

Module No1.

Import Unicode.UTF8. (\*We first give the axioms of Principia for the propositional calculus in \*1.\*)

Axiom MP1\_1 :  $\forall P Q : \text{Prop},$   
 $(P \rightarrow Q) \rightarrow P \rightarrow Q.$  (\*Modus ponens\*)

(\*\*1.11 omitted: it is MP for propositions containing variables. Likewise, omitted the well-formedness rules 1.7, 1.71, 1.72\*)

Axiom Taut1\_2 :  $\forall P : \text{Prop},$   
 $P \vee P \rightarrow P.$  (\*Tautology\*)

Axiom Add1\_3 :  $\forall P Q : \text{Prop},$   
 $Q \rightarrow P \vee Q.$  (\*Addition\*)

Axiom Perm1\_4 :  $\forall P Q : \text{Prop},$   
 $P \vee Q \rightarrow Q \vee P.$  (\*Permutation\*)

Axiom Assoc1\_5 :  $\forall P Q R : \text{Prop},$   
 $P \vee (Q \vee R) \rightarrow Q \vee (P \vee R).$

Axiom Sum1\_6 :  $\forall P Q R : \text{Prop},$   
 $(Q \rightarrow R) \rightarrow (P \vee Q \rightarrow P \vee R).$  (\*These are all the propositional axioms of Principia Mathematica.\*)

Axiom Impl1\_01 :  $\forall P Q : \text{Prop},$   
 $(P \rightarrow Q) = (\sim P \vee Q).$  (\*This is a definition in Principia: there  $\rightarrow$  is a defined sign and  $\vee, \sim$  are primitive ones. So we will use this axiom to switch between disjunction and implication.\*)

End No1.