On AGI architecture

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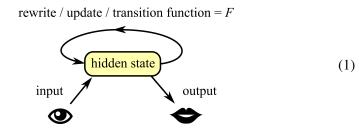
Hello friends 😜

I have made some intermediate progress recently, which I share below.

I am also looking for collaborators.

The simplest AGI architecture

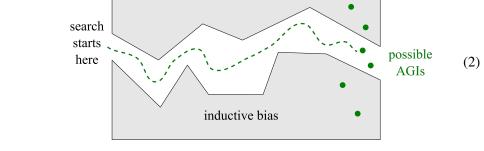
► The simplest AGI architecture consists of a single recurrent loop:



- It operates under reinforcement learning, maximizing rewards by the Bellman optimality condition
- ightharpoonup The transition function F can be implemented by a neural network
- According to No Free Lunch theorem, problem with this architecture is lack of inductive bias, learning is too slow

Some musings on No Free Lunch (NFL)

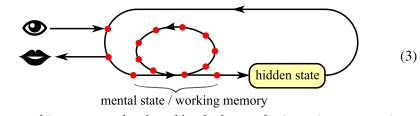
- According to NFL, there is no such things as "good" or "bad" inductive bias
- ► As long as it accelerates learning, and still accommodates AGI, it is good bias:



- ► For example, the neural network *F* can be made sparse while preserving deepness
- Yet, I proposed earlier to use logic as bias. Is that redundant? 😖

"Double loop" architecture

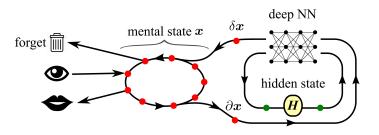
Assume working memory consists of disparate propositions (•), residing in an inner loop. As this loop is iterated, the propositions are condensed into the hidden state. Hence the "double-loop" architecture



- This same architecture may be shared by the human brain, as its structure is simple and thus could have been evolved
- ➤ As far as I know, BERT also contains an implicit recurrence, where words in a sentence are condensed into a hidden state, from which target words are generated one by one
- ► So it seems that if we modify BERT to be a "double loop", we can get an AGI:

words / concepts
$$\stackrel{\text{loop 1}}{\longrightarrow}$$
 sentences / propositions $\stackrel{\text{loop 2}}{\longrightarrow}$ mental state (4)

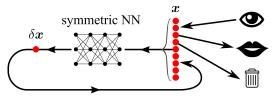
▶ Diagram (3) is a bit inaccurate, here is a more detailed diagram:



(5)

(6)

In contrast, one can use a symmetric NN to make the architecture even simpler:



▶ But it's not easy to decide whether (5) or (6) learns faster 🤢

Connection between reinforcement learning & quantum mechanics

► The optimal condition for reinforcement learning is the Bellman equation:

Bellman
$$S_t(x) = \max_{u} \{ L(x, u) + \gamma S_{t+1}(x) \}$$
 (7)

► The differential version of Bellman equation is the Hamilton-Jacobi equation in classical analytic mechanics (This has been recognized in 1970's by Kalman, Pontryagin and others):

Hamilton-Jacobi
$$\frac{\partial S(x,t)}{\partial t} = -H$$
 (8)

► The Hamiltionian *H* arises when trying to maximize the Lagrangian *L* using Lagrangian multipliers. Such multipliers have the interpretation of momentum.

$$L = KE - PE$$
 , $H = KE + PE$ (9)

where KE = kenetic energy, PE = potential energy.

▶ Up to now, we changed a discrete equation to a continuos differential equation, but that has not yielded any advantage

▶ We have always been told in textbooks that such a process of quantization can only be achieved heuristically, but some friend informed me that [Field 2010] has derived this result.

 Recently I independently discovered an exact way to go from the classical Hamilton-Jacobi equation to the Schrödinger equation via the substitution

 $\Psi = e^{-i\hbar S}$.

Hamilton-Jacobi $\frac{\partial S}{\partial t} = -H \implies i\hbar \frac{\partial \Psi}{\partial t} = H\Psi$ Schrödinger

(10)

heat equation via the introduction of imaginary time:

$$\frac{\partial \Psi}{\partial t} + i\Delta \Psi = 0 \iff \frac{\partial u}{\partial t} + \Delta u = 0 \quad \text{heat eqn.} \quad (11)$$

Schrödinger operator to act on graphs

Impressive as it may sound, this may be of low practical value

?

Topos theory

A topos is a category in which one can "do logic". The idea originated in 1950's when Lawvere tried to re-formulate the foundation of mathematics / set theory in the new language of category theory.

In a topos, 3 operations are allowed between objects:

- Cartesian product $A \times B$ (corresponding to $A \wedge B$ in propositional logic)
- exponentiation $A \to B = B^A$ (corresponding to $A \Rightarrow B$ in propositional logic)
- ▶ subobject classifier $A \hookrightarrow B$ (corresponding to the subset notion $A \subseteq B$)

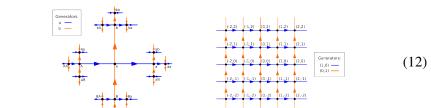
The significance of topos theory is that it distills which mathematical structures are able to carry on logic operations, e.g. relation graphs, algebras, etc.

In my theory, the neural network F implements $U \xrightarrow{F} V$ which is the exponentiation V^U , where U, V are vector spaces. This requires, at least, to embed the structure of $A \times B$ into vector space. However $A \times B = B \times A$ is commutative, which led me to consider Abelian group theory....

Permutation invariance

free group is grid-like:

- Recently a nice idea has been proposed to embed Word2Vec into Poincaré disc / hyperbolic space [Nickel and Kiela 2017]
- Can we similarly embed logic structures (as vectors) into hyperbolic space? Cayley graph of the free group F_2 is a tree, but Cayley graph of the Abelian



Generally, the free group F_n 's Cayley graph can be embedded into the (planar) hyperbolic disc, but the Abelianization of $F_n = F_n^{Ab} \cong \mathbb{Z}^n = \mathbb{Z} \times ... \mathbb{Z}$ is a *n*-dimensional grid, which seems impossible to embed on a plane.

Even considering representation theory, all irreducible representations of Abelian groups are 1-dimensional. The representation of F_n^{Ab} is precisely the direct sum of *n* copies of dim-1 representations. Useless!

- \triangleright Seems that \mathbb{Z}^n cannot be embedded into lower dimensions, unless we use some kind of fractal structure. However, fractals are exactly the realm that is out-of-reach of the universal approximating power of neural networks! Another strategy is to create symmetric neural networks whose output is
- invariant when the input is permuted. This could be achieved by "weight-sharing". For this to work, the activation function must be polynomials.
- ► A drawback of this approach is when # layers grow, # constraints also grow
- exponentially, making it hard to build deep (many-layer) networks An advantage is that the resulting NN is very sparse in terms of # weights.
- This is a form of inductive bias. As of this writing, I am yet exploring another approach that is inspired by
- Google's BERT. More on this later.

Field, JH (2010). "Derivation of the Schrödinger equation from the Hamilton-Jacobi equation in Feynman's path integral formulation of quantum mechanics". In: European Journal of Physics.

Nickel, Maximillian and Douwe Kiela (2017). "Poincaré embeddings for learning hierarchical

representations". In: Advances in neural information processing systems, pp. 6338–6347.

Thanks for watching 63