Section Handout #2 Solutions

If you have any questions about the solutions to the problems in this handout, feel free to reach out to your section leader, Anton, or Chris for more information.

1. Twice

```
// solution 1: with additional structures
Set<int> twice(Vector<int> &v) {
  Map<int, int> counts;
  for (int n : v) {
    counts[n]++;
  }

  Set<int> twice;
  for (int k : counts) {
    if (counts[k] == 2) {
      twice += k;
    }
  }
  return twice;
}
```

```
// solution 2: without auxiliary structures
Set<int> twice(Vector<int> &v) {
  Set<int> one, two, more;
  for (int n : v) {
    if (one.contains(n)) {
      one.remove(n);
      two.add(n);
    } else if (two.contains(n)) {
      two.remove(n);
      more.add(n);
    } else if (!more.contains(n)) {
      one.add(n);
    }
  }
  return two;
}
```

2. Friend List

```
Map<string, Vector<string>> friendList(string &filename) {
  ifstream infile(filename.c_str());
  Map<string, Vector<string>> friends;
  string s1, s2;
  while(infile >> s1 >> s2) {
    friends[s1] += s2;
    friends[s2] += s1;
  }
  return friends;
}
```

3. Tracing a Mystery

Call	Output
mystery1(4, 1)	4
mystery1(8, 2)	16, 8, 16
mystery1(3, 4)	12, 9, 6, 3, 6, 9, 12

4. Sum of Squares

```
int sumOfSquares(int n) {
  if (n == 0) return 0;
  return n * n + sumOfSquares(n – 1);
}
```

5. Reverse

```
string reverse(string &s) {
  if (s == "") return "";
  return reverse(s.substr(1)) + s[0];
}
```

6. Star String

There are multiple ways to handle invalid input. In our solution below, we chose to throw an exception. However, you can also have a well-defined value that you return in the event of invalid input. It's important that whatever you choose, you document it well.

```
string starString(int n) {
  if (n < 0) {
    throw "Invalid input.";
  } else if (n == 0) {
    return "*";
  } else {
    string stars = starString(n - 1);
    return stars + stars;
  }
}
```

Note that another possible solution is to return the result `starString(n - 1) + starString(n - 1)`. Why might you not want to use this solution?

7. Stutter Stack

```
void stutterStack(Stack<int> &s) {
  if (!s.isEmpty()) {
    int next = s.pop();
    stutterStack(s);
    s.push(next);
    s.push(next);
  }
}
```

8. Subsequence

```
bool isSubsequence(string &big, string &small) {
  if (small == "") {
    return true;
  } else if (big == "") {
    return false;
  } else {
    if (big[0] == small[0]) {
      return isSubsequence(big.substr(1), small.substr(1));
    } else {
      return isSubsequence(big.substr(1), small);
    }
  }
}
```

9. Tower of Hanoi

Solving the Tower of Hanoi problem with n disks is composed of three steps:

1. Move all the disks but the largest (or $n - 1$ disks) from the source peg to a spare peg in order to expose the largest disk.
2. Move the largest disk to the destination peg
3. Move all the disks but the largest (or $n - 1$ disks) from the spare peg to the destination peg

You might notice that the first and third steps can be expressed as their own Tower of Hanoi problem, which means we can implement them using recursive calls!

```cpp
void hanoi(int disks, int source, int dest) {
  if (disks > 0) {
    int thirdPeg = 6 - source - dest;  // the three peg indicies sum to 6 (1 + 2 + 3) which
                                       // means you can always find the third peg by
                                       // subtracting the source and dest from 6

    hanoi(disks - 1, source, thirdPeg);
    cout << "move disk " << disks << " from peg " << source
                                  << " to peg " << dest << endl;
    hanoi(disks - 1, thirdPeg, dest);
  }
}
```

10. Edit Distance

```cpp
int editDistance(string &s1, string &s2) {
  if (s1 == "") {
    return s2.length();
  } else if (s2 == "") {
    return s1.length();
  }

  // try three possibilities for the "zeroth" character:
  int add = 1 + editDistance(s1, s2.substr(1));
  int del = 1 + editDistance(s1.substr(1), s2);
  int sub = editDistance(s1.substr(1), s2.substr(1));
  if (s1[0] != s2[0]) {
    sub += 1;
  }
  return min(add, min(del, sub));
}
```