

Cache incorporates the data  
 $CacheCompleteFill(k) \triangleq$   
 $\wedge cacheFillStates[k].state = \text{"respondedto"}$   
 Either the cache is empty for that key  
 $\wedge \vee cache[k] \in CacheMiss$   
 or we are filling a newer version  
 $\vee \wedge cache[k] \notin CacheMiss$   
 $\wedge cache[k].version < cacheFillStates[k].version$   
 $\wedge cacheFillStates' = [cacheFillStates \text{ EXCEPT } \text{Reset to 0}$   
 $\quad ! [k].state = \text{"inactive"},$   
 $\quad ! [k].version = 0$   
 $\quad ]$   
 $\wedge cache' = [cache \text{ EXCEPT}$   
 $\quad ! [k] = [$   
 $\quad \quad type \mapsto \text{"hit"},$   
 $\quad \quad version \mapsto cacheFillStates[k].version$   
 $\quad \quad ]$   
 $\quad ]$   
 $\wedge \text{UNCHANGED } \langle database, invalidationQueue \rangle$

$CacheIgnoreFill(k) \triangleq$   
 $\wedge cacheFillStates[k].state = \text{"respondedto"}$   
 If we have a newer version in cache, ignore fill  
 $\wedge \wedge cache[k] \in CacheHit$   
 $\wedge cache[k].version \geq cacheFillStates[k].version$   
 $\wedge cacheFillStates' = [cacheFillStates \text{ EXCEPT } \text{Reset to 0}$   
 $\quad ! [k].state = \text{"inactive"},$   
 $\quad ! [k].version = 0$   
 $\quad ]$   
 Don't update cache  
 $\wedge \text{UNCHANGED } \langle cache, database, invalidationQueue \rangle$

$CacheHandleInvalidationMessage \triangleq$   
 $\wedge \exists message \in invalidationQueue : \text{Dequeue invalidation queue in any order}$   
 Key must be in cache  
 $\wedge \wedge cache[message.key] \in CacheHit$   
 Message needs to be newer than the cache  
 $\wedge cache[message.key].version < message.version$   
 Update item in cache  
 $\wedge cache' = [cache \text{ EXCEPT}$   
 $\quad ! [message.key] = [$   
 $\quad \quad type \mapsto \text{"hit"},$   
 $\quad \quad \text{Update to version in invalidation message}$   
 $\quad \quad ]$   
 $\quad ]$

$$\begin{aligned}
& \text{version} \mapsto \text{message.version} \\
& \quad ] \\
& \quad \text{Remove message from queue because handled} \\
& \quad \wedge \text{invalidationQueue}' = \text{invalidationQueue} \setminus \{\text{message}\} \\
& \quad \wedge \text{UNCHANGED } \langle \text{cacheFillStates}, \text{database} \rangle \\
\text{CacheIgnoreInvalidationMessage} & \triangleq \\
& \quad \wedge \exists \text{message} \in \text{invalidationQueue} : \text{Dequeue invalidation queue in any order} \\
& \quad \quad \text{Ignore invalidation messages for messages not in cache} \\
& \quad \wedge \vee \text{cache}[\text{message.key}] \in \text{CacheMiss} \\
& \quad \quad \text{Or when the cache already has the same or larger version} \\
& \quad \quad \vee \wedge \text{cache}[\text{message.key}] \notin \text{CacheMiss} \\
& \quad \quad \quad \wedge \text{cache}[\text{message.key}].\text{version} \geq \text{message.version} \\
& \quad \quad \text{Remove message from queue to ignore} \\
& \quad \quad \wedge \text{invalidationQueue}' = \text{invalidationQueue} \setminus \{\text{message}\} \\
& \quad \quad \text{Don't update cache} \\
& \quad \wedge \text{UNCHANGED } \langle \text{cacheFillStates}, \text{database}, \text{cache} \rangle
\end{aligned}$$


---

\ \* Modification History  
\ \* Last modified *Wed Jun 15 13:58:25 MST 2022* by *elliotswart*  
\ \* Created *Wed Jun 15 13:58:13 MST 2022* by *elliotswart*