

## Problem L

# Irreducible Basic Fractions

**Input:** standard input

**Output:** standard output

**Time Limit:** 4 seconds

A fraction  $m / n$  is *basic* if  $0 \leq m < n$  and it is *irreducible* if  $\gcd(m, n) = 1$ . Given a positive integer  $n$ , in this problem you are required to find out the number of *irreducible basic fractions* with denominator  $n$ .

For example, the set of all *basic fractions* with denominator 12, before reduction to lowest terms, is

$$\frac{0}{12}, \frac{1}{12}, \frac{2}{12}, \frac{3}{12}, \frac{4}{12}, \frac{5}{12}, \frac{6}{12}, \frac{7}{12}, \frac{8}{12}, \frac{9}{12}, \frac{10}{12}, \frac{11}{12}$$

Reduction yields

$$\frac{0}{12}, \frac{1}{12}, \frac{1}{6}, \frac{1}{4}, \frac{1}{3}, \frac{5}{12}, \frac{1}{2}, \frac{7}{12}, \frac{2}{3}, \frac{3}{4}, \frac{5}{6}, \frac{11}{12}$$

Hence there are only the following 4 *irreducible basic fractions* with denominator 12

$$\frac{1}{12}, \frac{5}{12}, \frac{7}{12}, \frac{11}{12}$$

## Input

Each line of the input contains a positive integer  $n$  ( $< 1000000000$ ) and the input terminates with a value 0 for  $n$  (do not process this terminating value).

## Output

For each  $n$  in the input print a line containing the number of *irreducible basic fractions* with denominator  $n$

## Sample Input

```
12
123456
7654321
0
```

## Sample Output

4  
41088  
7251444

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**Rezaul Alam Chowdhury**

“I shot an arrow into the air,  
It fell to earth, I knew not where;  
For, so swiftly it flew, the sight  
Could not follow it in its flight.

I breathed a song into the air,  
It fell to earth, I knew not where;  
For who has sight so keen and strong,  
That it can follow the flight of song?

Long, Long afterward, in an oak  
I found the arrow, still unbroke;  
And the song from beginning to end,  
I found again in the heart of a friend.”