

Artificial Intelligence (AI)

Mid Term

Time: 90 minutes

Date: October 04, 2018

Max. Marks: 60

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Roll No. *16VCS126*

Please read the following instructions carefully.

- There are 4 questions printed on both sides.
- No marks for providing just expressions/answers unless accompanied with correct justification and/or derivation.
- In case of any doubt, make your assumption, write it clearly and continue.
- Be precise and to the point in your answers.

=====XXXXXX=====

1. Provide justifications to make the following statements hold.

- (a) DFS is *always* complete except under one condition. (Basically provide that condition with example.)
- (b) BFS provides the shortest path to the goal provided one condition is met. (Again provide that condition with a suitable example.)
- (c) DFS with fringe is computationally more robust than hill climbing.
- (d) For a two player zero sum game, minimax tree provides the optimal play against a perfect adversary.

3+4+4+4 Marks

2. Consider the Tiles problem as shown in Fig. 1.

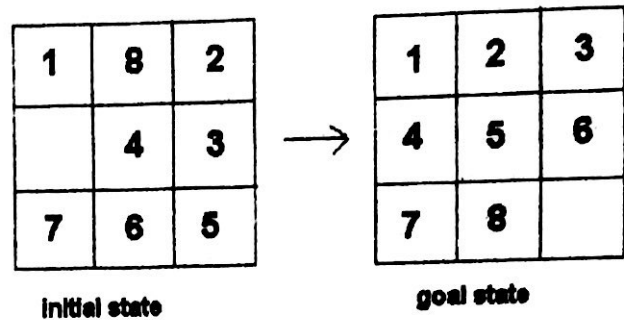


Figure 1: Tiles problem.

- (a) Design an A* algorithm for solving the above tiles problem.
- (b) Design two heuristics and compare them in terms of performance (measured with respect to the number of steps taken to reach the goal state).
- (c) Design a heuristic that is not admissible for the above problem.
- (d) Design a consistent heuristic for the above problem. Prove that it is admissible too.

5+3+2+(4+1) Marks

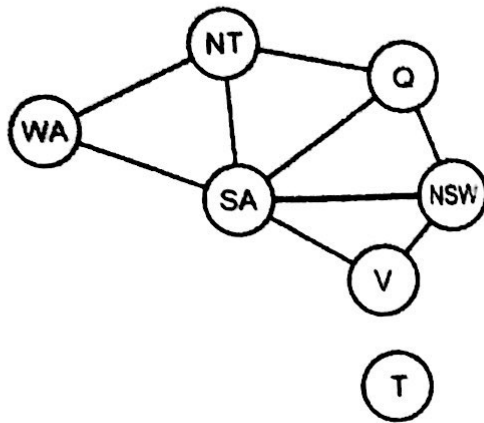


Figure 2: Graph for CSP for coloring Australia

3. Consider the coloring problem that we had discussed in the lectures on CSPs (Fig. 2). We are given that we can choose from a set of {blue, green, red} to color each node such that no two neighbours get the same color. We discussed many strategies in the class. Answer the following questions.
 - (a) Write the variables, domain and constraints for the problem.
 - (b) Explain how the Minimum Remaining Values and Least Constraining Value heuristics help in improving the time complexity for DFS with backtracking.
 - (c) In a quest to further improve backtracking, we introduced the notion of arc consistency. Discuss a scenario in which arc-consistency fails, i.e., even though the arcs are consistent, yet no valid assignment of the colors exist.
Hint: Think of 3-consistency.
 - (d) Show how the problem can be converted to tree structure to solve the problem efficiently. Can we efficiently find tree structures for all CSPs in general?
 - (e) Recall iterative improvement. In this algorithm, instead of starting from an empty assignment, we start from a random complete assignment. Solve the coloring problem using iterative improvement.

3+3+3+(2+1)+3 Marks

X Define X_n as the number of rows, columns, or diagonals with exactly n X's and no O's. Similarly, O_n is the number of rows, columns or diagonals with

just n O's. Assuming $n = 3$, the utility function assigns +1 to any position with $X_3 = 1$ and -1 to any position with $O_3 = 1$. All other terminal positions have utility 0. For nonterminal positions, we use a linear evaluation function defined as $Eval(s) = 3X_2(s) + X_1(s) - 3(O_2(s) + O_1(s))$.

- (a) Approximately how many possible games of tic-tac-toe are there?
- (b) Show the whole game tree starting from an empty board down to depth 2 (i.e., one X and one O on the board), taking symmetry into account.
- (c) Mark on your tree the evaluations of all the positions at depth 2.
- (d) Using the minimax algorithm, mark on your tree the backed-up values for the positions at depths 1 and 0, and use those values to choose the best starting move.
- (e) Circle the nodes at depth 2 that would not be evaluated if alpha-beta pruning were applied, assuming the nodes are generated in the optimal order for alpha-beta pruning.

3+3+3+3+3 Marks