

## Problem C

# The Stern-Brocot Number System

**Input:** standard input

**Output:** standard output

The *Stern-Brocot tree* is a beautiful way for constructing the set of all nonnegative fractions  $m/n$  where  $m$  and  $n$  are relatively prime. The idea is to start with two fractions  $\left(\frac{0}{1}, \frac{1}{0}\right)$  and then repeat the following operations as many times as desired:

Insert  $\frac{m+m'}{n+n'}$  between two adjacent fractions  $\frac{m}{n}$  and  $\frac{m'}{n'}$ .

For example, the first step gives us one new entry between  $\frac{0}{1}$  and  $\frac{1}{0}$ ,

$$\frac{0}{1}, \frac{1}{1}, \frac{1}{0};$$

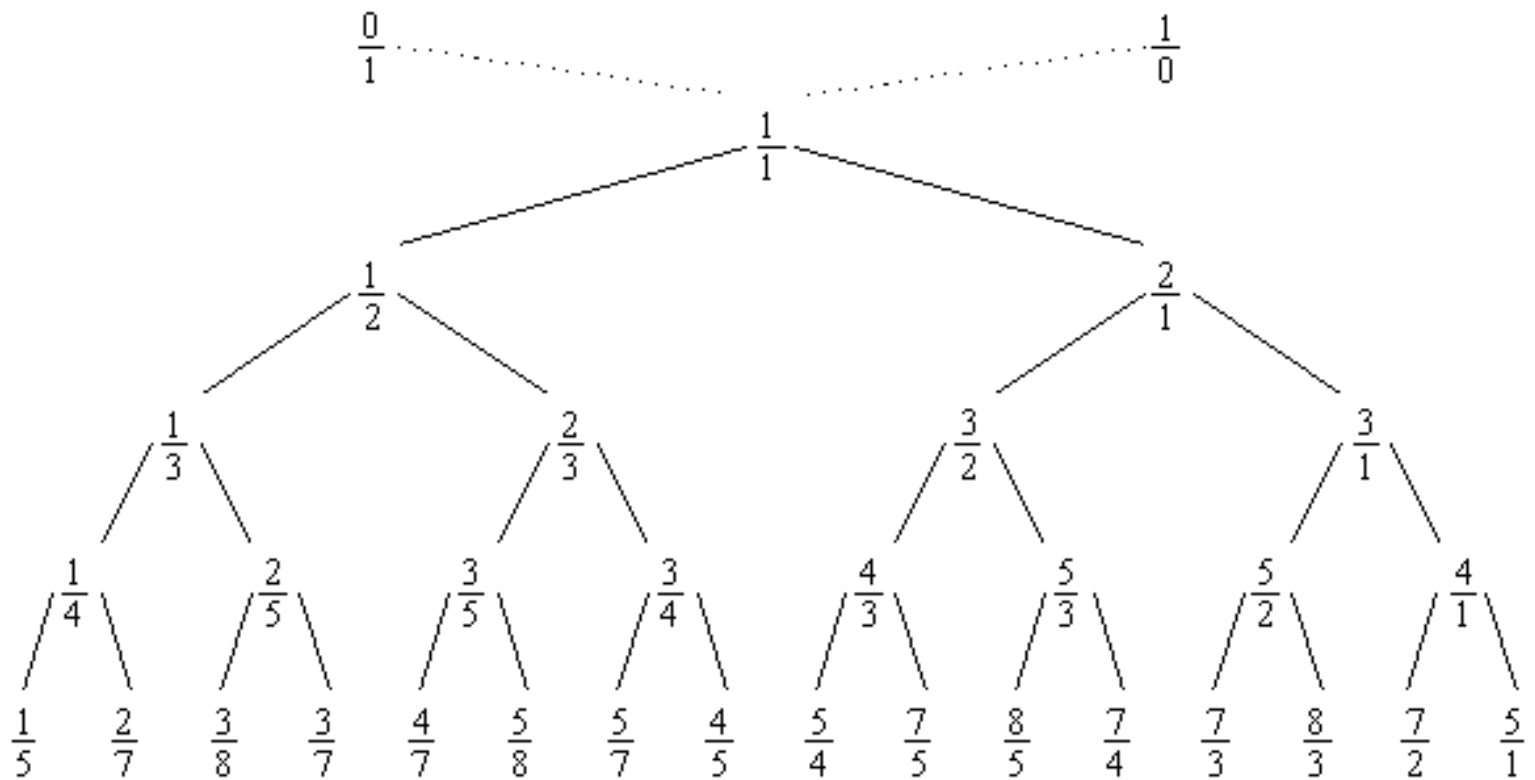
and the next gives two more:

$$\frac{0}{1}, \frac{1}{2}, \frac{1}{1}, \frac{2}{1}, \frac{1}{0}.$$

The next gives four more,

$$\frac{0}{1}, \frac{1}{3}, \frac{1}{2}, \frac{2}{3}, \frac{1}{1}, \frac{2}{2}, \frac{3}{1}, \frac{1}{1}, \frac{1}{0};$$

and then we will get 8, 16, and so on. The entire array can be regarded as an infinite binary tree structure whose top levels look like this:



The construction preserves order, and we couldn't possibly get the same fraction in two different places.

We can, in fact, regard the *Stern-Brocot tree* as a *number system* for representing rational numbers, because each positive, reduced fraction occurs exactly once. Let's use the letters *L* and *R* to stand for going down to the left or right branch as we proceed from the root of the tree to a particular fraction; then a string of *L*'s and *R*'s uniquely identifies a place in the tree. For example, *LRRL* means that we go left from

$\frac{1}{1}$  down to  $\frac{1}{2}$ , then right to  $\frac{2}{3}$ , then right to  $\frac{3}{4}$ , then left to  $\frac{5}{7}$ . We can consider *LRRL* to be a representation of  $\frac{5}{7}$ . Every positive fraction gets represented in this way as a unique string of *L*'s and *R*'s.

Well, actually there's a slight problem: The fraction  $\frac{1}{1}$  corresponds to the *empty* string, and we need a notation for that. Let's agree to call it *I*, because that looks something like 1 and it stands for "identity".

In this problem, given a positive rational fraction, you are expected to represent it in *Stern-Brocot number system*.

## Input

The input file contains multiple test cases. Each test case consists of a line contains two positive integers *m* and *n* where *m* and *n* are relatively prime. The input terminates with a test case containing two 1's for *m* and *n*, and this case must not be processed.

# Output

For each test case in the input file output a line containing the representation of the given fraction in the *Stern-Brocot number system*.

## Sample Input

```
5 7
878 323
1 1
```

## Sample Output

```
LRRL
RRLRRLRLLLLRLRRR
```

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