

# Some basic notions in AGI & my theory

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# Talk summary

- 1 What is inductive bias? “No free lunch” theorem
- 2 What gives neural networks their power?
- 3 Turing machines and universal logic
- 4 Structure of classical AI systems

# Section 1

What is inductive bias? “No free lunch” theorem

# The goal of machine learning

- The goal of machine learning is to search in a **space** of learning machines, those machines that satisfy certain criteria
- For example, among the neural networks of a certain size and shape, find the weights that satisfy an **objective function**

# AI Winter

- Generally speaking, bottleneck problem of AI = **search space too large**, thus learning too slow
- Historically, “AI Winter” occurred because **logic-based** AI learning suffers from combinatorial explosion, and we lacked workable **heuristics** to tackle it

# Inductive bias

- Every learning algorithm has its **inductive bias**
- That is to say, some regions of the search space would **not** be searched
- Bias makes learning faster
- But if bias is too strong, the space containing the solution would be cut off  
“Throw the baby out with the water”

# “No free lunch” theorem

- When search space has no *a priori* structure, any inductive bias would be **good at some problems while bad at others** — “no free lunch”
- For example, vision has the structure of 3D Euclidean geometry, thus the human visual cortex may have inductive bias for this invariance
- Or, human cognition has “logical” structure, using this inductive bias may accelerate machine learning of human intelligence

# Kolmogorov complexity

- is **incomputable**, but **approximable**
- The **semantic distance metric** between logic propositions is related to it, where one logic deduction step corresponds to 1 unit of semantic distance
- Find a set of logic rules, that **explains** the world, and not deduce false facts, and # of rules cannot be too large — these requirements *implicitly* approximate Kolmogorov complexity



## Section 2

What gives neural networks  
their power?

# Structure of a neural network

- 1 neuron is a **dot product** followed by a **non-linearity**:

$$\sigma \langle \mathbf{x}, \mathbf{w} \rangle \quad (1)$$

- The non-linearity can take various forms,  
eg:

$$\sigma(\xi) = \frac{1}{1 + e^{-\xi}} \quad (2)$$

# Structure of a neural network

- 1 **layer** of neurons is a matrix multiplication:

$$\mathcal{O}(W \cdot x) \quad (3)$$

- A neural **network** is the function **composition**  $(f \circ f)$  of many layers:

$$[\mathcal{O}W]^L x \quad (4)$$

# Properties of neural networks

- An NN is a function with many **parameters**
- It is a **universal function approximator** [Cybenko 1989]
- Its proof can be traced to Weierstrauss's approximation theorem (1885): any continuous function can be uniformly approximated by polynomials
- But the proof is **independent of depth**

# Power of NNs comes from depth

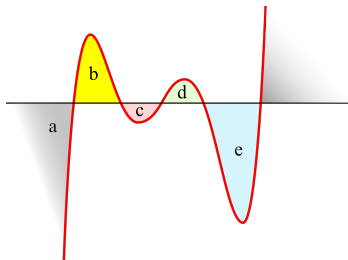
- Suppose  $\odot Wx$  is a *cubic* polynomial
- Adding each layer is equivalent to:

$$(\text{polynomial} \circ \text{polynomial}) \quad (5)$$

- Thus, the resulting polynomial has total degree  $= 3^L$
- In other words, total degree grows **exponentially**

# Power of NNs comes from depth

- **Fundamental theorem of algebra:**  
polynomial **degree** = zero-crossings of  
curve with  $x = 0$



(6)

- In higher dimensions: **how many pieces**  
does a surface carve up the space

# Power of NNs comes from depth

- Same idea as **VC-dimension** [Vapnik–Chervonenkis 1971]
- VC-dim = max # pieces the ambient space is *shattered* by a family of functions
- My conjecture: VC-dim of multi-layer NN grows exponentially as # layers
- Contradicts with current bound =  $O(W \log W)$  where  $W$  = total # parameters; I will investigate further

# Power of NNs comes from depth

- The **exponential growth** of VC-dim means that NNs can represent highly complex **families** of functions
- and with a relatively small  $\#$  of parameters, which can be implemented on a computer



# Revelation from convolutional NNs

- Yann LeCun in 1989 invented **ConvNets**, which revolutionized machine vision, and got him a Turing Award



# Revelation from convolutional NNs

- CNN replaces the conventional **dot product** with the **covolutional product**:

$$\boxed{\text{dot product}} \quad \mathcal{O}(\langle \mathbf{x}, \mathbf{w} \rangle) \rightsquigarrow \mathcal{O}(f * g) \quad \boxed{\text{convolution}} \quad (7)$$

- The convolution has **translation invariance**, which is suitable for vision:

$$T_x(f) * g = T_x(f * g) \quad (8)$$

- This is an **inductive bias**, which makes learning faster

# Revelation from convolutional NNs

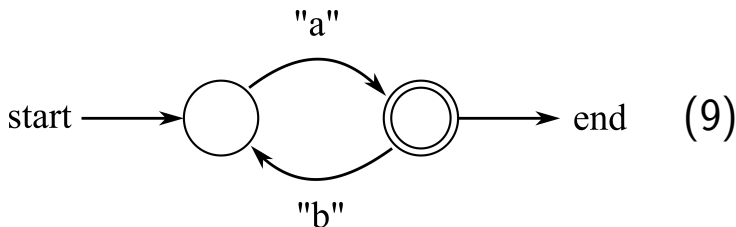
- Actually **vision** obeys **affine** invariance, *ie*: translations, rotations, dilations, ...
- It seems that merely translational invariance yields enough **acceleration** such that CNNs surpassed human vision performance in 2012
- Thus we see that **inductive bias** is still useful in deep learning

## Section 3

# Turing machines and universal logic

# Finite state machines

- Finite state machines are usually defined by tuples (skipped here), eg:



- This automata **accepts** strings like "a", "aba", "ababa..."

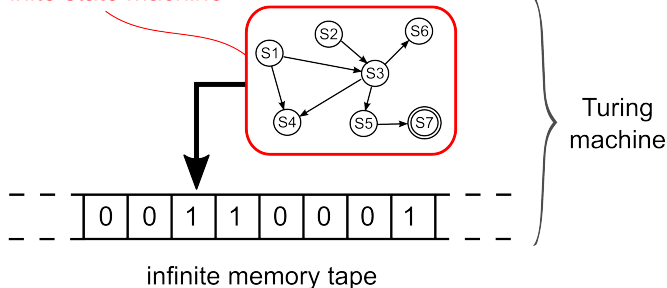
# Finite state machines

- FSMs can accept strings of the form  $a^m b^n$ , where  $m$  and  $n$  are different
- But they can't recognize  $a^k b^k$  as they have no way to “remember” how many times  $k$  is
- The **languages** accepted by FSMs are called **regular languages**
- Formulated in 1950s by Noam Chomsky (computer scientist + linguist, now a leftist critic of US politics)

# Turing machines

Turing machine = finite state machine + infinite **memory tape** (each state can read/write 1 symbol)

Finite state machine



(10)

# Turing machines

- Finite state machine + infinite tape = can compute all computable functions, *ie*,  
**Church-Turing hypothesis**
- Turing machines are **equivalent** to:  
 $\lambda$ -calculus, combinatory logic, cellular automata, game of life, recurrent neural networks, ... *etc*

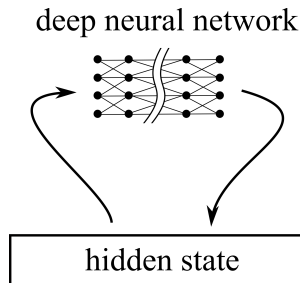


# Alan Turing (1912-1954)

- Turing was a man very much ahead of his time
- He considered neurons as learning machines
- Also considered evolutionary algorithms
- In 1940s there were no computers yet — he invented them!
- He formulated the form of **all computable functions**, thus **confining** the problem of AI within a framework

# Recurrent neural networks

Structure of RNNs can be seen as similar to (10):



(11)

Key is that the **hidden state** can store **intermediate results** of computations, enabling RNNs to be Turing-universal

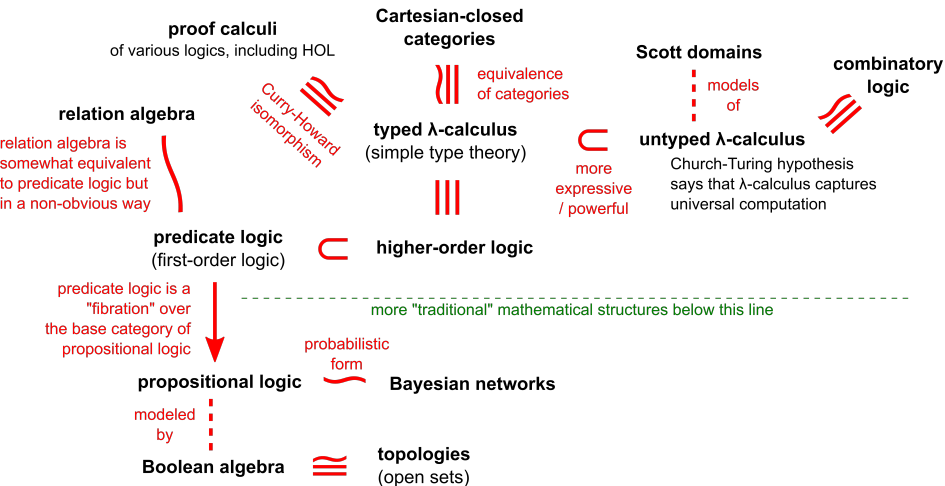
# Section 4

## Structure of classical AI systems

# John McCarthy (1927-2011)

- “Father of AI”
- Held the first AI conference in 1956 in Dartmouth
- Pioneered the use of **mathematical logic** as **knowledge representation** in AI
- In later years he studied **term rewriting systems**, a more **generalized** form of logic

# The world of logical structures



# Propositional vs predicate logic

- The important distinction is between **propositional** and first-order **predicate** logic
- In propositional logic, **propositions don't have internal structure**

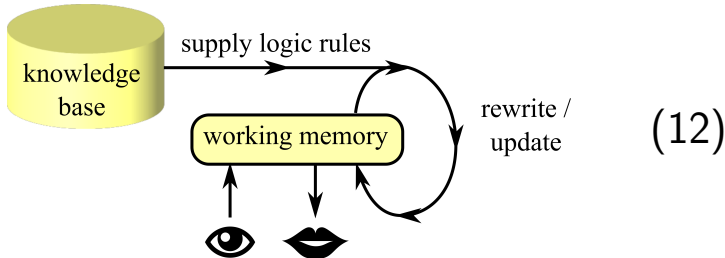
$P_1 = \text{"It rained yesterday"}$

$P_2 = \text{"It's raining today"}$

- Predicate logic:  $P_3 = \text{rain(New York, today)}$
- Predicates bring about the complexity of **substitutions**

# Architecture of logic-based AI systems

This cycle is as important as the *Carnot cycle* in the age of steam engines:



# What is a logic rule?

- Example: loving someone and not loved back implies heartbreak:

$$\heartsuit(x, y) \wedge \neg \heartsuit(y, x) \Rightarrow \text{☹}(x) \quad (13)$$

- This is a rule. Variables  $x, y$  need to be **substituted** with appropriate objects, eg  $\{x \setminus \text{John}, y \setminus \text{Mary}\}$
- Algorithm for finding substitutions is called **matching** or **unify**



# SOAR architecture

- is a famous **cognitive architecture**
- SOAR searches for logic rules that match with working memory, similar to what is depicted in (12)
- SOAR uses the **Rete** algorithm to search for applicable rules efficiently, this is an important algorithm in classical AI (*rete* meaning “web-like” in Latin)

# My theory

- In my theory, the rules and their matching mechanism are **absorbed** into an NN
- The NN is a weapon whose strength is in approximating very complex mappings; It is the most powerful machine-learning technology we have nowadays
- In my design I **relax** the structure of logic to get just the right amount of inductive bias
- In this design the central component is the **symmetric NN**

# Commutativity of logic $\wedge$

- The commutativity of  $\wedge$  is perhaps the most important law of logic, eg:

$$\text{hungry} \wedge \text{penniless} \Leftrightarrow \text{penniless} \wedge \text{hungry} \quad (14)$$

- Could be understood as: When deducing a conclusion from some premises, the propositions in the premise could be presented in **any order**, even containing irrelevant propositions
- The commutative law abstracts the structure of propositions, similar to the importance of commutative groups (also called Abelian group, in memory of Abel) in abstract algebra

# Symmetric neural networks

- Convolutional NNs possess translational invariance
- Similarly, **symmetric** NNs possess **permutation invariance**
- This can be realized via **weight-sharing**, as similar in ConvNets
- SymNet : logic  $\approx$  ConvNet : vision

# Will China build its own AGI?

- The failure of Japan in 1980s to develop 5th-Generation computers can be a lesson
- As the earth has limited resources, technological progress often is the result of competition among national entities
- In the US there are people against China; In China there are also people dragging our feet, supporting outsiders. Yet I have also recieved help from American friends
- Therefore, I tend to be more supportive of globalized AGI projects

Thanks for watching 😊