

3. Big-O notation

- Rank the following in order of increasing run times (shortest to longest), if they are same list them together.

$O(N)$	$O(\infty)$	$O(NM)$	$O(\sqrt{N})$	$O(5)$	$O(N^2)$	$O(N^{1.5})$
$O(\log N)$	$O(N \log N)$		$O(0)$	$O(N^4)$	$O(2/N)$	$O(2^N)$

- What is the complexity of each of the following pieces code? Show work.

i.	<pre>sum = 0; for (i = 0; i < n; i++) { sum++; }</pre>
ii.	<pre>sum = 0; for (i = 0; i < n; i++) { for (j = 0; j < n; j++) { sum++; } }</pre>
iii.	<pre>sum = 0; for (i = 0; i < n; i++) { for (j = 0; j < i; j++) { sum++; } }</pre>
iv.	<pre>sum = 0; for (i = 0; i < n * n; i++) { for (j = 0; j < n * n; j++) { sum++; } }</pre>

4. Project 6 on Page 57 from book

i. Most efficient, $O(N)$ - the program will run data as efficient as the size of the data, the size and efficiency essentially go up at the same rate. One loop through data for each n

ii. 3rd most efficient, $O(N^2)$ - the program must run through the length of data twice, as a result the program must go through the loop n^2 times.

iii. 2nd most efficient $O(NM)$ - the program must go through the loop through the entire data (n) for the first for loop and follows up to the current index for the second index (m). As a result the program goes through the loop nm times.

iv. Least efficient $O(n^4)$ - the program must go through the data n^2 times for the first for loop and n^2 times for the second for loop resulting in a very inefficient loop traverse going through n^4 times.