

Redeclaration of *specdatamodels* variables

EXTENDS *Sequences, Naturals, FiniteSets*

Represents every potential user in the system

CONSTANT *USERS*

Constants that should be set to single model values, to allow comparisons

Only equality comparisons will be made.

CONSTANTS

SubscriptionFee,
CancellationFee,
FailedPaymentFee

VARIABLES

Represents the current month

month,

Represents the status of the database. Design requirements require
that all persistent application state be stored here

database,

Required by spec

events

$vars \triangleq \langle events, month, database \rangle$

Provides all the data models required by the spec

INSTANCE *specdatamodels*

$Now \triangleq Len(events)$

$Months \triangleq 0 .. 10$

Strong Typing

$Month \triangleq Nat$

Database Rows

$UserRow \triangleq [$
subscribed : BOOLEAN ,
Forget cancelled
inTrial : BOOLEAN ,
trialStartTime : Nat,
billedForMonth : Nat
 $]$

$BillQueueItem \triangleq [$

$$\begin{aligned}
& user : USERS, \\
& fee : Fees \\
&] \\
TypeOk & \triangleq \\
& \wedge EventsOk \\
& \wedge month \in Month \\
& \wedge database.users \in [USERS \rightarrow UserRow] \\
& \wedge database.billQueue \in Seq(BillQueueItem)
\end{aligned}$$

API endpoints

$$\begin{aligned}
StartSubscription(u) & \triangleq \\
& \wedge database.users[u].subscribed = FALSE \\
& \wedge database' = [database \text{ EXCEPT} \\
& \quad !["users"][u].subscribed = TRUE \\
& \quad] \\
& \text{Observability required by stub} \\
& \wedge events' = Append(events, [type \mapsto "startsubscription", user \mapsto u]) \\
& \wedge UNCHANGED month
\end{aligned}$$

$$\begin{aligned}
CancelSubscription(u) & \triangleq \\
& \wedge database.users[u].subscribed = TRUE \\
& \wedge database' = \\
& \quad [database \text{ EXCEPT} \\
& \quad \quad !["users"][u].subscribed = FALSE, \\
& \quad \quad \text{Charge cancellation fee} \\
& \quad \quad !["billQueue"] = \\
& \quad \quad \quad Append(database.billQueue, \\
& \quad \quad \quad \quad [user \mapsto u, fee \mapsto CancellationFee]) \\
& \quad] \\
& \text{Observability required by stub} \\
& \wedge events' = Append(events, [type \mapsto "cancelsubscription", user \mapsto u]) \\
& \wedge UNCHANGED \langle month \rangle
\end{aligned}$$

$$\begin{aligned}
StartTrial(u) & \triangleq \\
& \wedge database.users[u].inTrial = FALSE \\
& \wedge database.users[u].subscribed = FALSE \\
& \wedge database' = [database \text{ EXCEPT} \\
& \quad !["users"][u].inTrial = TRUE] \\
& \text{Observability required by stub} \\
& \wedge events' = Append(events, [type \mapsto "starttrial", user \mapsto u])
\end{aligned}$$

$\wedge \text{UNCHANGED } \langle month \rangle$

$\text{CancelTrial}(u) \triangleq$
 $\wedge \text{database.users}[u].inTrial = \text{TRUE}$
 $\wedge \text{database}' = [\text{database EXCEPT}$
 $\quad ![\text{"users"}][u].inTrial = \text{FALSE}$
 $\quad]$

Observability required by stub
 $\wedge \text{events}' = \text{Append}(\text{events}, [\text{type} \mapsto \text{"canceltrial"}, \text{user} \mapsto u])$
 $\wedge \text{UNCHANGED } \langle month \rangle$

$\text{WatchVideo}(u) \triangleq$
 $\wedge \vee \text{database.users}[u].subscribed = \text{TRUE}$
 $\quad \vee \text{database.users}[u].inTrial = \text{TRUE}$

Observability required by stub
 $\wedge \text{events}' = \text{Append}(\text{events}, [\text{type} \mapsto \text{"watchvideo"}, \text{user} \mapsto u])$
 $\wedge \text{UNCHANGED } \langle month, database \rangle$

Stub method, do not changed
 $\text{Bill}(u, \text{fee}) \triangleq$
 $\wedge \text{events}' = \text{Append}(\text{events}, [\text{type} \mapsto \text{"bill"},$
 $\quad \text{user} \mapsto u,$
 $\quad \text{fee} \mapsto \text{fee}])$

$\text{PaymentFailed}(u, \text{fee}) \triangleq$
 $\wedge \text{database}' = [\text{database EXCEPT}$
 $\quad ![\text{"users"}][u].subscribed = \text{FALSE}$
 $\quad]$

Observability required by stub
 $\wedge \text{events}' = \text{Append}(\text{events}, [\text{type} \mapsto \text{"paymentfailed"},$
 $\quad \text{user} \mapsto u,$
 $\quad \text{fee} \mapsto \text{fee}])$
 $\wedge \text{UNCHANGED } \langle month \rangle$

Recurring Operations

This the the state that calls the Payment Failed API

$\text{ExistingBillFailed} \triangleq$
 $\vee \exists i \in 1 \dots \text{Len}(\text{events}) :$
 $\quad \text{Only a past bill can fail}$
 $\quad \wedge \text{events}[i] \in \text{BillEvent}$
 $\quad \wedge \text{PaymentFailed}(\text{events}[i].\text{user}, \text{events}[i].\text{fee})$

$$\begin{aligned}
& \text{BillSubscribedUsers} \triangleq \\
& \exists u \in \text{USERS} : \\
& \quad \text{That is subscribed} \\
& \quad \wedge \vee \text{database.users}[u].\text{subscribed} = \text{TRUE} \\
& \quad \quad \text{Subscribed from a trial so bill} \\
& \quad \quad \vee \wedge \text{database.users}[u].\text{inTrial} = \text{TRUE} \\
& \quad \quad \wedge \text{database.users}[u].\text{trialStartTime} < \text{month} \\
& \quad \text{Ensure users are not double billed} \\
& \quad \wedge \text{database.users}[u].\text{billedForMonth} < \text{month} \\
& \quad \wedge \text{database}' = \\
& \quad \quad [\text{database EXCEPT} \\
& \quad \quad \quad \text{Add subscription fee} \\
& \quad \quad \quad ![\text{"billQueue"}] = \\
& \quad \quad \quad \quad \text{Append}(\text{database.billQueue}, \\
& \quad \quad \quad \quad \quad [user \mapsto u, fee \mapsto \text{SubscriptionFee}]), \\
& \quad \quad \quad ![\text{"users"}][u].\text{billedForMonth} = \text{month} \\
& \quad \quad] \\
& \quad]
\end{aligned}$$

$$\begin{aligned}
& \text{ProcessBills} \triangleq \\
& \quad \wedge \text{Len}(\text{database.billQueue}) > 0 \\
& \quad \wedge \text{LET } \text{bill} \triangleq \text{Head}(\text{database.billQueue}) \text{ IN} \\
& \quad \quad \text{Bills user} \\
& \quad \quad \wedge \text{Bill}(\text{bill.user}, \text{bill.fee}) \\
& \quad \quad \wedge \text{database}' = \\
& \quad \quad \quad [\text{database EXCEPT} \\
& \quad \quad \quad \quad \text{Removes head of queue} \\
& \quad \quad \quad \quad ![\text{"billQueue"}] = \\
& \quad \quad \quad \quad \quad \text{SubSeq}(\text{database.billQueue}, \\
& \quad \quad \quad \quad \quad \quad 2, \text{Len}(\text{database.billQueue})) \\
& \quad \quad \quad] \\
& \quad]
\end{aligned}$$

Stub method that prevents the month from passing until all operations are complete. Represent worker methods, etc

$$\begin{aligned}
& \text{HandledMonth} \triangleq \\
& \quad \wedge \neg \text{ENABLED } \text{BillSubscribedUsers} \\
& \quad \wedge \neg \text{ENABLED } \text{ProcessBills}
\end{aligned}$$

$$\begin{aligned}
& \text{DO NOT MODIFY} \\
& \text{MonthPasses} \triangleq \\
& \quad \wedge \text{HandledMonth} \\
& \quad \wedge \text{month}' = \text{month} + 1 \\
& \quad \wedge \text{events}' = \text{Append}(\text{events}, [\text{type} \mapsto \text{"monthpass"}]) \\
& \quad \wedge \text{UNCHANGED } \langle \text{database} \rangle
\end{aligned}$$

Specification

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Init  $\triangleq$ 
   $\wedge events = \langle \rangle$  Events must be intialized empty, per stub
   $\wedge month = 0$ 
   $\wedge database = [$ 
    Users start with everything unset
     $users \mapsto$ 
     $[u \in USERS \mapsto$ 
       $[$ 
         $subscribed \mapsto \text{FALSE},$ 
         $inTrial \mapsto \text{FALSE},$ 
         $trialStartTime \mapsto 0,$ 
         $billedForMonth \mapsto 0$ 
       $]$ 
     $],$ 
    Bill queue starts empty
     $billQueue \mapsto \langle \rangle$ 
   $]$ 

```

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Next  $\triangleq$  \* Required by stub
   $\vee MonthPasses$ 
  \* State modified below
   $\vee \exists u \in USERS:$ 
     $\vee StartSubscription(u)$ 
     $\vee CancelSubscription(u)$ 
     $\vee StartTrial(u)$ 
     $\vee CancelTrial(u)$ 
     $\vee WatchVideo(u)$ 
  \* Add more user based states
  \* Payment failing behavior is part of spec not implementation
   $\vee ExistingBillFailed$ 
   $\vee BillSubscribedUsers$ 

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\* Modification History
\* Last modified Sun Jun 19 17:39:21 MST 2022 by elliotswart
\* Created Fri Jun 17 00:43:20 MST 2022 by elliotswart

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