AGI standard model — trying to establish a consensus

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0 Introduction

The "standard model" is a way of thinking, that may help us better understand the general theory of AGI systems.

The essence of the standard model is just to identify a **Working Memory** or "state" of the AGI system.

One benefit of our theory is that it relates Transformers / BERT / GPT to AGI systems. These language models are phenomenally intelligent, yet many people criticize them as not "truly" intelligent. The standard model suggests that they are indeed linked to AGI. There are other benefits.

1 Reinforcement learning

This is the simplest form of a **dynamical system**:

transition function F $\boxed{\text{state } x} = \text{"working memory"} \tag{1}$

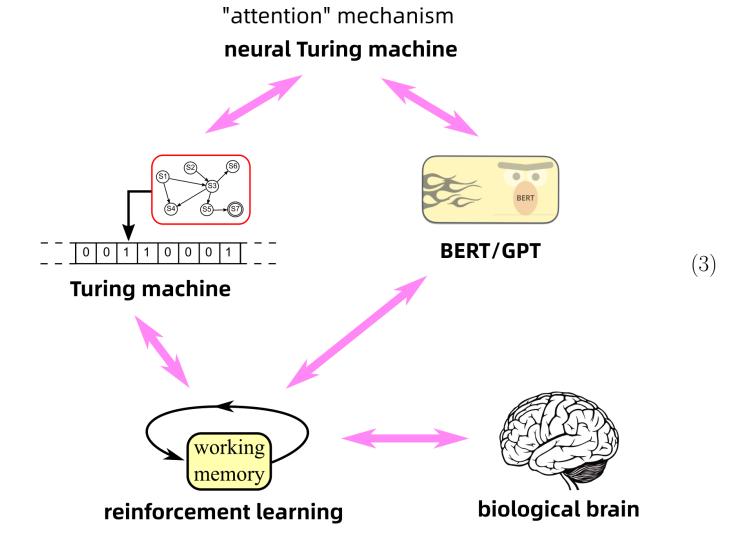
When we add an "action" or "control" variable u to it, it becomes the most basic **control system**:

$$F(x,u) \tag{2}$$

which is the setting for Dynamic Programming or **Reinforcement Learning**. The optimal solution for such systems is governed by the **Hamilton-Jacobi-Bellman equation**.

I call this the "standard model" because of the extreme simplicity of this setup, and that I don't know of other alternative models that deviate much from it.

The following diagram shows how the standard model relates to several other important areas, so we can reap profits from their interactions:



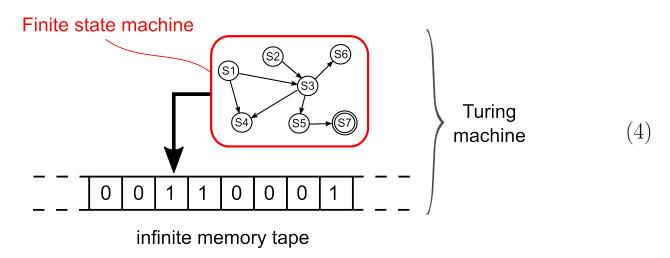
Recently, Yann LeCun's Energy-Based Models offers a way to circumvent the

problem of learning probability distributions over actions, when the action space is huge and high-dimensional.

2 Neural Turing Machines and Transformers

The attention mechanism was first proposed in the "Neural Turing Machine" paper by Graves et al.

Recall that a Turing machine is a **Finite State Machine** augmented with a **Memory Tape**:



In Neural Turing Machines, Graves *et al* proposed the attention mechanism for an RNN "Controller" (playing the role of the Finite State Machine) to read and write from a **Memory Matrix** (the tape), using a content-based addressing method.

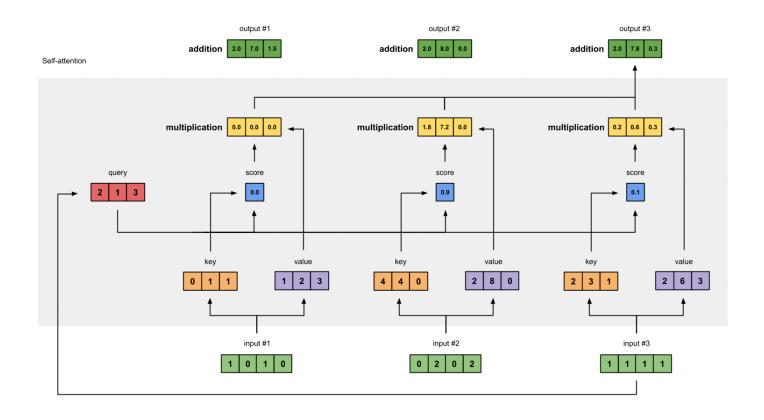
The Memory Matrix M consists of N items, each of constant size. The discreteness of the address would introduce discontinuities in gradients of the output, hence we need an **Attention Vector** to focus on a specific location in the memory matrix M.

The Attention Vector a is calculated via the following formula, familiar to students of the Transformer:

$$\vec{a} = \operatorname{soft} \max_{i} \{ \mathcal{D}(K, M_i) \}$$
 (5)

where D() is a similarity measure between the key K and memory item M_i . The key K is emitted by the Controller as the value that it is looking for.

This then evolved into the **Self Attention** mechanism used in all Transformers. Now let us refresh with this diagram illustrating Self-Attention (ripped from a blog article on the web):



The research done by Olah et al, in their 2021 paper <u>A Mathematical Framework for Transformer Circuits</u>, is very helpful towards understanding Transformers and Self-Attention. The paper is technically quite challenging, but thanks to the guidance of professor Xiao Da from Beijing I was able to understand the main ideas. Here I offer some pointers to help others understand the paper, without explaining it in full details.

(6)

The Self Attention A is calculated by matrix operations followed by **softmax**, and thus is non-linear. However, when A is held constant, the Transformer becomes a linear operation that can be expressed as **tensor products**:

$$T = \operatorname{Id} \otimes W_{U} \cdot \left(\operatorname{Id} + \sum_{h \in H_{1}} A^{h} \otimes W_{OV}^{h} \right) \cdot \operatorname{Id} \otimes W_{E}$$

$$\text{The token unembedding maps residual stream vectors to logits.}$$

$$\text{The attention layer has multiple heads.}$$

$$\text{The result of each is added into the residual stream vectors.}$$

$$\text{The token embedding maps tokens to residual stream vectors.}$$

Tensor product

Recall that a **linear** map is defined between two vector spaces:

$$F: U \to V. \tag{8}$$

Similarly one can define a **bi-linear** map:

$$\Phi: V \times W \to U \tag{9}$$

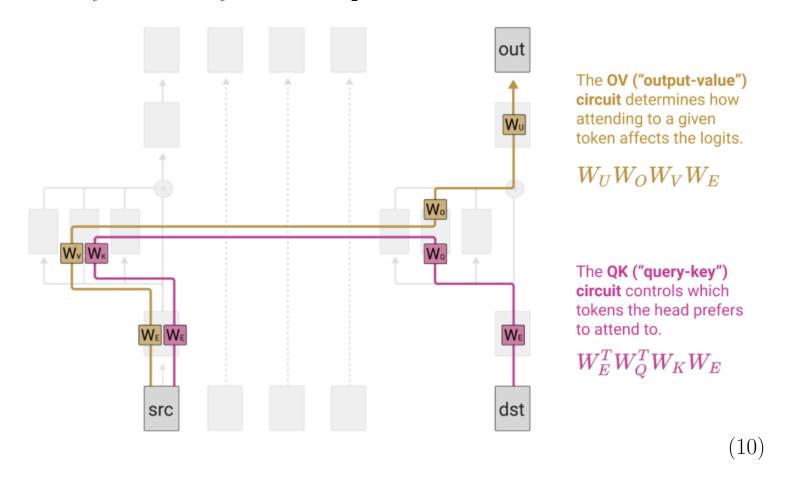
that is linear in both its first and second arguments. The tensor product \otimes is the **universal** multi-linear map.

The tensor product generalizes to the mathematically important **monoidal** categories. The latter captures the associativity (and optionally commutativity, for which we have symmetric monoidal categories), but the linearity is abstracted away.

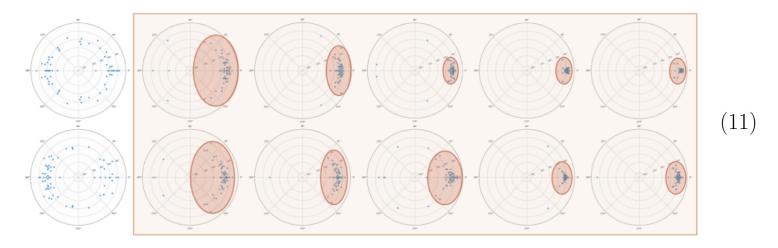
Monoidal categories can be depicted by **String Diagrams**. There are also **Neural String Diagrams** that describes the structure of neural networks. For example, the Transformer layer is **equivariant** in its inputs.

In the Transformer, we can see **Input Values** flowing through some "circuits"

defined by matrices to yield the **Output Values**:



Some Attention Heads merely perform "copying" of a vector from a previous layer to the next. If we spell this out as a linear equation, $W\vec{x} = \lambda \vec{x}$, where the transformation W merely results in a scaling of the vector \vec{x} . This is just an eigenvector equation. So if we plot the eigenvalues of the transformation matrices on the complex plane, the "copy" maps would have eigenvalues close to positive real numbers. The results shows that such "copy" maps are ubiquitous in Attention Heads (here 10 out of 12 maps are positive):



Such Attention Heads may be interpreted as **universally-quantified** (\forall) logic

rules. For example when we say "all men are mortal":

$$\forall x. \ Human(x) \Rightarrow Mortal(x) \tag{12}$$

any object instantiated as x (eg. "Socrates") would have to be **copied** from the LHS to the RHS.

3 Relation to the biological brain

There are two distinct aspects in the brain:

- Short-term or Working Memory is the **electric activation** of neuronal populations.
- Long-term memory is stored as synaptic strengths, established by synaptic formation and strengthening. The transfer from STM to LTM is called memory consolidation.

One theory has it that the prefrontal cortex maintains a number of "thoughts" with sub-populations or, perhaps, with **micro-columns**. These activated sub-populations are in competition with each other, through **lateral inhibition**. The thought(s) that win are the thoughts we retain – they "make sense".

4 Abductive reasoning

Abductive reasoning is basically just **bidirectional** inference.

Abduction has been relatively neglected in AGI research, which focuses on forward inference. Recently there is a call to study this important aspect.

When a system has both forward and backward connections, it forms a loop and its dynamics is likely to produce "resonance". This harks back to the ART (Adaptive Resonance Theory) proposed by Grossberg and Carpenter beginning in the 1980s.

Such resonance behavior can be viewed as the system seeking to minimize an energy, ie, trying to find the "best explanation" to a set of facts.

5 Dealing with assumptions

Example of an assumption: "If I play move x now, I will checkmate in 3 moves".

Tic Tac Toe example

Assume the current board is $\frac{| \cdot | \circ}{| \cdot |}$ and it's \times 's turn to play.

 \times can do the "double fork" by playing $\frac{| \cdot | \cdot |}{| \cdot |}$.

But how can an AGI know (or prove) this?

If the current board is $\frac{|\cdot| \circ}{|\cdot| \times |\cdot|}$ then a double fork exists. We need a predicate to detect double forks.

We need to reason that even if \bigcirc plays the "blocking" move $\frac{\bigcirc | \bigcirc |}{\bigcirc | \times | \times}$, \times can still win.

We can easily express the conditions for \times -can-win, but the difficult part is to make the assumption in red, in other words:

$$red-move \rightarrow \times -can-win$$
 (13)

The difficulty lies in that the LHS is **not true** under the current facts. This conditional statement must be proven by, first, assuming the LHS, and then deriving the RHS. Then the assumption is **discharged** and the conditional statement is proven, via the $(\rightarrow I)$ rule.

In the old days, in classical AI, assumptions are handled with **Truth Mainte-nance Systems** that keep track of inference traces symbolically. These systems can get quite complicated with the need to track multiple assumptions. For example, when we plan a bank robbery, we need to consider many possible forking scenarios.

Suppose M, N are proofs of $M : \phi \to \psi$ and $N : \phi$. Then the proof of ψ would be the application of M to N, denoted as @(M, N) or simply MN.

The assumption rule (Ax):

$$\Gamma, \phi \vdash \phi \qquad (Ax)$$
 (14)

for example can be written as:

$$x: \phi, \ y: \psi \vdash x: \phi$$
 (Ax)

which is why we say that an assumption is a λ -variable.

Discharging an assumption (ie, using the \rightarrow I rule) results in a λ -term.

An AGI needs the ability to place an implication $\phi \to \psi$ into working memory, and to prove it using the $(\to I)$ rule, ie, by making an assumption.

Algorithm: Put the assumption A in Working Memory. Make inferences, marking all conclusions with $A \to *$. When enough conclusions are obtained, remove the assumption A from Working Memory.