, 3, 4\}$, $Y = \text{Cost} \times \text{Duration}$, $x_0 = 0$

$$g(x) = \begin{cases} (0, 0) & x \in \{0, 4\} \\ (20000, 2) & x \in \{1, 3\} \\ (40000, 4) & x = 2 \end{cases} \quad (3)$$

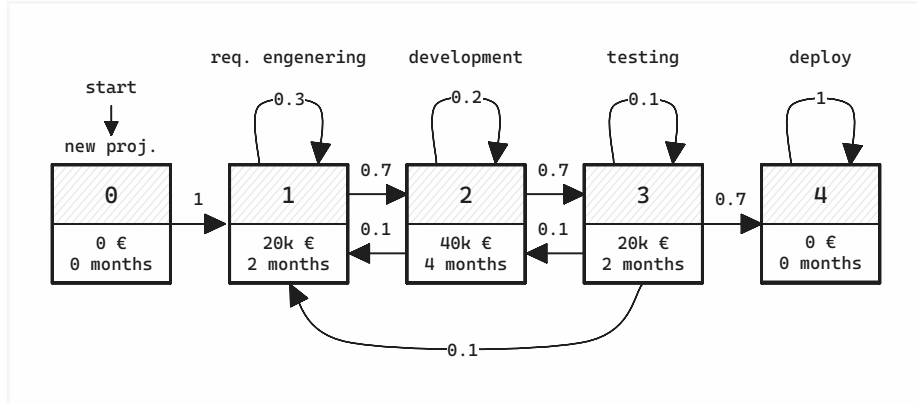


Figure 3: the model of a team's development process

ε	0	1	2	3	4
0	0	1	0	0	0
1	0	.3	.7	0	0
2	0	.1	.2	.7	0
3	0	.1	.1	.1	.7
4	0	0	0	0	1

Only **1 transition matrix** is needed, as $|U| = 1$ (there's 1 input value). If U had multiple input values, like $\{\text{on}, \text{off}, \text{wait}\}$, then 3 transition matrices would have been required, one **for each input value**.

¹If U is empty M can't transition, at least 1 input is required, i.e. ε

1.2.3 Network of MDPs

Let M_1, M_2 be two MDPs s.t.

- $M_1 = (U_1, X_1, Y_1, p_1, g_1)$
- $M_2 = (U_2, X_2, Y_2, p_2, g_2)$

Then $M = (U_1, X_1 \times X_2, Y_2, p, g)$ s.t.

- $p((x_1', x_2') \mid (x_1, x_2), u_1) = (p(x_1' \mid x_1, u_1), p(x_2' \mid x_2, g_1(x_1)))$
- $g((x_1, x_2)) = g_2(x_2)$
- TODO the connection can also be partial

1.3 Other methods

1.3.1 Incremental average

Given a set of values $X = \{x_1, \dots, x_n\} \subset \mathbb{R}$ the average $\bar{x}_n = \frac{\sum_{i=0}^n x_i}{n}$ can be computed with a simple procedure

```
float average(std::vector<float> X) {
    float sum = 0;
    for (auto x_i : X)
        sum += x_i;

    return sum / X.size();
}
```

Listing 1: examples/average.cpp

The problem with this procedure is that, by adding up all the values before the division, the **numerator** could **overflow**, even if the value of \bar{x}_n fits within the IEEE-754 limits. Nonetheless, \bar{x}_n can be calculated incrementally.

$$\begin{aligned}\bar{x}_{n+1} &= \frac{\sum_{i=0}^{n+1} x_i}{n+1} = \frac{\left(\sum_{i=0}^n x_i\right) + x_{n+1}}{n+1} = \frac{\sum_{i=0}^n x_i}{n+1} + \frac{x_{n+1}}{n+1} = \\ &= \frac{\left(\sum_{i=0}^n x_i\right)n}{(n+1)n} + \frac{x_{n+1}}{n+1} = \frac{\sum_{i=0}^n x_i}{n} \cdot \frac{n}{n+1} + \frac{x_{n+1}}{n+1} = \\ &= \bar{x}_n \cdot \frac{n}{n+1} + \frac{x_{n+1}}{n+1}\end{aligned}\quad (4)$$

With this formula the numbers added up are smaller: \bar{x}_n is multiplied by $\frac{n}{n+1} \sim 1$, and, if x_{n+1} fits in IEEE-754, then $\frac{x_{n+1}}{n+1}$ can also be encoded.

```
float incr_average(std::vector<float> X) {
    float average = 0;
    for (size_t n = 0; n < X.size(); n++)
        average =
            average * ((float)n / (n + 1)) + X[n] / (n + 1);

    return average;
}
```

Listing 2: examples/average.cpp

In examples/average.cpp the procedure average() returns Inf and incr_average() successfully computes the average.

1.3.2 Welford's online algorithm

In a similar fashion, it could be faster and require less memory to calculate the **standard deviation** incrementally. Welford's online algorithm can be used for this purpose.

$$\begin{aligned}
 M_{2,n} &= \sum_{i=1}^n (x_i - \bar{x}_n)^2 \\
 M_{2,n} &= M_{2,n-1} + (x_n - \bar{x}_{n-1})(x_n - \bar{x}_n) \quad \textcircled{2} \\
 \sigma_n^2 &= \frac{M_{2,n}}{n} \\
 s_n^2 &= \frac{M_{2,n}}{n-1}
 \end{aligned} \tag{5}$$

Given M_2 , if $n > 0$, the standard deviation is $\sqrt{\frac{M_{2,n}}{n}}$ $\textcircled{3}$. The average can be calculated incrementally like in Section 1.3.1 $\textcircled{1}$.

```

void Stat::save(real_t x_i) {
    real_t next_mean =
        mean_ * ((real_t)n / (n + 1)) + x_i / (n + 1);  $\textcircled{1}$ 

    m_2__ += (x_i - mean_) * (x_i - next_mean);  $\textcircled{2}$ 
    mean_ = next_mean;
    n++;
}

real_t Stat::stddev() const {
    return n > 0 ? sqrt(m_2__ / n) : 0;  $\textcircled{3}$ 
}

```

Listing 3: mocc/math.cpp

1.3.3 Euler method

When an ordinary differential equation can't be solved analitically, the solution must be approximated. There are many techniques: one of the simplest ones (yet less accurate and efficient) is the forward Euler method, described by the following equation:

$$y_{n+1} = y_n + \Delta \cdot f(x_n, y_n) \tag{6}$$

Let the function y be the solution to the following problem

$$\begin{cases} y(x_0) = y_0 \\ y'(x) = f(x, y(x)) \end{cases} \tag{7}$$

Let $y(x_0) = y_0$ be the initial condition of the system, and $y' = f(x, y(x))$ be the known **derivative** of y (y' is a function of x and $y(x)$). To approximate y , a Δ is chosen (the smaller, the more precise the approximation) s.t. $x_{n+1} = x_n + \Delta$. Now, understanding Equation 6 should be

easier: the value of y at the **next step** is the current value of y plus the value of its derivative y' (multiplied by Δ). In Equation 6 y' is multiplied by Δ because when going to the next step, all the derivatives from x_n to x_{n+1} must be added up, and it's done by adding up

$$(x_{n+1} - x_n) \cdot f(x_n, y_n) = \Delta \cdot f(x_n, y_n) \quad (8)$$

Where $y_n = y(x_n)$. Let's consider the example in Equation 9.

$$\begin{cases} y(x_0) = 0 \\ y'(x) = 2x \end{cases}, \quad \text{with } \Delta = 1, 0.5, 0.3, 0.25 \quad (9)$$

The following program approximates Equation 9 with different Δ values.

```
#define SIZE 4
float derivative(float x) { return 2 * x; }

int main() {
    size_t x[SIZE];
    for (size_t i = 0; i < SIZE; i++) {
        x[i] = 0;
        float delta = 1. / (i + 1);
        for (float t = 0; t ≤ 10; t += delta)
            x[i] += delta * derivative(t);
    }
    return 0;
}
```

Listing 4: examples/euler.cpp

The approximation is close, but not very precise. However, the error analysis is beyond this guide's scope.

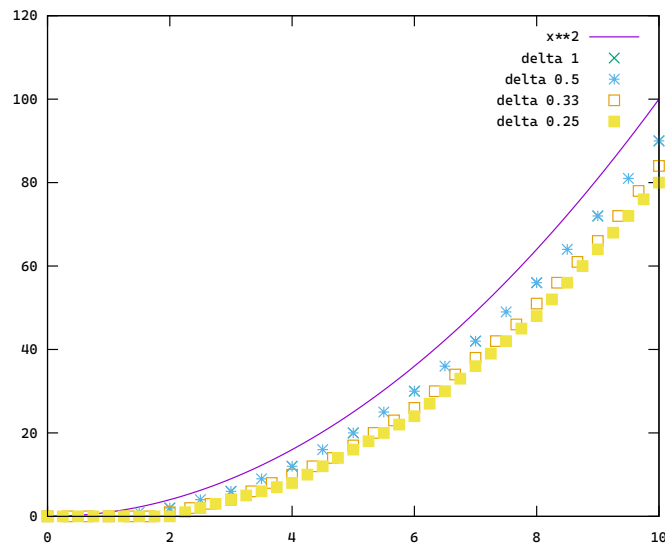


Figure 4: examples/euler.svg

1.3.4 Monte Carlo method

“Monte Carlo methods, or Monte Carlo experiments, are a broad class of computational algorithms that rely on repeated random sampling to obtain numerical results.” [2]

“The underlying concept is to use randomness to solve problems that might be deterministic in principle [...] Monte Carlo methods are mainly used in three distinct problem classes: optimization, numerical integration, and generating draws from a probability distribution” [2]

The cost to develop a feature is described by an uniform discrete distribution $\mathcal{U}\{300, 1000\}$. Determine the probability that the cost is less than 550.

The problem above can be easily solved analitically, but let’s use the Monte Carlo method to approximate its value.

```
#include <iostream>
#include <random>

int main() {
    std::random_device random_device;
    std::default_random_engine rand_engine(random_device());
    std::uniform_int_distribution<> rand_cost(300, 1000);

    const size_t ITERATIONS = 10000;
    size_t below_550 = 0;

    for (size_t i = 0; i < ITERATIONS; i++) ①
        if (rand_cost(rand_engine) < 550) ②
            below_550++; ③

    std::cout << (double)below_550/ITERATIONS ④ << std::endl;
    return 0;
}
```

The first step is to simulate for a certain number of iterations ① the system (in this example, “simulating the system” means generating a random integer cost between 300 and 1000 ②). If the the iteration respects the requested condition, then it’s counted ③.

At the end of the simulations, the probability is calculated as $\frac{\text{iterations below 550}}{\text{total iterations}}$ ④ . The bigger is the number of iterations, the more precise is the approximation. This type of calculation can be very easily distributed in a HPC (high performance computing) context.

2 How to C++

This section covers the basics assuming the reader already knows C.

2.1 The random library

The C++ standard library offers tools to easily implement MDPs.

2.1.1 Random engines

In C++ there are many ways to **generate random numbers** [3]. Generally it's not recommended to use `random()` ①. It's better to use a **random generator** ⑤, because it's fast, deterministic (given a seed, the sequence of generated numbers is the same) and can be used with distributions. A `random_device` is a non deterministic generator: it uses a **hardware entropy source** (if available) to generate the random numbers.

```
#include <iostream>
#include <random>

int main() {
    std::cout << random() ① << std::endl;

    std::random_device random_device; ②
    std::cout << random_device() ③ << std::endl;

    int seed = random_device(); ④
    std::default_random_engine random_engine(seed); ⑤
    std::cout << random_engine() ⑥ << std::endl;
}
```

Listing 6: examples/random.cpp

The typical course of action is to instantiate a `random_device` ②, and use it to generate a seed ④ for a `random_engine`. Given that random engines can be used with distributions, they're really useful to implement MDPs. Also, ③ and ⑥ are examples of **operator overloading** (Section 2.4).

From this point on, `std::default_random_engine` will be referred to as `urng_t` (uniform random number generator type).

```
#include <random>
// works like typedef in C
using urng_t = std::default_random_engine;

int main() {
    urng_t urng(190201);
}
```

2.1.2 Distributions

Just the capability to generate random numbers isn't enough, these numbers need to be manipulated to fit certain needs. Luckily, C++ covers **basically all of them**. For example, the MDP in Figure 3 can be easily simulated with the following code:

```
#include <iostream>
#include <random>
using urng_t = std::default_random_engine;

int main() {
    std::random_device random_device;
    urng_t urng(random_device());

    std::discrete_distribution<> transition_matrix[] = {
        {0, 1},
        {0, .3, .7},
        {0, .1, .2, .7},
        {0, .1, .1, .1, .7},
        {0, 0, 0, 0, 1},
    };

    size_t state = 0;
    for (size_t step = 0; step < 15; step++) {
        state = transition_matrix[state](urng);
        std::cout << state << std::endl;
    }

    return 0;
}
```

Listing 8: examples/transition_matrix.cpp

2.1.2.1 Uniform discrete distribution ([docs](#))

To test a system S it's required to build a generator that sends value v_t to S every T_t seconds. For each send, the value of T_t is an **integer** chosen uniformly in the range $[20, 30]$.

The C code to compute T_t would be `T = 20 + rand() % 11;`, which is very **error prone**, hard to remember and has no semantic value. In C++ the same can be done in a **simpler** and **cleaner** way:

```
std::uniform_int_distribution<> random_T(20, 30); ①
size_t T = ② random_T(urng);
```

The interval T_t can be easily generated ② without needing to remember any formula or trick. The behaviour of T_t is defined only once ①, so it

can be easily changed without introducing bugs or inconsistencies. It's also worth to take a look at the implementation of the exercise above (with the addition that $v_t = T_t$), as it comes up very often in software models.

```
#include <iostream>
#include <random>

using urng_t = std::default_random_engine;

int main() {
    std::random_device random_device;
    urng_t urng(random_device());
    std::uniform_int_distribution<> random_T(20, 30);

    size_t T = random_T(urng), next_request_time = T;
    for (size_t time = 0; time < 1000; time++) {
        if (time < next_request_time)
            continue;

        std::cout << T << std::endl;
        T = random_T(urng);
        next_request_time = time + T;
    }

    return 0;
}
```

Listing 9: examples/interval_generator.cpp

The `uniform_int_distribution` has many other uses, for example, it could uniformly generate a random state in a MDP. Let `STATES_SIZE` be the number of states

```
uniform_int_distribution<> random_state(0, STATES_SIZE - 1 ①);
```

`random_state` generates a random state when used. Be careful! Remember to use `STATES_SIZE - 1 ①`, because `uniform_int_distribution` is inclusive. Forgetting `-1` can lead to very sneaky bugs, like random segfaults at different instructions. It's very hard to debug unless using `gdb`. The `uniform_int_distribution` can also generate negative integers, for example $z \in \{x \mid x \in \mathbb{Z} \wedge x \in [-10, 15]\}$.

2.1.2.2 Uniform continuous distribution ([docs](#))

It's the same as above, with the difference that it generates **real** numbers in the range $[a, b) \subset \mathbb{R}$.

2.1.2.3 Bernoulli distribution ([docs](#))

To model a network protocol P it's necessary to model requests. When sent, a request can randomly fail with probability $p = 0.001$.

Generally, a random fail can be simulated by generating $r \in [0, 1]$ and checking whether $r < p$.

```
std::uniform_real_distribution<> uniform(0, 1);
if (uniform(urng) < 0.001)
    fail();
```

A `std::bernoulli_distribution` is a better fit for this specification, as it generates a boolean value and its semantics represents “an event that could happen with a certain probability p ”.

```
std::bernoulli_distribution random_fail(0.001);
if (random_fail(urng))
    fail();
```

2.1.2.4 Normal distribution ([docs](#))

Typical Normal distribution, requires the mean ① and the stddev ②.

```
#include <iomanip>
#include <iostream>
#include <map>
#include <random>

using urng_t = std::default_random_engine;

int main() {
    std::random_device random_device;
    urng_t urng(random_device());
    std::normal_distribution<> normal(12 ①, 2 ②);

    std::map<long, unsigned> histogram{};
    for (size_t i = 0; i < 10000; i++)
        ++histogram[(size_t)normal(urng)];

    for (const auto [k, v] : histogram)
        if (v / 200 > 0)
            std::cout << std::setw(2) << k << ' '
                        << std::string(v / 200, '*') << '\n';

    return 0;
}
```

Listing 10: examples/normal.cpp

```

8 **
9 ****
10 *****
11 *****
12 *****
13 *****
14 ****
15 **

```

2.1.2.5 Exponential distribution ([docs](#))

A server receives requests at a rate of 5 requests per minute from each client. You want to rebuild the architecture of the server to make it cheaper. To test if the new architecture can handle the load, its required to build a model of client that sends requests at random intervals with an expected rate of 5 requests per minute.

It's easier to simulate the system in seconds (to have more precise measurements). If the client sends 5/min, the rate in seconds should be $\lambda = \frac{5}{60} \sim 0.083$ requests per second.

```

int main() {
    std::random_device random_device;
    urng_t urng(random_device());
    std::exponential_distribution<> random_interval(5. / 60.);

    real_t next_request_time = 0;
    std::vector<real_t> req_per_min = {0};
    for (real_t time_s = 0; time_s < HORIZON; time_s++) {
        if (((size_t)time_s) % 60 == 0)
            req_per_min.push_back(0); ①

        if (time_s < next_request_time)
            continue;

        req_per_min.back()++; ②
        next_request_time = time_s + random_interval(urng);
    }

    real_t mean = 0;
    for (auto x : req_per_min) ③
        mean += x;

    std::cout << mean / req_per_min.size() << std::endl;
}

```

Listing 11: examples/exponential.cpp

The code above has a counter to measure how many requests were sent each minute. A new counter is added every 60 seconds ①, and it's incremented by 1 each time a request is sent ②. At the end, the average of the counts is calculated ③, and it comes out to be about 5 requests every 60 seconds (or 5 requests per minute).

2.1.2.6 Poisson distribution ([docs](#))

- TODO: The Poisson distribution is closely related to the Exponential distribution, as it generates a number of items given the rate.

2.1.2.7 Geometric distribution ([docs](#))

- TODO: A typical geometric distribution

2.1.2.8 Discrete distribution ([docs](#))

To choose the architecture for an e-commerce it's necessary to simulate realistic purchases. After interviewing 678 people it's determined that 232 of them would buy a shirt from your e-commerce, 158 would buy a hoodie and the other 288 would buy pants.

The objective is to simulate random purchases reflecting the results of the interviews. One way to do it is to calculate the percentage of buyers for each item, generate $r \in [0, 1]$, and do some checks on r . However, this specification can be implemented very easily in C++ by using a `std::discrete_distribution`, without having to do any calculation or write complex logic.

```
enum Item { Shirt = 0, Hoodie = 1, Pants = 2 };

int main() {
    std::discrete_distribution<>
        rand_item = {232, 158, 288}; ①

    for (size_t request = 0; request < 1000; request++) {
        switch (rand_item(urng)) {
            case Shirt: ② std::cout << "shirt"; break;
            case Hoodie: ② std::cout << "hoodie"; break;
            case Pants: ② std::cout << "pants"; break;
        }

        std::cout << std::endl;
    }

    return 0;
}
```

Listing 12: examples/TODO.cpp

The `rand_item` instance generates a random integer $x \in \{0, 1, 2\}$ (because 3 items were specified in the array ①, if the items were 10, then x would have been s.t. $0 \leq x \leq 9$). The `= {a, b, c}` syntax can be used to initialize the a discrete distribution because C++ allows to pass a `std::array` to a constructor [4].

The `discrete_distribution` uses the in the array to generates the probability for each integer. For example, the probability to generate 0 would be calculated as $\frac{232}{232+158+288}$, the probability to generate 1 would be $\frac{158}{232+158+288}$ and the probability to generate 2 would be $\frac{288}{232+158+288}$. This way, the sum of the probabilities is always 1, and the probability is proportional to the weight.

To map the integers to the actual items ② an `enum` is used: for simple enums each entry can be converted automatically to its integer value (and viceversa). In C++ there is another construct, the `enum class` which doesn't allow implicit conversion (the conversion must be done with a function or with `static_cast`), but it's more typesafe (see Section 2.5.3).

The `discrete_distribution` can also be used for transition matrices, like the one in Table 1. It's enough to assign each state a number (e.g. sunny = 0, rainy = 1), and model the transition probability of **each state** as a discrete distribution.

```
std::discrete_distribution[] transition_matrix = {
    /* 0 */ { /* 0 */ 0.8, /* 1 */ 0.2},
    /* 1 */ { /* 0 */ 0.5, /* 1 */ 0.5}
}
```

In the example above the probability to go from state 0 (sunny) to 0 (sunny) is 0.8, the probability to go from state 0 (sunny) to 1 (rainy) is 0.2 etc...

The `discrete_distribution` can be initialized if the weights aren't already know and must be calculated.

```
for (auto &weights ① : matrix)
    transition_matrix.push_back(
        std::discrete_distribution<>(
            weights.begin(), ② weights.end() ③ )
    );
```

Listing 13: practice/2025-01-09/1/main.cpp

The weights are stored in a vector ①, and the `discrete_distribution` for each state is initialized by indicating the pointer at the beginning `reft(2)` and at the end ③ of the vector. This works with dynamic arrays too.

2.2 Data

2.2.1 Manual memory allocation

If you allocate with `new`, you must deallocate with `delete`, you can't mixup them with `malloc()` and `free()`

To avoid manual memory allocation, most of the time it's enough to use the structures in the standard library, like `std::vector<T>`.

2.2.2 Data structures

2.2.2.1 Vectors

You don't have to allocate memory, basically never! You just use the structures that are implemented in the standard library, and most of the time they are enough for our use cases. They are really easy to use.

Vectors can be used as stacks.

2.2.2.2 Deques

Deques are very common, they are like vectors, but can be pushed and popped in both ends, and can be used as queues.

2.2.2.3 Sets

Not needed as much, works like the Python set. Can be either a set (ordered) or an unordered set (uses hashes)

2.2.2.4 Maps

Could be useful. Can be either a map (ordered) or an unordered map (uses hashes)

2.3 I/O

Input output is very simple in C++.

2.3.1 Standard I/O

2.3.2 Files

Working with files is way easier in C++

```
#include <fstream>

int main(){
    std::ofstream output("output.txt");
    std::ifstream params("params.txt");

    while (etc ... ) {}
```

```
    output.close();  
    params.close();  
}
```

2.4 Operator overloading

In Listing 6, to generate a random number, `random_device()` ③ and `random_engine()` ⑥ are used like functions, but they aren't functions, they're instances of a **class**. That's because in C++ you can define how a certain operator (like `+`, `+=`, `<<`, `>>`, `[]`, `()` etc..) should behave when used on an instance of the **class**. It's called **operator overloading**, a relatively common feature:

- in Python operation overloading is done by implementing methods with special names, like `__add__()` [5]
- in Rust it's done by implementing the Trait associated with the operation, like `std::ops::Add` [6].
- Java and C don't have operator overloading

For example, `std::cout` is an instance of the `std::basic_ostream` **class**, which overloads the method "`operator<<()`" [7]. The same applies to file streams.

2.5 Code structure

2.5.1 Classes

- TODO:
 - Maybe constructor
 - Maybe operators? (more like nah)
 - virtual stuff (interfaces)

2.5.2 Structs

- basically like classes, but with everything public by default

2.5.3 Enums

- enum vs enum class
- an example maybe
- they are useful enough to model a finite domain

2.5.4 Inheritance

3 Debugging with `gdb`

It's super useful! Trust me, if you learn this everything is way easier (printf won't be useful anymore)

First of all, use the `-ggdb3` flags to compile the code. Remember to not use any optimization like `-O3...` using optimizations makes the program harder to debug.

```
DEBUG_FLAGS := -ggdb3 -Wall -Wextra -pedantic
```

Then it's as easy as running `gdb ./main`

- TODO: could be useful to write a script if too many args
- TODO: just bash code to compile and run
- TODO (just the most useful stuff, technically not enough):
 - `r`
 - `c`
 - `n`
 - `c 10`
 - `enter` (last instruction)
 - `b`
 - on lines
 - on symbols
 - on specific files
 - `clear`
 - `display`
 - `set print pretty on`

4 Examples

Each example has 4 digits xxxx that are the same as the ones in the software folder in the course material. The code will be **as simple as possible** to better explain the core functionality, but it's **strongly suggested** to try to add structure (*classes etc..*) where it **seems fit**.

4.1 First examples

This section puts together the **formal definitions** and the C++ knowledge to implement some simple MDPs.

4.1.1 A simple MDP [1100]

The first MDP $M = (U, X, Y, p, g)$ is such that

- $U = \{\varepsilon\}^2$
- $X = [0, 1] \times [0, 1]$, each state is a pair ③ of **real** numbers ②
- $Y = [0, 1] \times [0, 1]$
- $p : X \times X \times U \rightarrow X = \mathcal{U}(0, 1) \times \mathcal{U}(0, 1)$, the transition probability is a **uniform continuous** distribution ①
- $g : X \rightarrow Y : (r_0, r_1) \mapsto (r_0, r_1)$ outputs the current state ④
- $x_0 = (0, 0)$ is the initial state ③

```
int main() {
    std::random_device random_device;
    urng_t urng(random_device());
    std::uniform_real_distribution<real_t> uniform(0, 1); ①

    std::vector<real_t ② > state(2, 0); ③
    std::ofstream log("log");

    for (size_t time = 0; time ≤ HORIZON; time++) {
        for (auto &r : state)
            r = uniform(urng); ①

        log << time << ' ';
        for (auto r : state)
            log << r << ' '; t ④
        log << std::endl;
    }

    log.close();
    return 0;
}
```

Listing 14: software/1100/main.cpp

²See Section 1.2.2.1

4.1.2 MDPs network pt.1 [1200]

This example has 2 MDPs M_0, M_1 s.t.

- $M_0 = (U^0, X^0, Y^0, p^0, g^0)$
- $M_1 = (U^1, X^1, Y^1, p^1, g^1)$

M_0 and M_1 are similar to the MDP in Section 4.1.1, with the difference that $U^i = [0, 1] \times [0, 1]$, having $U^i = X^i$, meaning p must be redefined:

$$p^i(x'|x, u) = \begin{cases} 1 & \text{if } x' = u \\ 0 & \text{otherwise} \end{cases} \quad (10)$$

Then the 2 MDPs can be connected

$$\begin{aligned} U_{t+1}^0 &= (r_0 \cdot \mathcal{U}(0, 1), r_1 \cdot \mathcal{U}(0, 1)) \text{ where } g^1(X_t^1) = (r_0, r_1) \\ U_{t+1}^1 &= (r_0 + \mathcal{U}(0, 1), r_1 + \mathcal{U}(0, 1)) \text{ where } g^0(X_t^0) = (r_0, r_1) \end{aligned} \quad (11)$$

Given that $g^i(X_t^i) = X_t^i$ and $U_t^i = X_t^i$, the connection in Equation 11 can be simplified:

$$\begin{aligned} X_{t+1}^0 &= (r_0 \cdot \mathcal{U}(0, 1), r_1 \cdot \mathcal{U}(0, 1)) \text{ where } X_t^1 = (r_0, r_1) \\ X_{t+1}^1 &= (r_0 + \mathcal{U}(0, 1), r_1 + \mathcal{U}(0, 1)) \text{ where } X_t^0 = (r_0, r_1) \end{aligned} \quad (12)$$

With Equation 12 the code is easier to write, but this approach works for small examples like this one. For more complex systems it's better to design a module for each component and handle the connections more explicitly.

```
const size_t HORIZON = 100;
struct MDP { real_t state[2]; };

int main() {
    std::vector<MDP> mdps(2, {0, 0});

    for (size_t time = 0; time ≤ HORIZON; time++)
        for (size_t r = 0; r < 2; r++) {
            mdps[0].state[r] = mdps[1].state[r]*uniform(urng);
            mdps[1].state[r] = mdps[0].state[r]+uniform(urng);
        }
}
```

Listing 15: software/1200/main.cpp

4.1.3 MDPs network pt.2 [1300]

This example is similar to the one in Section 4.1.2, with a few notable differences:

- $U^i = X^i = Y^i = \mathbb{R} \times \mathbb{R}$
- the initial states are $x_0^0 = (1, 1), x_0^1 = (2, 2)$
- the connections are slightly more complex.
- no probability is involved

Having

$$p((x_0', x_1') | (x_0, x_1), (u_0, u_1)) = \begin{cases} 1 & \text{if ...} \\ 0 & \text{otherwise} \end{cases} \quad (13)$$

The implementation would be

```
int main() {
    std::vector<MDP> mdps({{1, 1}, {2, 2}});

    for (size_t time = 0; time ≤ HORIZON; time++) {
        mdps[0].state[0] =
            .7 * mdps[0].state[0] + .7 * mdps[0].state[1];
        mdps[0].state[1] =
            -.7 * mdps[0].state[0] + .7 * mdps[0].state[1];

        mdps[1].state[0] =
            mdps[1].state[0] + mdps[1].state[1];
        mdps[1].state[1] =
            -mdps[1].state[0] + mdps[1].state[1];
    }
}
```

Listing 16: software/1300/main.cpp

4.1.4 MDPs network pt.3 [1400]

The original model behaves exactly lik Listing 16, with a different implementation. As an exercise, the reader is encouraged to come up with a different implementation for Listing 16.

4.2 Traffic light [2000]

This example models a **traffic light**. The three original versions (2100, 2200 and 2300) have the same behaviour, with a different implementation.

Let T be the MDP that describes the traffic light, s.t.

- $U = \{\varepsilon, \sigma\}$ where
 - ε means “do nothing”
 - σ means “switch light”
- $X = \{\text{green}, \text{yellow}, \text{red}\}$
- $Y = X$
- $g(x) = x$
- $p(x' | x, \varepsilon) = \begin{cases} 1 & \text{if } x' = x \\ 0 & \text{otherwise} \end{cases}$
- $p(x' | x, \sigma) = \begin{cases} 1 & \text{if } (x = \text{green} \wedge x' = \text{yellow}) \vee (x = \text{yellow} \wedge x' = \text{red}) \vee (x = \text{red} \wedge x' = \text{green}) \\ 0 & \text{otherwise} \end{cases}$

Meaning that, if the input is ε , T maintains the same color with probability 1. Otherwise, if the input is σ , T changes color with probability 1, iif the transition is valid (green \rightarrow yellow, yellow \rightarrow red, red \rightarrow green)

```

#include <fstream>
#include <random>

using real_t = double;
using urng_t = std::default_random_engine;
const size_t HORIZON = 1000;

enum Light { GREEN = 0, YELLOW = 1, RED = 2 }; ①

int main() {
    std::random_device random_device;
    urng_t urng(random_device());
    std::uniform_int_distribution<> rand_interval(60, 120); ②
    std::ofstream log("log");

    Light traffic_light = Light::RED;
    size_t next_switch = rand_interval(urng);

    for (size_t time = 0; time ≤ HORIZON; time++) {
        log << time << ' ' << next_switch - time << ' '
            << traffic_light << std::endl;

        if (time < next_switch)
            continue;

        traffic_light = ③
            (traffic_light == RED
             ? GREEN
             : (traffic_light == GREEN ? YELLOW : RED));

        next_switch = time + rand_interval(urng);
    }

    log.close();
    return 0;
}

```

Listing 17: software/2000/main.cpp

TODO:

- ① `enum` vs `enum class`
- ② reference the same trick used in the uniform int distribution example
- ③ is basically the behaviour of the formula described above
- how is the time represented?
- how can it be implemented with mocc?

4.3 Control center

This example adds complexity to the traffic light by introducing a **remote control center**, network faults and repairs. It requires some time (it has too many variants), I'll work on it later.

4.3.1 No network [3100]

4.3.2 Network monitor

4.3.2.1 No faults [3200]

4.3.2.2 Faults & no repair [3300]

4.3.3 Faults & repair [3400]

4.3.4 Faults & repair + correct protocol [3500]

4.4 Statistics

4.4.1 Expected value [4100]

In this one we just simulate a development process (phase 0, phase 1, and phase 2), and we calculate the average ...

4.4.2 Probability [4200]

In this one we simulate a more complex software developmen process, and we calculate the average cost (Wait, what? Do we simulate it multiple times?)

4.5 Development process simulation

An MDP can be implemented by using a **transition matrix** (like in Section 1.2.2.1). The simplest implementation can be done by using a `std::discrete_distribution` by using the trick in Listing 8.

4.5.1 Random transition matrix [5100]

This example builds a **random transition matrix**.

```
const size_t HORIZON = 20, STATES_SIZE = 10;

int main() {
    std::random_device random_device;
    urng_t urng(random_device());
    auto random_state = ①
        std::uniform_int_distribution<>(0, STATES_SIZE - 1);
    std::uniform_real_distribution<> random_real_0_1(0, 1);

    std::vector<std::discrete_distribution<>>
        transition_matrix(STATES_SIZE); ②
    std::ofstream log("log.csv");

    for (size_t state = 0; state < STATES_SIZE; state++) {
        std::vector<real_t> weights(STATES_SIZE); ③
        for (auto &weight : weights)
            weight = random_real_0_1(urng);

        transition_matrix[state] = ④
            std::discrete_distribution<>(weights.begin(),
                                         weights.end());
    }

    size_t state = random_state(urng);
    for (size_t time = 0; time ≤ HORIZON; time++) {
        log << time << " " << state << std::endl;
        state = transition_matrix[state ⑤](urng); ⑥
    }

    log.close();
    return 0;
}
```

Listing 18: software/5100/main.cpp

A **transition matrix** is a `vector<discrete_distribution<>>` ② just like in Listing 8. Why can we do this? First of all, the states are numbered from 0 to `STATES_SIZE - 1`, that's why we can generate a random state ① just by generating a number from 0 to `STATES_SIZE - 1`.

The problem with using a simple `uniform_int_distribution` is that we don't want to choose the next state uniformly, we want to do something like in Figure 5.

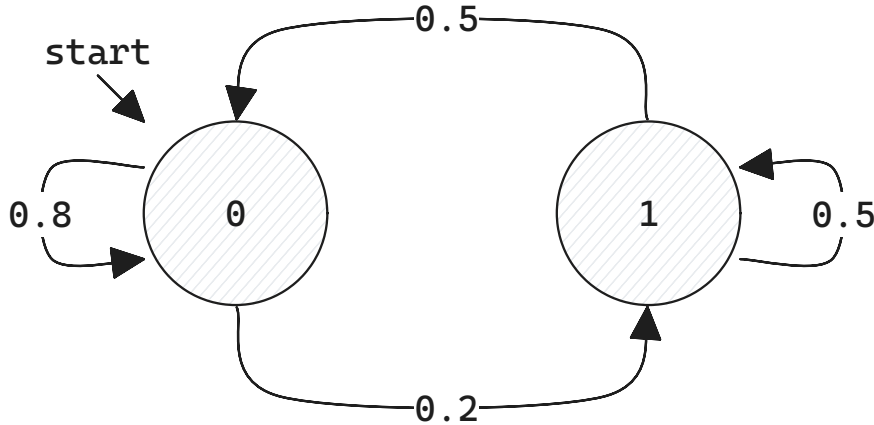


Figure 5: A simple Markov Chain

Luckily for us `std::discrete_distribution<>` does exactly what we want. It takes a list of weights $w_0, w_1, w_2, \dots, w_n$ and assigns each index i the probability $p(i) = \frac{\sum_{i=0}^n w_i}{w_i}$ (the probability is proportional to the weight, so we have that $\sum_{i=0}^n p(i) = 1$ like we would expect in a Markov Chain).

To instantiate the `discrete_distribution` ④, unlike in Listing 8, we need to first calculate the weights ③, as we don't know them in advance.

To randomly generate the next state ⑥ we just have to use the `discrete_distribution` assigned to the current state ⑤.

4.5.2 [5200] Software development & error detection

Our next goal is to model the software development process of a team. Each phase takes the team 4 days to complete, and, at the end of each phase the testing team tests the software, and there can be 3 outcomes:

- **no error** is introduced during the phase (we can't actually know it, let's suppose there is an all-knowing "oracle" that can tell us there aren't any errors)
- **no error detected** means that the "oracle" detected an error, but the testing team wasn't able to find it
- **error detected** means that the "oracle" detected an error, and the testing team was able to find it

If we have **no error**, we proceed to the next phase... the same happens if **no error was detected** (because the testing team sucks and didn't find any errors). If we **detect an error** we either reiterate the current phase (with a certain probability, let's suppose 0.8), or we go back to

one of the previous phases with equal probability (we do this because, if we find an error, there's a high chance it was introduced in the current phase, and we want to keep the model simple).

In this exercise we take the parameters for each phase (the probability to introduce an error and the probability to not detect an error) from a file.

```
#include <...>

using real_t = double;
const size_t HORIZON = 800, PHASES_SIZE = 3;

enum Outcome ① {
    NO_ERROR = 0,
    NO_ERROR_DETECTED = 1,
    ERROR_DETECTED = 2
};

int main() {
    std::random_device random_device;
    std::default_random_engine urng(random_device());
    std::uniform_real_distribution<> uniform_0_1(0, 1);
    std::vector<std::discrete_distribution<>>
        phases_error_distribution;

    {
        std::ifstream probabilities("probabilities.csv");
        real_t probability_error_introduced,
            probability_error_not_detected;

        while (probabilities >> probability_error_introduced >>
            probability_error_not_detected)
            phases_error_distribution.push_back(
                ② std::discrete_distribution<>({
                    1 - probability_error_introduced,
                    probability_error_introduced *
                        probability_error_not_detected,
                    probability_error_introduced *
                        (1 - probability_error_not_detected),
                }));

        probabilities.close();
        assert(phases_error_distribution.size() ==
            PHASES_SIZE);
    }

    real_t probability_repeat_phase = 0.8;

    size_t phase = 0;
    std::vector<size_t> progress(PHASES_SIZE, 0);
```

```

std::vector<Outcome> outcomes(PHASES_SIZE, NO_ERROR);

for (size_t time = 0; time < HORIZON; time++) {
    progress[phase]++;

    if (progress[phase] == 4) {
        outcomes[phase] = static_cast<Outcome>(
            phases_error_distribution[phase](urng));
        switch (outcomes[phase]) {
            case NO_ERROR:
            case NO_ERROR_DETECTED:
                phase++;
                break;
            case ERROR_DETECTED:
                if (phase > 0 && uniform_0_1(urng) >
                    probability_repeat_phase)
                    phase = std::uniform_int_distribution<>(
                        0, phase - 1)(urng);
                break;
        }

        if (phase == PHASES_SIZE)
            break;

        progress[phase] = 0;
    }
}

return 0;
}

```

Listing 19: software/5300/main.cpp

TODO: `class enum` vs `enum`. We can model the outcomes as an `enum`
 ①... we can use the `discrete_distribution` trick to choose randomly
 one of the outcomes ②. The other thing we notice is that we take the
 probabilities to generate an error and to detect it from a file.

4.5.3 Optimizing costs for the development team [5300]

If we want we can manipulate the “parameters” in real life: a better experienced team has a lower probability to introduce an error, but a higher cost. What we can do is:

1. randomly generate the parameters (probability to introduce an error and to not detect it)
2. simulate the development process with the random parameters

By repeating this a bunch of times, we can find out which parameters have the best results, a.k.a generate the lowest development times (there are better techniques like simulated annealing, but this one is simple enough for us).

4.5.4 Key performance index [5400]

We can repeat the process in exercise [5300], but this time we can assign a parameter a certain cost, and see which parameters optimize cost and time (or something like that? Idk, I should look up the code again).

4.6 Complex systems

4.6.1 Insulin pump [6100]

4.6.2 Buffer [6200]

4.6.3 Server [6300]

5 MOCC library

Model CheCking library for the exam

5.1 Design

Basically: the “Observer Pattern” [8] can be used to implement MDPs, because a MDP is like an entity that “is notified” when something happens (receives an input, in fact, in the case of MDPs, another name for input is “action”), and notifies other entities (gives an output, or reward).

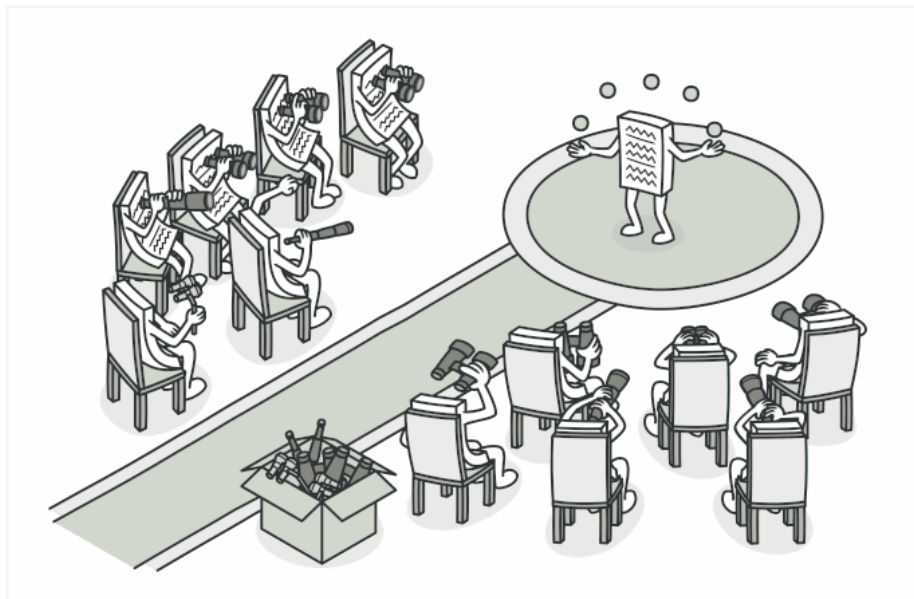


Figure 6: <https://refactoring.guru/design-patterns/observer>

By using the generics (templates) in C++ it's possible to model type-safe MDPs, whose connections are easier to handle (if an entity receives inputs of type Request, it cannot be mistakenly connected to an entity that gives an output of type Time).

5.2 mocc

```
using real_t = double;
```

The `real_t` type is used as an alias for floating point numbers to ensure the same format is used everywhere in the library.

```
using urng_t = std::default_random_engine;
```

The `urng_t` type is used as an alias for `std::default_random_engine` to make the code easier to write.

5.3 math

```
class Stat
```

The `Stat` class is used to calculate the mean and the standard deviation of a set of values (as discussed in Section 1.3.1 and Section 1.3.2)

```
void save(real_t x);
```

The `save()` method is used to add a value to the set of values. The mean and the standard deviation are automatically updated when a new value is saved.

```
real_t mean() const;
```

Returns the precalculated mean.

```
real_t stddev() const;
```

Returns the precalculated standard deviation.

Example

```
Stat cost_stat;

cost_stat.save(302);
cost_stat.save(305);
cost_stat.save(295);
cost_stat.save(298);

std::cout
    << cost_stat.mean() << " "
    << cost_stat.stddev() << std::endl;
```

5.4 time

```
ALIAS_TYPE(T, real_t)
```

The `T` is the type for the **time**, it's represented as a `real_t` to allow working in smaller units of time (for example, when the main unit of time of the simulation is the *minute*, it could still be useful to work with *seconds*). `T` is a **strong alias**, meaning that if a MDP takes in input `T`, it cannot be connected to a MDP that gives in output a simple `real_t`.

```
class Stopwatch : public Observer<>, public Notifier<T>
```

A Stopwatch starts at time `0`, and each iteration of the system it increments its time counter by Δ . It can be used to measure time from a certain point of the simulation (it can be at any point of the simulation). It sends a notification with the elapsed time at each iteration.

```
Stopwatch(real_t delta = 1);
```

The default Δ for the Stopwatch is `1`, but it can be changed. Usually, a Stopwatch is connected to a System.

```
real_t elapsed();
```

Returns the time elapsed since the Stopwatch was started.

```
void update() override;
```

This method **must** be called to update the Stopwatch. It is automatically called when the Stopwatch is connected to a System, or, more generally, to a Notifier<>.

Example

```
System system;
Stopwatch s1, s2(2.5);

size_t iteration = 0;
system.addObserver(&s1);

while (s1.elapsed() < 10000) {
    if (iteration == 1000) system.addObserver(&s2);
    system.next(); iteration++;
}

std::cout << s1.elapsed() << ' ' << s2.elapsed() << std::endl;
```

```
enum class TimerMode { Once, Repeating }
```

A Timer can be either in Repeating mode or in Once mode:

- In Repeating mode, everytime the timer hits 0, it resets
- In Once mode, when the timer hits 0, it stops

```
class Timer : public Observer<>, public Notifier<>
```

A Timer starts with a certain duration. At every iteration the duration decreases by Δ . When a Timer hits 0, it sends a notification to its subscribers (with no input value).

```
Timer(real_t duration, TimerMode mode, real_t delta = 1);
```

A Timer requires the starting duration and it's mode. It's more useful to use the Once mode if the duration is different at each reset, this way it can be set manually.

```
void set_duration(real_t time);
```

Sets the current duration of the Timer. It's useful when the duration is generated randomly each time the Timer hits 0.

```
void update() override;
```

This method must be called to updated the time of the Timer. Generally the Timer is connected to a System.

Example

```
TODO: example
```

5.5 alias

```
template <typename T> class Alias
```

The `class Alias` is used to create **strong aliases** (a strong alias is a type that can be used in place of its underlying type, except in templates, as its considers a totally different type).

```
Alias() {}
```

It initializes the value for the underlying type to its default one.

```
Alias(T value)
```

It initializes the underlying type with a certain value. Useful when the underlying type needs complex initialization. It also allows to assign a value of the underlying type (e.g. `Alias<int> a_int = 5;`).

```
operator T() const
```

Allows the `Alias<T>` to be casted to `T` (e.g. `Alias<int> a_int = 5; int v = (int)a_int;`). The casting doesn't need to be explicit.

```
ALIAS_TYPE(ALIAS, TYPE)
```

The `ALIAS_TYPE` macro is used to quickly create a strong alias. The `Alias<T>` class is never used directly.

5.6 observer

```
template <typename ... T> class Observer
```

- TODO

5.7 notifier

```
template <typename ... T> class Notifier
```

- TODO

5.8 Auxiliary

```
template <typename T> class Recorder : public Observer<T>
```

```
class Client : public Observer<U ...>,
               public Notifier<Observer<U ...> *, T>
```

- TODO (+ using Host)

```
class Server : public Observer<Observer<U ...> *, T>
```

- TODO (+ using Host)

```
class System : public Notifier<>
```

- TODO

6 Practice

In short, every system can be divided into 4 steps:

- reading parameters from a file (from files as of 2024/2025)
- initializing the system
 - this include instantiating the MDPs and connecting them
- simulating the system
- saving outputs to a file

```
std::ifstream params("parameters.txt");
char c;

while (params >> c) ①
    switch (c) {
        case 'A': params >> A; break;
        case 'B': params >> B; break;
        case 'C': params >> C; break;
        case 'D': params >> D; break;
        case 'F': params >> F; break;
        case 'G': params >> G; break;
        case 'N': params >> N; break;
        case 'W': params >> W; break;
    }

params.close();
```

Listing 20: practice/1/main.cpp

Reading the input: `std::ifstream` can read (from a file) based on the type of the variable read. For example, `c` is a `char`, so ① will read exactly 1 character. If `c` was a string, `params >> c` would have read a whole word (up to the first whitespace). For example, `A` is a float and `N` is a int, so `params >> A` will try to read a float and `params >> N` will **try** to read an int. (TODO: float → `real_t`, int → `size_t`)

```
#ifndef PARAMETERS_HPP_
#define PARAMETERS_HPP_

#include "../mocc/alias.hpp" ①
#include "../mocc/mocc.hpp" ②

ALIAS_TYPE(ProjInit, real_t) ③
ALIAS_TYPE(TaskDone, real_t) ③
ALIAS_TYPE(EmplCost, real_t) ③

static ④ real_t A, B, C, D, F, G;
static size_t N, W, HORIZON = 100000;

#endif
```


Listing 21: practice/1/parameters.hpp

The parameters are declared in a `parameters.hpp` file, for a few reasons

- they are declared globally, and are globally accessible without having to pass to classes constructors
- any class can just import the file with the parameters to access the parameters
- they are static ④ (otherwise clang doesn't like global variables)
- in `parameters.hpp` there are also auxiliary types ③, used in the connections between entities

```
System system; ①
Stopwatch stopwatch; ②

system.addObserver(&stopwatch); ③

while (stopwatch.elapsed() ≤ HORIZON) ④
    system.next(); ⑤
```

Simulating the system is actually easy:

- declare the system ①
- add a stopwatch ② (which starts from time 0, and everytime the system is updated, it adds up time)
 - it is needed to stop the simulation after a certain amount of time, called HORIZON
- connect the stopwatch to the system ③
- run a loop (like how a game loop would work) ④
- in the loop, transition the system to the next state ⑤

6.1 Development team (time & cost)

6.1.1 Employee

```
#ifndef EMPLOYEE_HPP_
#define EMPLOYEE_HPP_

#include <random>

#include "../mocc/stat.hpp"
#include "../mocc/time.hpp"
#include "parameters.hpp"

class Employee : public Observer<T>,
                 public Observer<ProjInit>,
                 public Notifier<TaskDone, EmplCost> {

    std::vector<std::discrete_distribution<>>
        transition_matrix;
```

```

urng_t &urng;
size_t phase = 0;
real_t proj_init = 0;

public:
    const size_t id;
    const real_t cost;
    Stat comp_time_stat;

    Employee(urng_t &urng, size_t k)
        : urng(urng), id(k),
          cost(1000.0 - 500.0 * (real_t)(k - 1) / (W - 1)) {

        transition_matrix =
            std::vector<std::discrete_distribution<>>(N);

        for (size_t i = 1; i < N; i++) {
            size_t i_0 = i - 1;
            real_t tau = A + B * k * k + C * i * i + D * k * i,
                  alpha = 1 / (F * (G * W - k));

            std::vector<real_t> p(N, 0.0);
            p[i_0] = 1 - 1 / tau;
            p[i_0 + 1] =
                (i_0 == 0 ? (1 - p[i_0])
                 : (1 - alpha) * (1 - p[i_0]));

            for (size_t prev = 0; prev < i_0; prev++)
                p[prev] = alpha * (1 - p[i_0]) / i_0;

            transition_matrix[i_0] =
                std::discrete_distribution<>(p.begin(),
                                              p.end());
        }

        transition_matrix[N - 1] =
            std::discrete_distribution<>{1};
    }

    void update(T t) override {
        if (phase < N - 1) {
            phase = transition_matrix[phase](urng);
            if (phase == N - 1) {
                comp_time_stat.save(t - proj_init);
                notify((real_t)t, cost);
            }
        }
    };

    void update(ProjInit proj_init) override {
        this->proj_init = proj_init;
    }

```

```
        phase = 0;
    };
};

#endif
```

Listing 22: practice/1/employee.hpp

6.1.2 Director

6.2 Task management

6.2.1 Worker

6.2.2 Generator

6.2.3 Dispatcher (not the correct name)

6.2.4 Manager (not the correct name)

6.3 Backend load balancing

6.3.1 Env

6.3.2 Dispatcher, Server and Database

6.3.3 Response time

6.4 Heater simulation

7 Extras

7.1 VDM (Vienna Development Method)

“The Vienna Development Method (VDM) is one of the longest established model-oriented formal methods for the development of computer-based systems and software. It consists of a group of mathematically well-founded languages and tools for expressing and analyzing system models during early design stages, before expensive implementation commitments are made. The construction and analysis of the model help to identify areas of incompleteness or ambiguity in informal system specifications, and provide some level of confidence that a valid implementation will have key properties, especially those of safety or security. VDM has a strong record of industrial application, in many cases by practitioners who are not specialists in the underlying formalism or logic. Experience with the method suggests that the effort expended on formal modeling and analysis can be recovered in reduced rework costs arising from design errors.” [9]

7.1.1 It’s cool, I promise

- Alloy? Maybe it’s a good alternative, haven’t tried it enough
- VDM is basically OCL (Object Constraint Language) but better.

7.1.2 VDM++ to design valid UMLs

7.2 Advanced testing techniques (in Rust & C)

- TODO: cite “Rust for Rustaceans”
- TODO: unit tests aren’t the only type of test

7.2.1 Mocking (mockall)

7.2.2 Fuzzing (cargo-fuzz)

7.2.3 Property-based testing

7.2.4 Test augmentation (Miri, Loom, Valgrind)

7.2.5 Performance testing

- Rust is very focused on performance
- TODO: non-functional requirements

7.3 Model checking with Bevy (Rust)

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