

LOGIC	facts	rules
ALGEBRA	element	element
	$p \in A$	$(p \rightarrow q) \in A$
WORLD	states	state transitions
	$x_t$	$x_t \xrightarrow{f} x_{t+1}$

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$x_t$   
 $\delta x$   
 $qdded$   
 $x_t$   
 $x_{t+1}$   
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 $F(x) = 0\dot{x} = f(x)$

(2)

$F$   
 $f$   
 $f$   
 $(x_t) = x_{t+1} - x_t = \delta x$

(3)

$\{x_i\}$   
 $F(x_t) = 0(x_t) = \delta x = x_{t+1} - x_t$

(4)

$F$   
 $f$   
 $x_t$   
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 $F$   
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 $F(x_t)$   
 $f(x_t)$

Logic formula

$$\bigtriangleup_{\forall x.x}$$

$$\forall x.x \rightarrow x$$

$$\forall x,y,z.x,y \wedge y,z \rightarrow_{x,z}$$

general Horn formula

$$\forall_{x...} P \wedge Q \wedge R... \rightarrow Z$$

Algebraic form

$$\begin{matrix} \vdots \\ h(x) \\ \forall_x h(x) \end{matrix}$$

$$\forall_x (1 + h(x) + h(x) \cdot m(x))$$

$$\forall_x \forall_y \forall_z (1 + f(x,y) \cdot f(y,z) + f(x,y) \cdot f(y,z) \cdot g(x,z))$$

$$\mapsto$$

$$\forall_{x...} (1 + P \cdot Q \cdot R... + P \cdot Q \cdot R... \cdot Z)$$

$$\mapsto$$

(5)

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$$\mathcal{L} = \sum_{\text{eqns}} \epsilon^2 = \sum_i \left(\phi_i(x...) - 1\right)^2.$$

(6)

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$$\nabla_{\Phi} \mathcal{L} = \frac{\partial \mathcal{L}}{\partial \Phi}$$

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$$x_t \rightarrow x_{t+\Delta t}$$

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$x_t$

$$\text{Intg}(\delta x) =$$

$$P(\delta x | x_t)$$

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