

End Semester Exam

Part-A

MATH-II, 26TH APRIL, 2016

TIME: — — — MINUTES, MAXIMUM MARKS: — — —

Name: _____

Roll No.: _____

Note: Encircle/Tick the **correct** answer for objective type questions. Each question carry 5 marks for correct answer and carry a **negative marking of 2 mark for wrong answer**. Overwriting will be treated as a wrong answer. Use only the last page of main answer sheet for rough work and calculation. Write down the final answer, no marks for formula or incomplete solution.

1. Let V be a vector space and let $S_1 = \{u_1, u_2, \dots, u_n\}$ and $S_2 = \{v_1, v_2, \dots, v_m\}$ be two subset of V . If S_1 spans V and S_2 is linearly independent, then

(A) $n \leq \dim V \leq m$ (B) $m \leq \dim V \leq n$ (C) $n < m \leq \dim V$ (D) $\dim V < n < m$

2. Let V be a seven-dimensional vector space and U, W both are six-dimensional distinct subspaces of V . Then $\dim(U \cap W) =$

(A) 6 (B) 2 (C) 5 (D) 1

3. Which of the following pairs of vectors is an orthogonal pair in \mathbb{R}^2 with respect to the inner product defined by $\langle u, v \rangle = 3u_1v_1 + 2u_2v_2$, where $u = (u_1, u_2)$, $v = (v_1, v_2)$.

(A) $u = (1, 1)$, $v = (1, -1)$ (B) $u = (1, -1)$, $v = (2, 3)$
(C) $u = (1, -1)$, $v = (3, 2)$ (D) $u = (1, 1)$, $v = (-1, -1)$

4. An interval in which the IVP $xy' + 2y = 4x^2$, $y(1) = 2$ has unique solution is _____.
Sol: $0 < t < \infty$

5. Third Picard's successive approximation of the IVP $y' = 4x(1+y)$, $y(0) = 0$ is _____.
Sol: $2x^2 + 2x^4 + \frac{4x^6}{3}$

6. Let $p(x)$, $q(x)$, $r(x)$ are continuous functions on an interval I . Further, suppose $y_1(x)$, $y_2(x)$ are any two solutions of the linear non-homogeneous equation $y'' + p(x)y' + q(x)y = r(x)$, $\forall x \in I$. Then $2ay_1 + 3by_2$ is also a solution for _____.
(Obtain conditions on the constants a and b)
Sol: $2a + 3b = 1$

7. A particular solution for $y'' + 4y = \operatorname{cosec} 2x$ is _____.
Sol: $-(1/2)x \cos 2x + (1/4) \sin 2x \ln(\sin 2x)$

8. Inverse Laplace trasformation for $\ln(1 + \frac{4a^2}{s^2})$ is _____.
Sol: $\frac{2}{t}[1 - \cos 2at]$