

# **South China University of Technology**

# 《机器学习》课程实验报告

学	院	<u>软件学院</u>		
专	业.	软件工程		
组	员 .	李嘉灏		
学	号 _	20153061951		
山	箱	786699266@qq. com		
指导教师		吴庆耀		
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- 1. 实验题目: 逻辑回归、线性分类与随机梯度下降
- 2. 实验时间: 2017 年 12 月 13 日
- 3. 报告人:李嘉灏
- 4. 实验目的:
- 1. 对比理解梯度下降和随机梯度下降的区别与联系。
- 2. 对比理解逻辑回归和线性分类的区别与联系。
- 3. 进一步理解 SVM 的原理并在较大数据上实践。

## 5. 数据集以及数据分析:

实验使用的是 LIBSVM Data 的中的 a9a 数据,包含 32561 / 16281 (testing) 个样本,每个样本有 123/123 (testing) 个属性。

其中 label 表示该记录的类别,+1 为正类,-1 为负类。其中正类有 11687 个样本,负类有 37155 个样本。

#### 6. 实验步骤:

#### 逻辑回归与随机梯度下降

- 1. 读取实验训练集和验证集。
- 2. 逻辑回归模型参数初始化,可以考虑全零初始化,随机初始化或者正态分布初始化。
- 3. 选择Loss函数及对其求导,过程详见课件ppt。
- 4. 求得**部分样本**对Loss函数的梯度G。
- 5. 使用不同的优化方法更新模型参数 (NAG, RMSProp, AdaDelta和Adam)。
- 6. 选择合适的阈值,将验证集中计算结果**大于阈值的标记为正类,反之为负类**。在验证集上测试并得到不同优化方法的 Loss函数值 $L_{NAG}$ , $L_{RMSProp}$ , $L_{AdaDelta}$ 和 $L_{Adam}$ 。
- 7. 重复步骤4-6若干次,**画出** $L_{NAG}$ , $L_{RMSProp}$ , $L_{AdaDelta}$ 和 $L_{Adam}$ **随迭代次数的变化图**。

#### *线性分类与随机梯度下降*

- 1. 读取实验训练集和验证集。
- 2. 支持向量机模型参数初始化,可以考虑全零初始化,随机初始化或者正态分布初始化。
- 3. 选择Loss函数及对其求导,过程详见课件ppt。
- 4. 求得**部分样本**对Loss函数的梯度G。
- 5. 使用不同的优化方法更新模型参数 (NAG, RMSProp, AdaDelta和Adam) 。
- 6. 选择合适的阈值,将验证集中计算结果**大于阈值的标记为正类,反之为负类**。在验证集上测试并得到不同优化方法的 Loss函数值 $L_{NAG}$ , $L_{RMSProp}$ , $L_{AdaDelta}$ 和 $L_{Adam}$ 。
- 7. 重复步骤4-6若干次,**画出L\_{NAG},L\_{RMSProp},L\_{AdaDelta}和L\_{Adam}随迭代次数的变化图。**

## 7. 代码:

## 逻辑回归:

```
from sklearn import datasets, model_selection, linear_model
 import numpy as np
 import jupyter
 import matplotlib.pyplot as plt
 import math
 import random
X_train, y_train = datasets.load_symlight_file("a9atrain.txt")
x_{=} = np.array(X_train.toarray(), np.float32).reshape((-1, 123))
y_ = np.array(y_train, np.float32).reshape((-1, 1))
for i in range(y_.shape[0]):
    if y_[i,0] == -1.0 : y_[i,0] = 0.
X_ = np.hstack([x_, np.ones((x_.shape[0], 1))])
X_test, y_test = datasets.load_symlight_file("a9atest.txt")
xt_ = np.array(X_test.toarray(), np.float32).reshape((-1, 122))
yt_ = np.array(y_test, np.float32).reshape((-1, 1))
for i in range(yt .shape[0]):
     if yt [i,0] == -1.0: yt [i,0] = 0.
Xt_{=} = np.hstack([xt_{,} np.zeros((xt_{,shape[0], 1)),np.ones((xt_{,shape[0], 1))])
def h_theta(Xi, Theta):
    e_t = math.exp(Xi.dot(Theta.T))
return e_t / (1 + e_t)
def compute_loss(X, y, Theta):
    m = y.shape[0]
    loss = 0.
    for i in range(m):
         loss += (y[i] * math.log(h_theta(X[i,:], Theta))) + ((1 - y[i]) * math.log(1 - h_theta(X[i,:], Theta)))
    loss /= - m
    return loss
def compute gradient(X, y, Theta):
    m = y.shape[0]
    gradient = np.zeros(Theta.shape)
    for i in range(m):
    \begin{array}{lll} & \text{gradient} \ += \ (h\_\text{theta}(X[\text{i, :}], \ \text{Theta}) \ - \ y[\text{i]}) \ * \ (X[\text{i, :}]) \\ & \text{gradient} \ /= \ m \end{array}
```

```
def train_model_nag(X, y, Theta, learning_rate, gamma, iteration = 10000):
    test_loss_history = np.zeros((iteration, 1))
    v = np.zeros(Theta.shape)
    Theta_gradient = np.zeros(Theta.shape)
    for iter in range(iteration):
         index = random.randint(0, y.shape[0]-10)
         Theta = Theta - gamma * v
v = gamma * v - learning_rate * compute_gradient(X[index:index+10,:], y[index:index+10], Theta)
         Theta = Theta + v
         test_loss_history[iter] = compute_loss(Xt_, yt_, Theta)[-1:]
    return test_loss_history, Theta
def train_model_rmsprop(X, y, Theta, learning_rate, gamma, epsilon, iteration = 10000):
    test loss history = np.zeros((iteration, 1))
    Gt = 0.
    Theta_gradient = np.zeros(Theta.shape)
    for iter in range(iteration):
         index = random.randint(0, y.shape[0]-10)
         Theta_gradient = compute_gradient(X[index:index+10,:], y[index:index+10], Theta)
        G_t = gamma * G_t + (1 - gamma) * Theta_gradient.dot(Theta_gradient.T)
Theta = Theta - (learning_rate / np.sqrt(G_t + epsilon)) * Theta_gradient
test_loss_history[iter] = compute_loss(Xt_, yt_, Theta)[-1:]
    return test_loss_history, Theta
```

return gradient

```
def train_model_adadelta(X, y, Theta, gamma, epsilon, iteration):
    test_loss_history = np.zeros((iteration, 1))
    Theta_gradient = np.zeros(Theta.shape)
    G_t = 0.
    delta_theta = np.zeros(Theta.shape)
    delta_t = 0.03
    for iter in range(iteration):
        index = random.randint(0, y.shape[0]-10)
        Theta_gradient = compute_gradient(X[index:index+10,:], y[index:index+10], Theta)
        G_t = gamma * G_t + (1 - gamma) * Theta_gradient.dot(Theta_gradient.T)
        delta_theta = - (np.sqrt(delta_t + epsilon) / np.sqrt(G_t + epsilon)) * Theta_gradient
        Theta = Theta + delta theta
        delta_t = gamma * delta_t + (1 - gamma) * (delta_theta.dot(delta_theta.T))
        test_loss_history[iter] = compute_loss(Xt_, yt_, Theta)[-1:]
    return test_loss_history, Theta
def train_model_adam(X, y, Theta, learning_rate, beta1, beta2, epsilon, iteration):
    test_loss_history = np.zeros((iteration, 1))
    Theta gradient = np.zeros(Theta.shape)
    v t = 0.
    m_t = np.zeros(Theta.shape)
    for iter in range(iteration):
        index = random.randint(0, y.shape[0]-10)
        Theta_gradient = compute_gradient(X[index:index+10,:], y[index:index+10], Theta)
        m_t = beta1 * m_t + (1 - beta1) * Theta_gradient
v_t = beta2 * v_t + (1 - beta2) * Theta_gradient.dot(Theta_gradient.T)
        mt_estimate = m_t / (1 - pow(beta1, iter + 1))
wt_estimate = v_t / (1 - pow(beta2, iter + 1))
Theta = Theta - learning_rate * mt_estimate / (np.sqrt(vt_estimate) + epsilon)
        test_loss_history[iter] = compute_loss(Xt_, yt_, Theta)[-1:]
    return test_loss_history, Theta
iteration = 1000
be1 = 0.9
be2 = 0.999
ep = 1e-8
t_nag = np.zeros((1, 124))
t_rmsprop = np.zeros((1, 124))
t_adadelta = np.zeros((1, 124))
t adam = np.zeros((1, 124))
```

```
bel = 0.9
bel = 0.9
bel = 1e-8
t_nag = np.zeros((1, 124))
t_msprop = np.zeros((1, 124))
t_adadelta = np.zeros((1, 124))

t_adam = np.zeros((1, 124))

nag_loss_history, t_mag = train_model_nag(X_, y_, t_nag, 0.005, bel, iteration)
rmsprop_loss_history, t_rmsprop = train_model_msprop(X_, y_, t_rmsprop, 0.005, bel, ep, iteration)
adadelta_loss_history, t_adadelta = train_model_adadelta(X_, y_, t_adadelta, bel, ep, iteration)
adam_loss_history, t_adam = train_model_adam(X_, y_, t_adam, 0.005, bel, bel, ep, iteration)

plt.plot(nag_loss_history, 'g', label='NAG')
plt.plot(rmsprop_loss_history, 'b', label='NAGProp')
plt.plot(adadelta_loss_history, 'y', label='AdaDelta')
plt.plot(adadelta_loss_history, 'y', label='AdaDelta')
plt.legend(loc='upper right')
plt.ylabel('iteration_count')
plt.xlabel('iteration_count')
plt.title('loss_graph')
plt.show()
```

## 线性分类:

```
import numpy
import random
import jupyter
import math
from sklearn.datasets import load_svmlight_file
from sklearn.model_selection import train_test_split
from matplotlib import pyplot

x, y_train = load_svmlight_file("a9atrain.txt")
x_train = x.toarray()
x, y_test = load_svmlight_file("a9atest.txt")
x_test = x.toarray()
X_train = numpy.hstack([x_train, numpy.ones((x_train.shape[0], 1))])
X_test = numpy.hstack([x_test, numpy.ones((x_test.shape[0], 1))])
X_test = numpy.hstack([X_test, numpy.ones((x_test.shape[0], 1))])
```

```
def compute_grad(x, y, w):
    gradient = x * (y - x.dot(w.T))
    return gradient

def compute_loss(x, y, w, random_i):
    loss = 0
    a = len(random_i)
    for m in range(a):
        loss += 0.5 * ((y[random_i[m]] - x[random_i[m],:].dot(w.T)) ** 2)
    return loss/a
```

```
def NAG_train(x, y, x_test, y_test, w, C, lr, gamma, threshold, iteration):
   vt = numpy.zeros(w.shape)
   loss history = []
   test_loss_history = []
   random_index = []
   random_test_index = []
   for i in range(iteration):
       random num = random.randint(0, x.shape[0]-1)
       random_test_num = random.randint(0, x_test.shape[0]-1)
       random index.append(random num)
       random_test_index.append(random_test_num)
   for i in range (iteration):
       gradient = compute_grad(x[random_index[i],:], y[random_index[i]], w-gamma*vt)
       vt = gamma*vt - lr*gradient
       w -= vt
       loss = compute_loss(x, y, w, random_index)
       loss_history.append(loss)
        test_loss_history.append(compute_loss(x_test, y_test, w, random_test_index))
        if loss < threshold :</pre>
            break
   return w, loss_history, test_loss_history
```

```
def RMSProp_train(x, y, x_test, y_test, w, C, lr, gamma, threshold, iteration):
   Gt = 0
    loss_history = []
    test_loss_history = []
   random index = []
    random_test_index = []
    for i in range (iteration):
       random num = random.randint(0, x.shape[0]-1)
        random_test_num = random.randint(0, x_test.shape[0]-1)
        random index.append(random num)
        random_test_index.append(random_test_num)
    for i in range(iteration):
        gradient = compute_grad(x[random_index[i],:], y[random_index[i]], w)
        Gt = gamma*Gt + (1-gamma)*gradient.dot(gradient.T)
        w += lr * gradient / math.sqrt(Gt+1e-8)
        loss = compute_loss(x, y, w, random_index)
       loss_history.append(loss)
        test_loss_history.append(compute_loss(x_test, y_test, w, random_test_index))
        if loss < threshold :</pre>
            break
    return w, loss history, test loss history
def AdaDelta train(x, y, x test, y test, w, C, lr, gamma, threshold, iteration):
   Gt = 0
   variable t = 0
    loss_history = []
   test loss history = []
   random index = []
    random test index = []
    for i in range(iteration):
       random_num = random.randint(0, x.shape[0]-1)
       random_test_num = random.randint(0, x_test.shape[0]-1)
       random_index.append(random_num)
       random_test_index.append(random_test_num)
    for i in range(iteration):
       gradient = compute_grad(x[random_index[i],:], y[random_index[i]], w)
       Gt = gamma*Gt + (1-gamma)*gradient.dot(gradient.T)
       variable_w = - math.sqrt(variable_t + 1e-8) * gradient / math.sqrt(Gt + 1e-8)
       w -= variable w
       variable_t = gamma*variable_t + (1-gamma)*variable_w.dot(variable_w.T)
       loss = compute loss(x, y, w, random index)
       loss_history.append(loss)
       test_loss_history.append(compute_loss(x_test, y_test, w, random_test_index))
       if loss < threshold :
             break
    return w, loss_history, test_loss_history
```

```
def Adam_train(x, y, x_test, y_test, w, C, lr, gamma, threshold, iteration):
     moment = numpy.zeros((1, x.shape[1]))
      B = 0.9
     loss_history = []
      test loss history = []
      random_index = []
      random_test_index = []
      for i in range (iteration):
            random num = random.randint(0, x.shape[0]-1)
            random_test_num = random.randint(0, x_test.shape[0]-1)
            random_index.append(random_num)
            random_test_index.append(random_test_num)
      for i in range(iteration):
            gradient = compute_grad(x[random_index[i],:], y[random_index[i]], w)
           moment = B*moment + (1-B)*gradient
            Gt = gamma*Gt + (1-gamma)*gradient.dot(gradient.T)
            a = lr * math.sqrt(1 - pow(gamma, iteration)) / (1-pow(B, iteration))
            w += a * moment / math.sqrt(Gt + 1e-8)
           loss = compute loss(x, y, w, random index)
            loss_history.append(loss)
            test loss history.append(compute loss(x_test, y_test, w, random_test_index))
      if loss < threshold :
                break
      return w, loss_history, test_loss_history
iteration = 3000
NAG w = numpy.zeros((1, X train.shape[1]))
NAG_w, NAG_loss_history, NAG_test_loss_history = NAG_train(X_train, y_train, X_test, y_test, NAG_w, 0.3, 0.001, 0.9, 0.0
RMS_w = numpy.zeros((1, X_train.shape[1]))
RMS_w, RMS_loss_history, RMS_test_loss_history = RMSProp_train(X_train, y_train, X_test, y_test, RMS_w, 0.3, 0.001, 0.9,
AdaDelta_w = numpy.zeros((1, X_train.shape[1]))
AdaDelta_w, AdaDelta_loss_history, AdaDelta_test_loss_history = AdaDelta_train(X_train, y_train, X_test, y_test, AdaDelt
Adam_w = numpy.zeros((1, X_train.shape[1]))
Adam_w, Adam_loss_history, Adam_test_loss_history = Adam_train(X_train, y_train, X_test, y_test, Adam_w, 0.3, 0.001, 0.9
pyplot.plot(NAG_test_loss_history, label = 'NAG_validation_loss')
pyplot.plot(RMS_test_loss_history, label = 'RMSProp_validation_loss')
pyplot.plot(AdaDelta_test_loss_history, label = 'AdaDelta_validation_loss')
pyplot.plot(Adam_test_loss_history, label = 'Adam_validation_loss')
pyplot.plot(Adam_test_loss_nisto.
pyplot.legend(loc='upper right')
pyplot.ylabel('loss')
pyplot.xlabel('iteration')
pyplot.title('graph')
pyplot.show()
```

#### 逻辑回归:

### 8. 模型参数的初始化方法:

全零初始化。

## 9.选择的 loss 函数及其导数:

loss function:

$$L(\theta) = -\frac{1}{m} \sum_{i=0}^{n} (y_i \log(h_{\theta}(X_i)) + (1 - y_i) \log(1 - \log(h_{\theta}(X_i))))$$

PS:

$$h_{\theta}(X) = \frac{1}{1 + e^{-\theta^T \cdot X}}$$

Gradient: 
$$\frac{\partial L}{\partial \theta} = \frac{1}{n} \sum_{i=0}^{n} X_i (h_{\theta}(X) - y_i)$$

# 10.实验结果和曲线图:

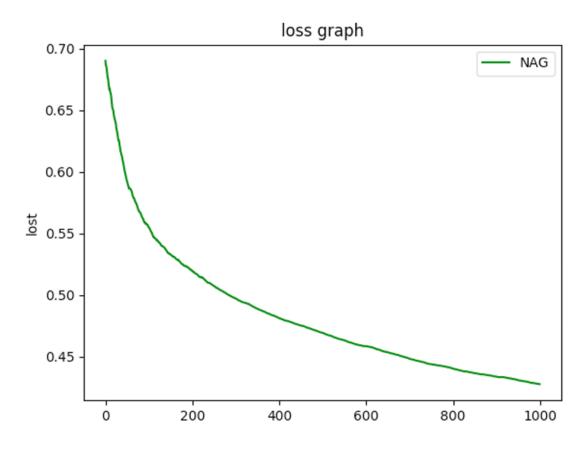
# **1.NAG**:

超参数选择: η=0.005

γ =0.9

epoch = 1000

预测结果(最佳结果):



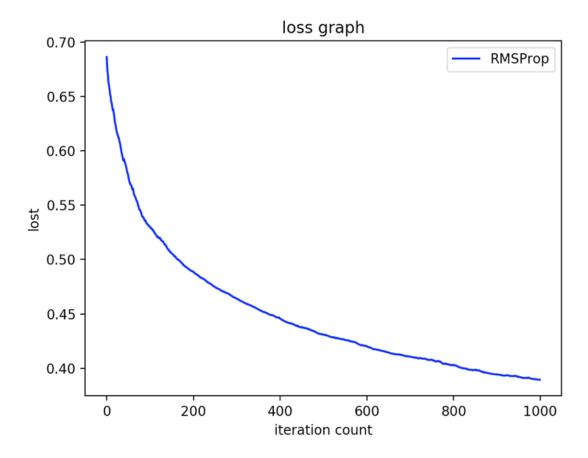
# 2.RMSProp:

$$\gamma = 0.9$$

$$\varepsilon$$
 = 1e-8

epoch = 1000

## 预测结果(最佳结果):



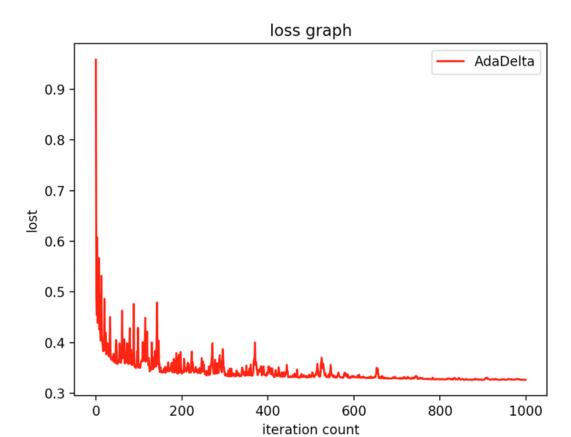
# 3.Adam:

$$\beta_1 = 0.9$$

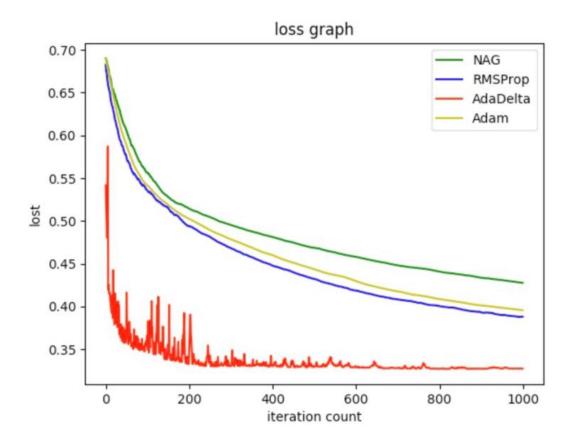
$$\beta_2 = 0.999$$

 $\varepsilon$  = 1e-8 epoch=1000

## 预测结果(最佳结果):



#### loss 曲线图:



## 11.实验结果分析:

- 1.AdaDelta 优点是较快的达到了局部最优解,缺点是震荡明显;
- 2.NAG 缺点是收敛速度和收敛幅度上都较小, 优点则是曲线较为平滑;
- 3.RMSProp 和 Adam 的曲线基本是一致的,收敛速度比 NAG 快,但是比 AdaDelta 慢。

结论: 四种方法都可以较为快速收敛到局部最优解,都比普通梯度下降法更好

### 线性分类:

### 8. 模型参数的初始化方法:

全零初始化

### 9.选择的 loss 函数及其导数:

loss function:

$$L(\theta) = \frac{1}{2n} \sum_{i=0}^{n} (y_i - h_{\theta}(X_i))^2$$

PS:

$$h_{\theta}(X) = \sum_{i=0}^{n} \theta_i X_i$$

gradient:

$$\frac{\partial L}{\partial \theta} = \frac{1}{n} \sum_{i=0}^{n} (y_i - h_{\theta}(X_i)) \cdot X_i$$

# 10.实验结果和曲线图:

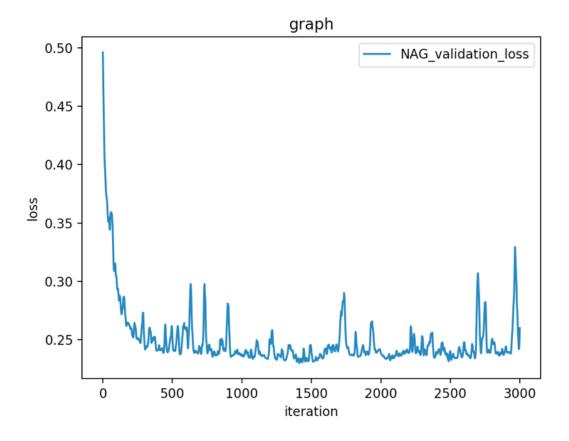
# **1.NAG:**

超参数选择: η=0.001

 $\gamma = 0.9$ 

epoch = 3000

预测结果(最佳结果):

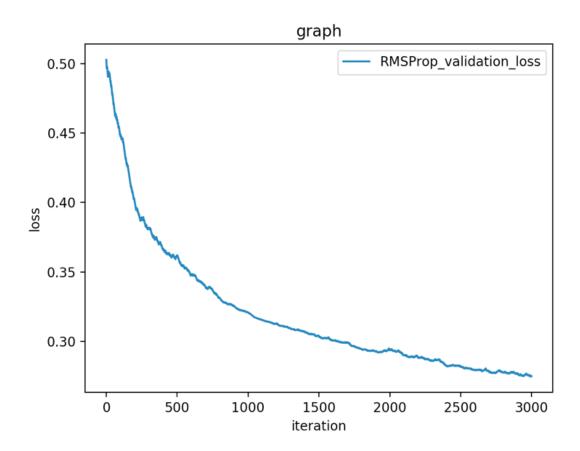


# 2.RMSProp:

$$\gamma = 0.9$$

$$\varepsilon$$
 = 1e-8 epoch = 3000

#### 预测结果(最佳结果):



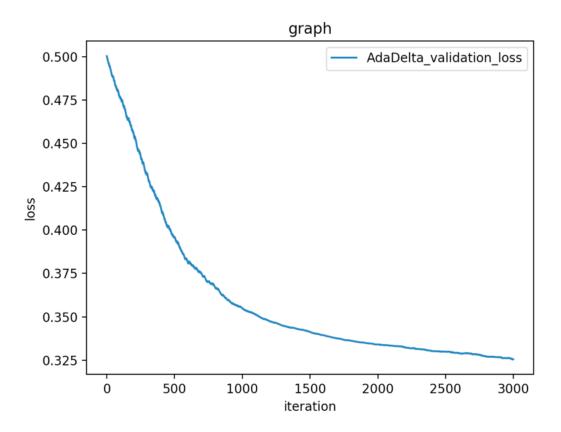
# 3.AdaDelta:

超参数选择:  $\gamma = 0.9$ 

 $\varepsilon$  = 1e-8

epoch=3000

# 预测结果(最佳结果):



# 4.Adam:

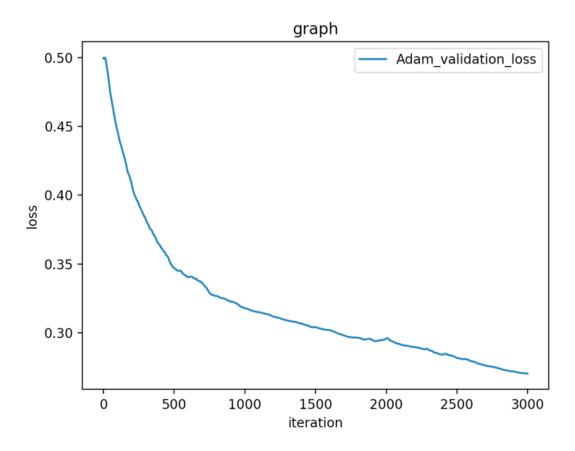
$$\beta_1 = 0.9$$

$$\beta_2 = 0.999$$

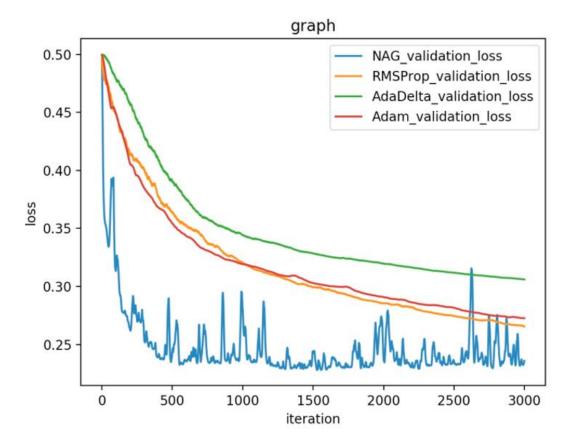
$$\varepsilon$$
 = 1e-8

epoch=3000

## 预测结果(最佳结果):



loss 曲线图:



#### 11.实验结果分析:

- 1.NAG 优点是收敛速度最快,缺点是震荡明显;
- 2.RMSProp 与 Adam 的收敛速度几乎是一样的, 优点是震荡不明显;
- 3.AdaDelta 缺点是收敛较慢,优点是是曲线比较平滑。

结论:相比普通梯度下降算法,这四种算法在不同程度上做了改进,更加优秀。

# 12.对比逻辑回归和线性分类的异同点:

相同点都属于分类问题并且都用于预测。 不同点为逻辑回归只可以处理线性的情况,但是 SVM 都可以。

### 13.实验总结:

本次实验中,我学习到了很多回归、线性和随机梯度等在实践运用的经验,将课程中学习到的知识运用在实际问题上。同时在实验中通过漫长的调试最终还是幸运的完成了实验。

在对模型的训练过程中,我体会到了调整参数的重要性。最初由于超参数学习率等参数设置得不合理,导致 loss 图像与最佳的预期相差很多。好在我在进行数次的不同的调参后,模型往预计方向改变,我也从中学到了很多。