

# Schema Enrichment in Knowledge Bases

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## ABSTRACT

The Semantic Web is still growing and the availability of large knowledge graphs increased over the past years. In spite of the growing number of knowledge bases there exist very few with a sophisticated schema. Often they only consist of a collection of facts with no consistent structure. Other knowledge bases contain only schema information without instances of the defined schemata.

But only the combination of both of these extremes, sophisticated schema and available instance data can enable powerful reasoning, easier checking for consistency and improved queryability.

This report summarizes the content of two papers: (1) “Class expression learning for ontology engineering” by Lehmann et al and (2) “Universal OWL Axiom Enrichment for Large Knowledge Bases” by Böhmann et al. The method of the first article focuses at finding and creating class expressions in an automatic or semiautomatic approach based on given knowledge in the graph. Whereas the methods of the second paper enrichs knowledge bases with different types of OWL2 axioms.

## 1. INTRODUCTION

While the availability and size of knowledge bases has grown dramatically in the last few years, there is still often a significant lack of sophisticated schema. Enrichment of schema information based on already existing data is the main content of this report. To illustrate the benefits of a sophisticated schema together with reliable instance data consider the following example.

*Example 1.* Imagine a knowledge base containing famous persons like Barack Obama, Mahatma Gandhi, Elvis Presley etc. and a property called **birthPlace**. An algorithm may find out that every of these person contains this property and therefore the **birthPlace** can be a functional property with the domain **Person**.

```
ObjectProperty: birthPlace
Domain: Person
Range: Place
SubPropertyOf: hasBeenAt
```

Adding such axiom to the knowledge base can have several benefits[3]: (1) Axioms can serve as documentation for the right usage of the schema, (2) adding additional schema can improve consistency and help to debug missing or incorrect information, (3) additional (implicit) information can be inferred, in our example every person also **hasBeenAt** their **birthPlace**. Adding new axioms and finding/fixing missing information can be done in an semi-automated approach. A knowledge engineer can then decide if new axioms are fitting and existing data must be adjusted.

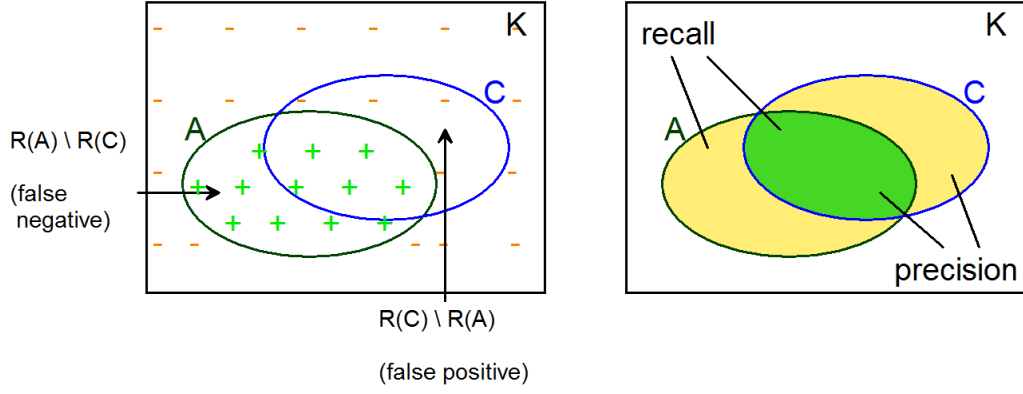
In summary, the combination of a good schema with large instance data allows for powerful reasoning, improved query ability and simplified consistency checking.

After a short description of the term *enrichment* this report explains the ideas of the class learning algorithms by Lehman et al. Afterwards the concept behind semantic enrichment with OWL axioms is explained. The last chapter focuses on different heuristic used in the previously described methods. The last part of the reports consists of a short evaluation and related work.

## 2. ENRICHMENT OVERVIEW

In this context the term enrichment describes the extension of the (semantic) schema of a knowledge base. The process of knowledge base enrichment increases the semantic richness and the expressiveness of an ontology. The goal of the enrichment progress is to find axioms, which can be added to an existing ontology. A special case is to find definition of classes and subclasses. This process is closely related to the Inductive Logic Programming (ILP) as it is described later in this report. Ontology enrichment methods usually depend on machine learning or on applying heuristics to find additional axioms in the knowledge graph.[3]

As stated before, knowledge base enrichment usually work on existing data to improve the semantic schema. It supports the so called *grass-root* approach for creating ontologies. Here the whole ontology structure is not created upfront, but evolves over time and with every part of data that is added to the knowledge base.[3]



**Figure 1:** This figure visualises the class  $A$  and the expression to test  $C$  as a Venn diagram. It also shows the terms *recall* and *precision*.

### 3. CLASS LEARNING

#### 3.1 Motivation

The class learning approach is one method of enrichment of knowledge bases. It aims at finding new definition of classes to extend the semantic schema. For the motivation of the method consider the following example.

*Example 2.* For this example consider a knowledge base containing a class *President of the United States* with instance data like Abraham Lincoln, John F. Kennedy, Bill Clinton and Barack Obama. A class Learning algorithm may suggest that the President class is equivalent to the following two class expressions:

- 1) *Person and born in the USA*
- 2) *American citizen and born in the USA*<sup>1</sup>

These suggestions would then be presented to a knowledge engineer who than can decide if they are plausible and therefore should be added to the knowledge graph or should be discarded. Should the engineer for instance choose the second statement, he could check if there are instances of the class *President*, where the individual is not of type American citizen. This could indicate an error or missing information in the knowledge graph which could then be fixed in this semi-automated approach by the knowledge engineer.

#### 3.2 Learning Problem

The problem of learning class definitions for given data depend on the so called inductive reasoning as opposed to inference or deductive reasoning. [7] Inductive Reasoning is also a key concept in Inductive Logic Programming.

*Definition 1.* We are searching for a formal description of the class  $A$ , which has existing instances in the examined ontology. A possible class expression  $C$  then contains axioms of the form  $A \subseteq C$  or  $A \equiv C$ .

<sup>1</sup>The class 'American citizen' is here a subclass of 'Person', which makes the second statement more specific.

This means that the learned expression  $C$  is a description of the individuals of  $A$ . In our president example, the individuals are the presidents John F. Kennedy, Barack Obama etc. whereas  $C$  can be one of the suggested expression. In many cases there will be no exact solution for  $C$ , but rather an approximation. This can be the case, if the knowledge base contains false class assignments or missing information. In our example the birthplace of Thomas Jefferson might be missing in the ontology. However, if most of the other presidents have the correct birthplace the learning algorithm may still suggest the expressions. Again, missing information may be completed by the knowledge engineer.

In a complex knowledge base a class learning algorithm may find many new class definition and often different expression for the same class. Based on Occam's razor [4] simple solutions are preferred over complex ones, because they are more readable and thus easier for the knowledge engineer to evaluate. Simplicity is measured in a straight forward way: the length of an expression, which consists of role, concept and quantifiers. The algorithm is biased towards shorter expressions. [7]

#### 3.3 Algorithm

One algorithm for solving the learning problem is called CELOE (Class Expression Learning for Ontology Engineering). It is described in [7]. An brief overview of CELOE is given in Figure 2. The algorithm follows the "generate and test" approach which is the common concept in ILP. [11] In the learning process many class expression are created and tested against the background knowledge. Each of these class expressions is evaluated using different heuristics, which are described in detail in a separate section.

To find appropriate class expression to describe existing classes CELOE uses a so called *refinement operator*. The idea of these operator is based on the work in [8],[9] and [10]. Refinement operators are used to search in the space of expressions. It can be seen as a top-down algorithm as it is illustrated in Figure 3. As an example consider the following path ( $\rightsquigarrow$  indicates a refinement step):

$T \rightsquigarrow \text{Person} \rightsquigarrow \text{Person} \sqcap \text{takesPartIn.T} \rightsquigarrow \text{Person} \sqcap$

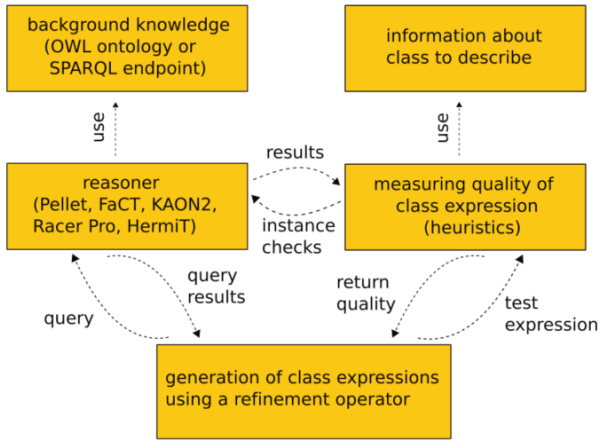


Figure 2: CELOE[7]

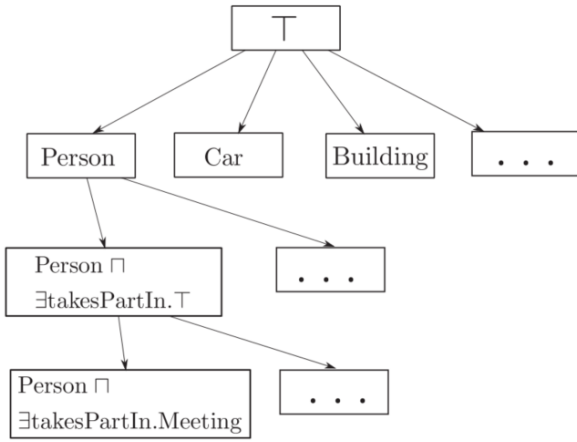


Figure 3: Tree[7]

*takesPartIn.Meeting*

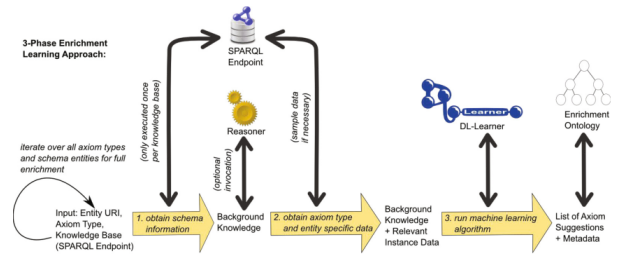


Figure 4: 3-Phase Enrichment Workflow[3]

## 4. ENRICHMENT WITH OWL AXIOMS

OWL offers many different types of axioms for a method to enrich the knowledge base. Figure 4 shows the 3 steps in the enrichment workflow as described in [3]:

1. The first phase is about obtaining general information about the knowledge base, in particular axioms, which define the class hierarchy are obtained. The schema queried via SPARQL, but is loaded only once.
2. In the second phase data is again obtained via SPARQL. These background checks allows the method to learn and test new axioms. Examples for axiom types are explained in the following text.
3. The score of axiom candidates is computed and the result is returned.

The algorithm for suggestion of new axioms is based on checking and counting RDF triples. In the following example we want to learn if the class *A* is an appropriate domain of a predicate *p*. For that we count the triples that match this statement to obtain a score.

*Example 3.* Lets look at the predicate `onto:attendsMeeting` and check if we can find a suitable candidate for a domain. Note that `onto:Manager` is a subclass of `onto:Employee`.

### Listing 1: Triples written in turtle syntax

```

onto:Software_Engineer
  onto:attendsMeeting      onto:TeamMeeting;
  rdf:type                 onto:Employee.
onto:Software_Architekt
  onto:attendsMeeting      onto:TeamMeeting;
  rdf:type                 onto:Employee.
onto:Project_Manager
  onto:attendsMeeting      onto:ManagerMeeting;
  rdf:type                 onto:Manager.
onto:Manager               rdfs:subClassOf  onto:Employee.

```

Looking at this example we would obtain a score of 33.3 % (1 out of 3) for the class `onto:Manager` and 100 % (3 out of 3) for the class `onto:Employee`.

Obviously this extreme simple and straightforward method of calculating the score for the domain of a predicate *p* has some limitation. Mainly the method doesn't discriminate between a score calculated by having 100 out of 100 correct

observations or only 3 out of 3. Different methods, for example the Wald method [?], overcome that problem. More involved heuristics are shown in the next section.

## 4.1 Obtaining Axioms via SPARQL queries

This section explains how SPARQL queries are used to extract information in step 2 of the enrichment workflow.

### Subclass and Disjointness of classes

This query evaluates all individuals (?ind) and checks if they are instance of the user defined class definition in \$class. In this query higher count indicates a better candidate for a superclass. Lower value indicates a disjointness.

```
SELECT ?type (COUNT(?ind ) AS ?count ) WHERE {
  ?ind a <$class >.
  ?ind a ?type .
} GROUP BY ?type
```

### Subsumption and Disjointness of properties

A somewhat similar query can be used to learn subsumption and disjointness of predicates.

```
SELECT ?p (COUNT(? s ) AS ?count ) WHERE {
  ?s ?p ?o .
  ?s <$property> ?o .
} GROUP BY ?p
```

### Domain and Range of properties

A query for the domain of a property counts the occurrences subjects of type ?type having the property \$property.

```
SELECT ?type COUNT(DISTINCT ?ind ) WHERE {
  ?ind <$property> ?o .
  ?ind a ?type .
} GROUP BY ?type
```

The query for the range of \$property is analog. It can be also distinguished between object and data properties. Here only the queries for object properties are listed.

```
SELECT ?type (COUNT(DISTINCT ?ind ) AS ?cnt ) WHERE {
  ?s <$property> ? ind .
  ?ind a ?type .
} GROUP BY ?type
```

### Inverse of Properties

To check if a property is inverse we check the \$property with subject and object and in swapped position. As always we count how often the expression holds.

```
SELECT ?p (COUNT(*) AS ?count ) WHERE {
  ?s <$property> ?o .
  ?o ?p ?s .
} GROUP BY ?p
```

## 5. HEURISTICS

### 5.1 Finding the right heuristic

A heuristic measures how well a given class expression fits the learning problem. [7] To test an algorithm we must have positive and negative examples. As we want to describe class  $A$  with  $C$  we can consider every instance of  $A$  as a positive and everything else as negative examples. The predictive

accuracy can be described as:

$$predacc(C) = 1 - \frac{|R(A) \setminus R(C)| + |R(C) \setminus R(A)|}{n} \quad n = |Ind(K)|$$

Here,  $Ind(K)$  stands for the set of individuals in the knowledge base.  $R(A) \setminus R(C)$  are the false negatives whereas  $R(C) \setminus R(A)$  are the false positives.

As you can see in Figure 2 for the term *precision* we consider the intersection of  $A$  and  $C$  ( $R(A) \cap R(C)$ ) and the false positive. In other words, how many individuals are rightful considered with our class expression  $C$ .

For the other term *recall* we consider again the intersection of  $A$  and  $C$  and the false negative. This score tells us how many individuals of  $A$  we can describe with our class expression  $C$ .

Table 4.1 compares the score of four different heuristics. They are:

- **pred. acc.** The formula for the predictive accuracy was shown above.
- **F-Measure** The F-Measure is defined as harmonic mean of precision and recall. It can be weighted by a factor  $\beta$ , [7] choose 3 for  $\beta$  for learning super classes, which gives recall a higher weight than precision.  

$$F-Measure = \frac{\beta+1}{\frac{\beta}{prec} + \frac{1}{acc}}$$
- **A-Measure** For the A-Measure we choose the arithmetic mean of precision and recall.  

$$A-Measure = \frac{prec+acc}{2}$$
- **Jaccard** The Jaccard index is well known to compare two sets. It is defined as the size of the intersection divided by the size of the union of the sets.  

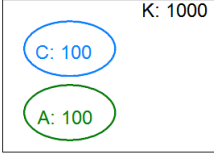
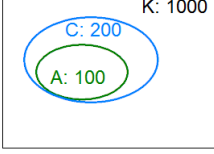
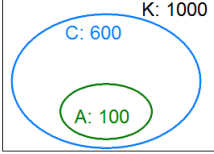
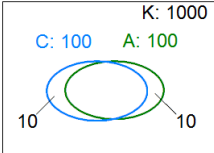
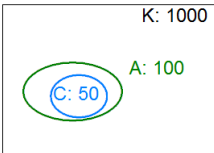
$$Jaccard(A, B) = \frac{|A \cap C|}{|A \cup C|}$$

### 5.2 Efficient heuristic computation

For big knowledge base the performance and efficiency of the algorithm is crucial. To compute and test class expression retrieval operations are often required. To minimize the cost and improve performance [7] provide three optimisations:

- **Reduction of instance checks** The obvious choice is to reduce the number of instance checks required to test expressions. Assuming that we want to learn an equivalence axiom for class  $A$  with the super class  $A'$ . Instead of checking every individual of the knowledge graph we can restrict our retrieval operation to instances of  $A'$ .
- **Approximate and closed world reasoning** To deal with the very high number of instance checks against the knowledge base CELOE uses a special reasoner.[7] It uses an approximate and incomplete reasoning for fast instance checks (FIC). The reasoner depends on the first run on a standard OWL reasoner to check instances and property relationships. The result of this first reasoning is stored in memory for fast (but approximated) instance checks. The reasoner follows a closed world assumption.
- **Stochastic coverage computation** This optimisation again reduces the necessary instance checks. Looking at the different heuristics, we can see that  $|R(A)|$

**Table 1: Heuristics**

Illustration	accuracy & recall		pred. acc.	F-Measure	A-Measure	Jaccard
	accuracy	0%	80 %	0 %	0 %	0 %
	recall	0%				
	accuracy	50%	90 %	66.7 %	75 %	50 %
	recall	100%				
	accuracy	16.7%	50 %	28.6 %	58.3 %	16.7 %
	recall	100%				
	accuracy	90%	98 %	90 %	90 %	81.8 %
	recall	90%				
	accuracy	50%	95 %	66.7 %	75 %	50 %
	recall	100%				

needs to be computed only once whereas e.g. the expensive expression  $R(A) \cap R(C)$  is computed for every different  $C$ . To improve performance we can try to approximate the result by testing randomly drawn objects and checking if we are sufficiently confident that our estimation is within a certain bound.

## 6. EVALUATION

To evaluate the methods of class learning, the authors of [7] tested their algorithm on a variety of real world ontologies of different sizes and domains. The goal of the evaluation consisted of 3 parts: determine the influence of reasoning and heuristics on suggestions, test the performance and efficiency on large real world ontologies and to test the accuracy of approximations described in section 5.2.

To perform the evaluation, the authors in [7] wrote a dedicated plugin for the Protégé editor. The plugin first looks for classes with enough instances. For each of these classes they ran the CELOE algorithm to generate suggestions for definitions, here they tested two different reasoner and the previously described five heuristics. The results of these tests were categorized in three main categories: (1) the suggestion improves the ontology (improvement), (2) the suggestion does not improve the ontology and therefor should

not be added to the ontology (not), (3) adding the suggestion results in a modelling error (error). A small part of the results is shown in Table 6, the full evaluation results are shown in [7]. The second evaluation results were

**Table 2: Evaluation**

Reasoner/heuristic	Improv. Not acc.	missed Improv.
Pellet/F-Measure	16.70	64.66
Pellet/A-Measure	16.70	64.66
Pellet/pred.acc.	16.59	64.93
Pellet FIC/F-Measure	36.60	52.62
Pellet FIC/A-Measure	36.19	52.84
Pellet FIC/pred.acc.	32.99	52.58

based on the performance of the approximation reasoner as described in section 5.2. The tests showed that an approximation lead to significant performance improvement, this is especially the case for larger ontologies. The time required to test a class expression showed smaller variations and a performance gain of several orders of magnitudes has been achieved. The approximation has shown to be very accurate and had hardly any influence on the learning algorithm.

Preliminary Evaluation has also been done in [3] for OWL

axiom enrichment. The authors choosed DBpedia to test their algorithms. Table 6 shows a small subset of the results. In [3] the evaluation is discussed in great detail. For example the three newly discovered symmetric object properties are: `dbo:neighboringMunicipality`, `dbo:sisterCollege` and `dbo:currentPartner`.

**Table 3: Evaluation combined of Object and data property**

axiom type	recall	new axioms	precision
SubClassOf	180/185	155	75 %
EquivalentClasses	0/0	1812	50 %
DisjointClasses	0/0	2449	100 %
PropertyDomain	833/942	1298	54 %
PropertyRange	291/1032	500	46 %
SymmetricProperty	0/0	3	100 %

## 7. RELATED WORK

Related work can be divided into two categories: the first part covers supervised machine learning with OWL, the second part is focused on (semi-)automated ontology engineering methods.

Early work of supervised learning in description logic was published in [5, 6], which uses the so called *least common subsumer* to solve the learning problem. Later work invented the concept of the refinement operator to solve the problem in a top-down approach.[2] The refinement operator was later adapted for description logic [8, 9, 10] and is used as described in CELOE.

The starting point of (semi-)automatic ontology engineering was set by [12], a formal concept analysis was descibed in [1]. Another interesting approach is presented in [13] which proposes to improve knowlege bases through relation exploration. It is implemented in the RELExO framework.

## 8. CONCLUSIONS

The algorithms and methods summarized in this report like they were presented in [7] and [3] show promising results. The authors of [7] analysed their CELOE algorithm with different heuristics and proved that approximating heuristic values are often very accurate while improving the performance significantly. The strong bias towards shorter expressions increase the readability of suggestions and help the knowlege engineer to verify additional statements.

The enrichment methods in [3] also show great potential. The evaluation of this approached showed that the method also works on very large scales, like the size of the DBpedia knowlege base. In future works the authors will investigate enhancements in the presented methods and collaborate with the authors of [14] to further fine-tune the approach.

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