# Software Engineering

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# 1 Software models

When designing **complex software** we have to make major **design choices** at the beginning of the project. Often those choices can't be driven by experience or reasoning alone, that's why a **model** of the project is needed to compare different solutions. Our formal tool of choice is the **Discrete Time Markov Chain** (Section 1.2.3).

# 1.1 The "Amazon Prime Video" article

If you were tasked with designing the software architecture for **Amazon Prime Video** (a live streaming service for Amazon), how would you go about it? What if you had the **non-functional requirement** to keep the costs as low as possible?

In a recent article, Marcin Kolny, a Senior SDE at Prime Video, describes how they "reduced the cost of the audio/video monitoring infrastructure by 90%" [1] by using a monolith application instead of distributed microservices (an outcome one wouldn't usually expect).

While there isn't always definitive answer, one way to go about this kind choice is building a model of the system to compare the solutions. In the case of Prime Video, "the audio/video monitoring service consists of three major components:" [1]

- the media converter converts input audio/video streams
- the **defect detectors** execute algorithms that analyze frames and audio buffers in real-time looking for defects and send notifications
- the **orchestrator** controls the flow in the service

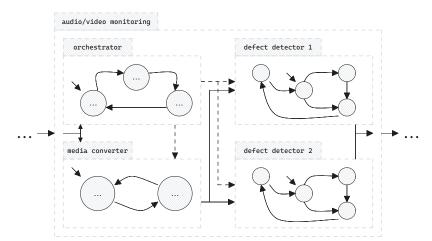


Figure 1: Model of the audio/video monitoring system

We want to model the components as some kind of stateful machine (with inputs and outputs, Figure 1), interconnect them and **simulate** the behaviour of the system as a whole.

#### 1.2 Formal notation

#### 1.2.1 The concept of time

TODO: rewrite

The models treated in the course evolve through **time**. Time can be modeled in many ways (I guess?), but, for the sake of simplicity, we will consider discrete time. Let W be the 'weather system' and D the 'driving ability' system in Section 1.2, we can define the evolution of D as

$$D(0) = \text{'good'}$$

$$D(t+d) = f(D(t), W(t))$$
(1)

Given a time instant t (let's suppose 12:32) and a time interval d (1 minute), the driving ability of D at 12:33 depends on the driving ability of D at the time 12:32 and the weather at 12:32.

#### 1.2.2 Markov Chain

A Markov Chain is...

#### 1.2.3 DTMC (Discrete Time Markov Chain)

A DTMC M is a tuple (U, X, Y, p, g) s.t.

- $U \neq \emptyset \land X \neq \emptyset \land Y \neq \emptyset$  (otherwise stuff doesn't work)
- U can be either
  - $\{u_1, ..., u_n\}$  where  $u_i$  is an input value
  - $\{()\}$  if M doesn't take any input
- $X = \{x_1, ..., x_n\}$  where  $x_i$  is a state
- $Y = \{y_1, ..., y_n\}$  where  $y_i$  is an output value
- $p: X \times X \times U \rightarrow [0,1]$  is the transition function
- $g: X \to Y$  is the output function

$$\forall x \in X \ \forall u \in U \ \sum_{x' \in X} p(x'|x, u) = 1$$
 (2)

$$M(0) = x_1$$

$$M(t+d) = \begin{cases} x_1 & \text{with probability} \ \ p(x_1|M(t),U(t)) \\ x_2 & \text{with probability} \ \ p(x_2|M(t),U(t)) \\ \dots \end{cases} \tag{3}$$

It's interesting to notice that the transition function depends on the input values. If you consider the 'driving ability' system in Section 1.2, you can see that the probability to go from good to bad is higher if the weather is rainy and lower if it's sunny.

#### 1.2.3.1 An example of DTMC

Let's consider the development process of a team. We can define a DTMC M=(U,X,Y,p,g) s.t.

- $U = \{()\}$ , as it doesn't have any input
- $X = \{0, 1, 2, 3\}$
- $Y = \text{Cost} \times \text{Duration (in months)}$

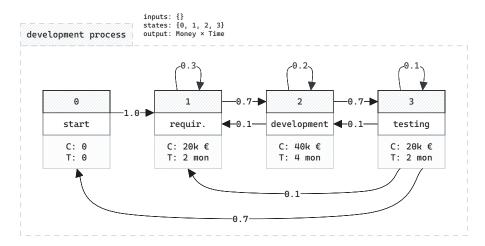


Figure 2: the model of a team's development process

$$g(x) = \begin{cases} (0,0) & \text{if } x = 0\\ (20000,2) & \text{if } x = 1\\ (40000,4) & \text{if } x = 2\\ (20000,2) & \text{if } x = 3 \end{cases} \tag{4}$$

#### 1.2.4 Network of Markov Chains

TODO...

# 1.3 Tips and tricks

#### 1.3.1 Mean

TODO: 'mean' trick, ggwp

$$\varepsilon_n = \frac{\sum_{i=0}^n v_i}{n}$$

$$\varepsilon_{n+1} = \frac{\sum_{i=0}^{n+1} v_i}{n+1} = = \frac{\left(\sum_{i=0}^n v_i\right) + v_{n+1}}{n+1} = \frac{\sum_{i=0}^n v_i}{n+1} + \frac{v_{n+1}}{n+1} = (5)$$

$$\frac{\left(\sum_{i=0}^n v_i\right)n}{(n+1)n} + \frac{v_{n+1}}{n+1} = \frac{\sum_{i=0}^n v_i}{n} \cdot \frac{n}{n+1} + \frac{v_{n+1}}{n+1} = \frac{\varepsilon_n \cdot n + v_{n+1}}{n+1}$$

# 1.3.2 Eulero's method for differential equations

Useful later...

This section will cover the basics needed for the exam.

#### 2.1 Useful #include <random> features not in C

The <random> library offers useful tools to build our models. It makes Markov Chains and probabilistic models really easy to implement.

#### $2.1.1 \; \text{random}$ () $vs \; \text{random\_device} \; vs \; \text{default\_random\_engine}$

In C++ there are many ways to **generate random numbers**, I'm gonna keep it short and sweet: don't use random(), use std::random\_device to generate the **seed** and from then on just some random engine like std::default\_random\_engine.

```
#include <iostream>
#include <random>
int main() {
    std::cout << random() ① << std::endl;

    std::random_device random_device; ②
    std::cout << random_device() ③ << std::endl;

    std::default_random_engine r_engine(random_device() ④ );
    std::cout << r_engine() ⑤ << std::endl;
}</pre>
```

Listing 1: examples/random.cpp

I'll explain: random() ① doesn't work very well (TODO: link to the article\*), you're encouraged to use the generators C++ offers... but each works in a different way, and you have to choose the best one depending on your needs. std::random\_device ② is used to generate the seed ④ because it uses device randomness (if available, TODO: link to docs / article \*), but it's really slow. That seed is used to to instantiate one of the other engines ⑤, like ::default\_random\_engine (TODO: link with different engines and types). TODO BONUS: only r\_eng used with distr

#### Note:

If you see ③ and ⑤, random\_device and r\_engine aren't functions, they are instances, but you can call the () operator on them because C++ has operator overloading, and it allows you to call custom operators on instances... the same goes for std::cout and <<

#### 2.1.2 Distributions

Just the capability of generating random numbers isn't enough, we often need to manipulate those numbers to fit our needs. Luckly, C++ covers basically all of them... for example, this is how easy it is to simulate a transition matrix in Figure 2:

```
_____
 #include <iostream>
 #include <random>
 const size t HORIZON = 15;
 int main() {
     std::random device random device;
     std::default_random_engine random_engine(random_device());
     std::discrete_distribution<size_t> transition_matrix[] = {
         \{0, 1\},\
         {0, .3, .7},
{0, .2, .2, .6},
         \{0, .1, .2, .1, .6\},\
          {1},
     };
     size_t state = 0;
     for (size_t time = 0; time < HORIZON; time++) {</pre>
         state = transition_matrix[state](random_engine);
         std::cout << state << std::endl;</pre>
     }
 }
                          ______
             Listing 2: examples/transition_matrix.cpp
2.1.2.1 \; \mathsf{std}:: \mathsf{uniform\_int\_distribution}
2.1.2.2\; {\tt std::uniform\_real\_distribution}
2.1.2.3 std::bernoulli_distribution
2.1.2.4 std::poisson_distribution
2.1.2.5 \ \mathsf{std}{::} \mathsf{geometric\_distribution}
2.1.2.6 std::discrete distribution
2.2 Dynamic structures
2.2.1 std::vector<T>() instead of malloc()
2.2.2 \text{ std::deque<T>()}
```

- 2.2.3 Sets
- **2.2.4** Maps
- 2.3 I/O
- 2.3.1 #include <iostream>
- **2.3.2** Files

# 3 Exercises

Each exercise has 4 digits xxxx that are the same as the ones in the software folder in the course material.

#### **3.1** [1000] First examples

Now we have to put together our **formal definitions** and our C++ knowledge to build some simple DTMCs and networks.

#### 3.1.1 [1100] A simple Markov Chain

Let's begin our modeling journey by implementing a DTMC M s.t.

- $U = \{()\}$  it takes no input
- $X = [0,1] \times [0,1]$  it has infinite states (all the pairs of real numbers between 0 and 1)
- $Y = [0,1] \times [0,1]$
- $p: X \times X \times U \rightarrow X = \mathcal{U}(0,1) \times \mathcal{U}(0,1)$
- $g: X \to Y: (r_0, r_1) \mapsto (r_0, r_1)$  it outputs the current state
- X(0) = (0,0)

```
#include <fstream>
#include <random>

using real_t = double;

int main() {
    std::random_device random_device;
    std::default_random_engine random_engine(random_device());
    std::uniform_real_distribution<real_t> uniform(0, 1); 1)

const size_t HORIZON = 10; 2
    std::vector<real_t> state(2, 0); 3)

for (size_t time = 0; time <= HORIZON; time++)
    for (auto &r : state)
        r = uniform(random_engine); 4)

return 0;
}</pre>
```

Listing 3: software/1100/main.cpp

#### 3.1.2 [1200] Connect Markov Chains pt.1

In this exercise we build 2 markov chains, and connect them...

Now let's model a system with two DTMCs  $M_0, M_1,$  and lets define the functions

$$U(M_0,t+1)=\cdots\,U(M_1,t+1)=\cdots$$

## 3.1.3 [1300] Connect Markov Chains pt.2

The same as above, but with a different connection

#### 3.1.4 [1400] Connect Markov Chains pt.3

The same as above, but with a different connection

# 3.2 [2100, 2200, 2300] Traffic light

This is

# **3.3** [3000] Control center

- 3.3.1 [3100] No network
- 3.3.2 [3200] Network monitor (no faults)
- 3.3.3 [3300] Network monitor (faults, no repair)
- 3.3.4 [3400] Network monitor (faults, repair)
- 3.3.5 [3500] Network monitor (faults, repair, correct protocol)
- **3.4** [4000] Statistics
- 3.4.1 [4100] Expected value
- 3.4.2 [4200] Probability

#### 3.5 [5000] Transition matrix

One of the ways to implement a Markov Chain (like in Section 1.2.2) is by using a **transition matrix**. The simplest implementation can be done by using a std::discrete\_distribution by using the trick in Listing 2.

#### 3.5.1 [5100] Random transition matrix

In this example we build a random transition matrix.

```
#include <fstream>
#include <random>
#include <vector>
using real t = double;
const size_t HORIZON = 20, STATES_SIZE = 10;
int main() {
    std::random_device random_device;
    std::default_random_engine random_engine(random_device());
    auto random_state = (1)
        std::uniform_int_distribution<>(0, STATES_SIZE - 1);
    std::uniform_real_distribution<> random_real_0_1(0, 1);
    std::vector<std::discrete_distribution<>>
        transition matrix(STATES SIZE); (2)
    std::ofstream log("log.csv");
    for (size_t state = 0; state < STATES_SIZE; state++) {</pre>
        std::vector<real_t> weights(STATES_SIZE); 3
        for (auto &weight : weights)
            weight = random_real_0_1(random_engine);
        transition_matrix[state] = 4
            std::discrete distribution<>(weights.begin(),
                                          weights.end());
   }
    size_t state = random_state(random_engine);
    for (size_t time = 0; time <= HORIZON; time++) {</pre>
        log << time << " " << state << std::endl;
        state = transition_matrix[state (5)](random_engine); (6)
   }
    log.close();
    return 0;
}
```

Listing 4: software/5100/main.cpp

A transition matrix is a vector<discrete\_distribution<>> ② just like in Listing 2. Why can we do this? First of all, the states are numbered from 0 to STATES\_SIZE - 1, that's why we can generate a random state ① just by generating a number from 0 to STATES\_SIZE - 1.

The problem with using a simple uniform\_int\_distribution is that we don't want to choose the next state uniformly, we want to do something like in Figure 3.

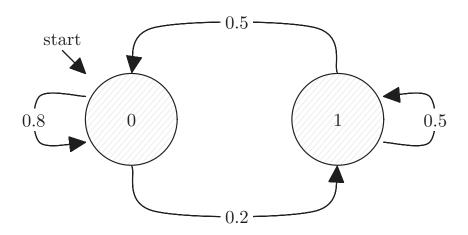


Figure 3: A simple Markov Chain

Luckly for us std::discrete\_distribution<> does exactly what we want. It takes a list of weights  $w_0, w_1, w_2, ..., w_n$  and assigns each index i the probability  $p(i) = \frac{\sum_{i=0}^n w_i}{w_i}$  (the probability is proportional to the weight, so we have that  $\sum_{i=0}^n p(i) = 1$  like we would expect in a Markov Chain).

To instantiate the discrete\_distribution ④, unlike in Listing 2, we need to first calculate the weights ③, as we don't know them in advance.

To randomly generate the next state 6 we just have to use the discrete\_distribution assigned to the current state 5.

#### 3.5.2 [5200] Software development & error detection

Our next goal is to model the software development process of a team. Each phase takes the team 4 days to complete, and, at the end of each phase the testing team tests the software, and there can be 3 outcomes:

- no error is introduced during the phase (we can't actually know it, let's suppose there is an all-knowing "oracle" that can tell us there aren't any errors)
- no error detected means that the "oracle" detected an error, but the testing team wasn't able to find it

• error detected means that the "oracle" detected an error, and the testing team was able to find it

If we have **no error**, we proceed to the next phase... the same happens if **no error was detected** (because the testing team sucks and didn't find any errors). If we **detect an error** we either reiterate the current phase (with a certain probability, let's suppose 0.8), or we go back to one of the previous phases with equal probability (we do this because, if we find an error, there's a high chance it was introduced in the current phase, and we want to keep the model simple).

In this exercise we take the parameters for each phase (the probability to introduce an error and the probability to not detect an error) from a file.

```
#include <...>
using real t = double;
const size t HORIZON = 800, PHASES SIZE = 3;
enum Outcome (1) {
   NO ERROR = 0,
    NO ERROR DETECTED = 1,
    ERROR DETECTED = 2
};
int main() {
    std::random_device random_device;
    std::default_random_engine urng(random_device());
    std::uniform_real_distribution<> uniform_0_1(0, 1);
    std::vector<std::discrete distribution<>>
        phases error distribution;
    {
        std::ifstream probabilities("probabilities.csv");
        real_t probability_error_introduced,
            probability_error_not_detected;
        while (probabilities >> probability_error_introduced >>
               probability_error_not_detected)
            phases_error_distribution.push_back(
                2 std::discrete_distribution<>({
                    1 - probability error introduced,
                    probability_error_introduced *
                        probability_error_not_detected,
                    probability error introduced *
                        (1 - probability_error_not_detected),
                }));
```

```
probabilities.close();
        assert(phases_error_distribution.size() ==
               PHASES_SIZE);
    }
    real t probability repeat phase = 0.8;
    size t phase = 0;
    std::vector<size t> progress(PHASES SIZE, 0);
    std::vector<Outcome> outcomes(PHASES_SIZE, NO_ERROR);
    for (size_t time = 0; time < HORIZON; time++) {</pre>
        progress[phase]++;
        if (progress[phase] == 4) {
            outcomes[phase] = static cast<Outcome>(
                phases_error_distribution[phase](urng));
            switch (outcomes[phase]) {
            case NO ERROR:
            case NO_ERROR_DETECTED:
                phase++;
                break;
            case ERROR DETECTED:
                if (phase > 0 && uniform 0 1(urng) >
                                      probability repeat phase)
                    phase = std::uniform int distribution<>(
                         0, phase - 1)(urng);
                break:
            }
            if (phase == PHASES_SIZE)
                break;
            progress[phase] = 0;
        }
    }
    return 0;
}
```

Listing 5: software/5300/main.cpp

TODO: class enum vs enum. We can model the outcomes as an enum ①... we can use the discrete distribution trick to choose randomly one of the outcomes ②. The other thing we notice is that we take the probabilities to generate an error and to detect it from a file.

# 3.5.3 [5300] Optimizing costs for the development team

If we want we can manipulate the "parameters" in real life: a better experienced team has a lower probability to introduce an error, but a higher cost. What we can do is:

- 1. randomly generate the parameters (probability to introduce an error and to not detect it)
- 2. simulate the development process with the random parameters

By repeating this a bunch of times, we can find out which parameters have the best results, a.k.a generate the lowest development times (there are better techinques like simulated annealing, but this one is simple enough for us).

# 3.5.4 [5400] Key performance index

We can repeat the process in exercise [5300], but this time we can assign a parameter a certain cost, and see which parameters optimize cost and time (or something like that? Idk, I should look up the code again).

# 3.6 [6000] Complex systems

- 3.6.1 [6100] Insulin pump
- 3.6.2 [6200] Buffer
- 3.6.3 [6300] Server
- 4 Exam
- 4.1 Development team (time & cost)
- 4.2 Backend load balancing
- 4.3 Heater simulation
- 5 CASE library

TODO...

# Bibliography

[1] Marcin Kolny, "Scaling up the Prime Video Audio-Video Monitoring Service and Reducing Costs by 90%." Accessed: Mar. 25, 2024. [Online]. Available: https://web.archive.org/web/20240325042615/https://www.primevideotech.com/video-streaming/scaling-up-the-prime-video-audio-video-monitoring-service-and-reducing-costs-by-90#expand