Background

RR Lyrae variable stars (RRLs), commonly found in globular clusters (GCs), are important stellar candles used for measuring cosmic distances. Globular clusters, which are dense, old, and metal-poor star clusters, are primarily located in the Milky Way's halo. Due to the limited astronomical data available in the past, the membership ratios of variable stars have not been fully investigated. This motivates the search for the ratio of RR Lyrae stars in globular clusters using the newly released GAIA database.

Goals

- Using GAIA Data Release 3, analyze the membership ratio R of RRLs in GCs.
- Determine which cluster parameters influence R most.
- Propose **explanations** regarding the cause of such result.

Methodology

Estimating Number of Stars in Globular Clusters

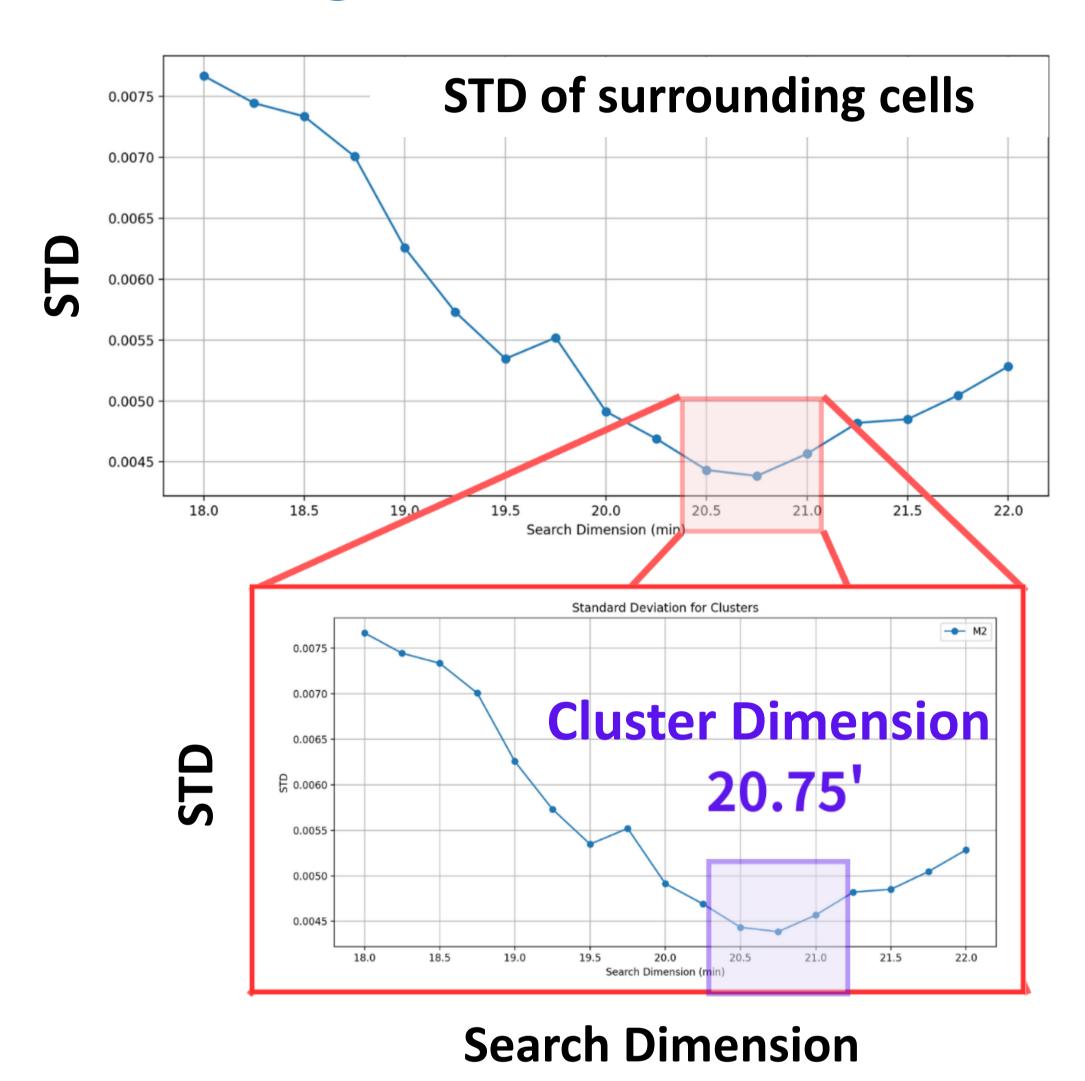


Figure 1 Estimating cluster dimension by calculating the dimension yielding lowest STD of stars surrounding the cluster.

Key Physical Parameters

Physical Parameter	Symbol	Unit
Age	A	Gyr (10 ⁹ years)
Metallicity [Fe/H]	M	dex
Half-light radius	r	Light years (ly)
Membership ratio of RRLs	R	Parts per million (ppm)

$$R \equiv \frac{\text{Number of RRLs in GC}}{\text{Total Number of Stars in GC}} \times 10^6 \text{ ppm}$$

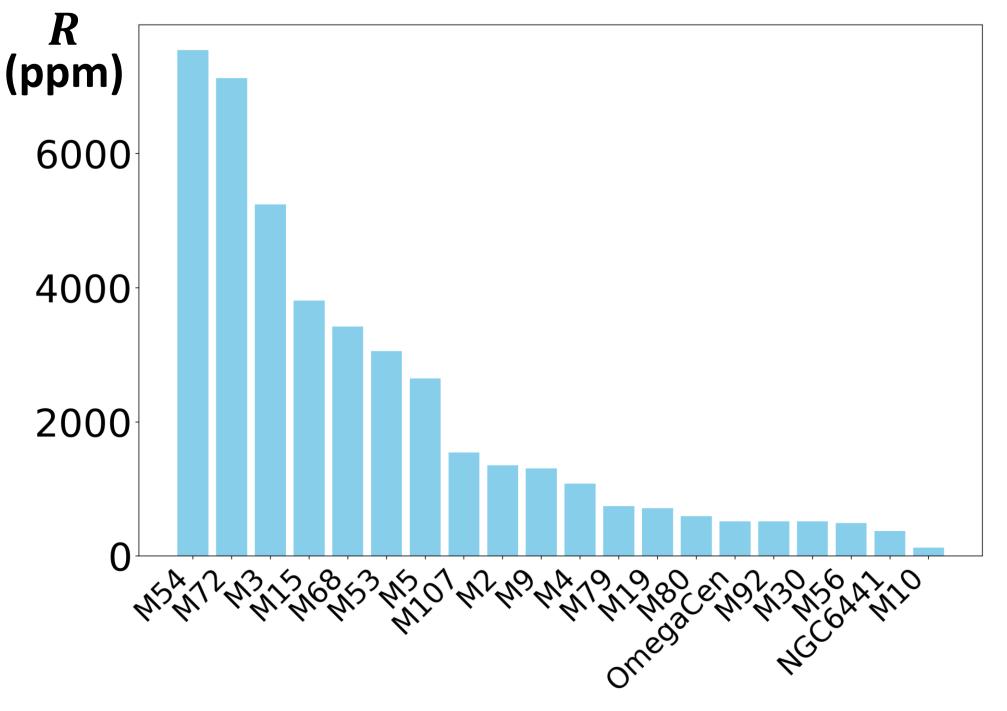


Figure 4 Bar chart of *R* for 20 GCs.

This work has made use of data from the European Space Agency (ESA) mission **Gaia**.

418	1102	405	Number of stars ≈ 32314 – AVG of surrounding cells
1537	32314	1577	418, 1102,, 392
400	1085	392	Best estimate when STD of surrounding cells Is minimum.

Figure 2 Heatmap of number of stars. Numbers represent the number of stars in the 3 by 3 grid. Search dimension expanded until STD of surrounding cells reach minimum.

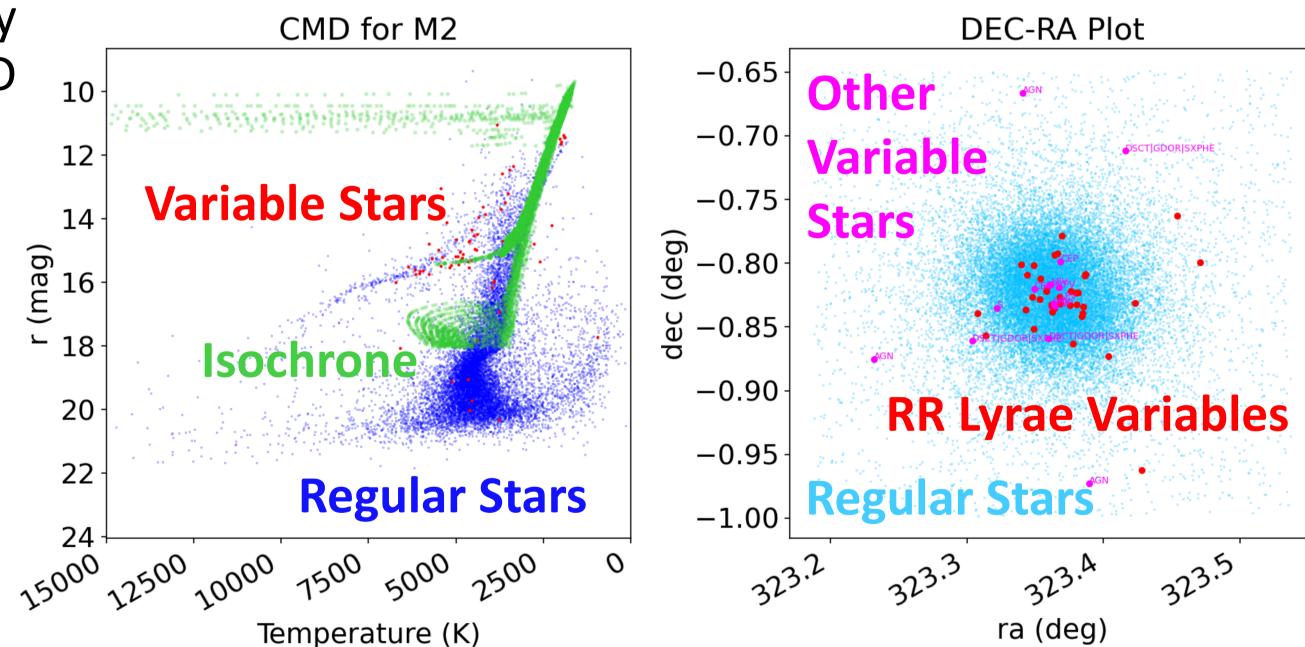


Figure 3 CMD (left) and DEC-RA plot (right) of cluster M2. The isochrone line was shifted to fit the blue dots. Variable stars that deviate from the isochrone line were removed.

Membership Ratios $\log A \equiv \log_{10} A$

$$\alpha = \mathbf{a}_{\alpha} \cdot \log A + \mathbf{b}_{\alpha} \cdot M$$
$$\beta = \mathbf{a}_{\beta} \cdot \log A + \mathbf{b}_{\beta} \cdot M + \mathbf{c}_{\beta} \cdot \log r$$

Google Colab & VScode						
Python						
GAIA Database			Isochrone			
astroquery.gaia		isochrones.mist				
Data Analysis		Regression		Plotting		
Excel		scipy		numpy		
AVG	Average		DEC	Declination		
STD	Standard deviation		RA	Right Ascension		
RRL	RR Lyrae					
GC	Globular C	Globular Cluster				
CMD	MD Color-Magnitude Diagram					

Star Cluster Evolution

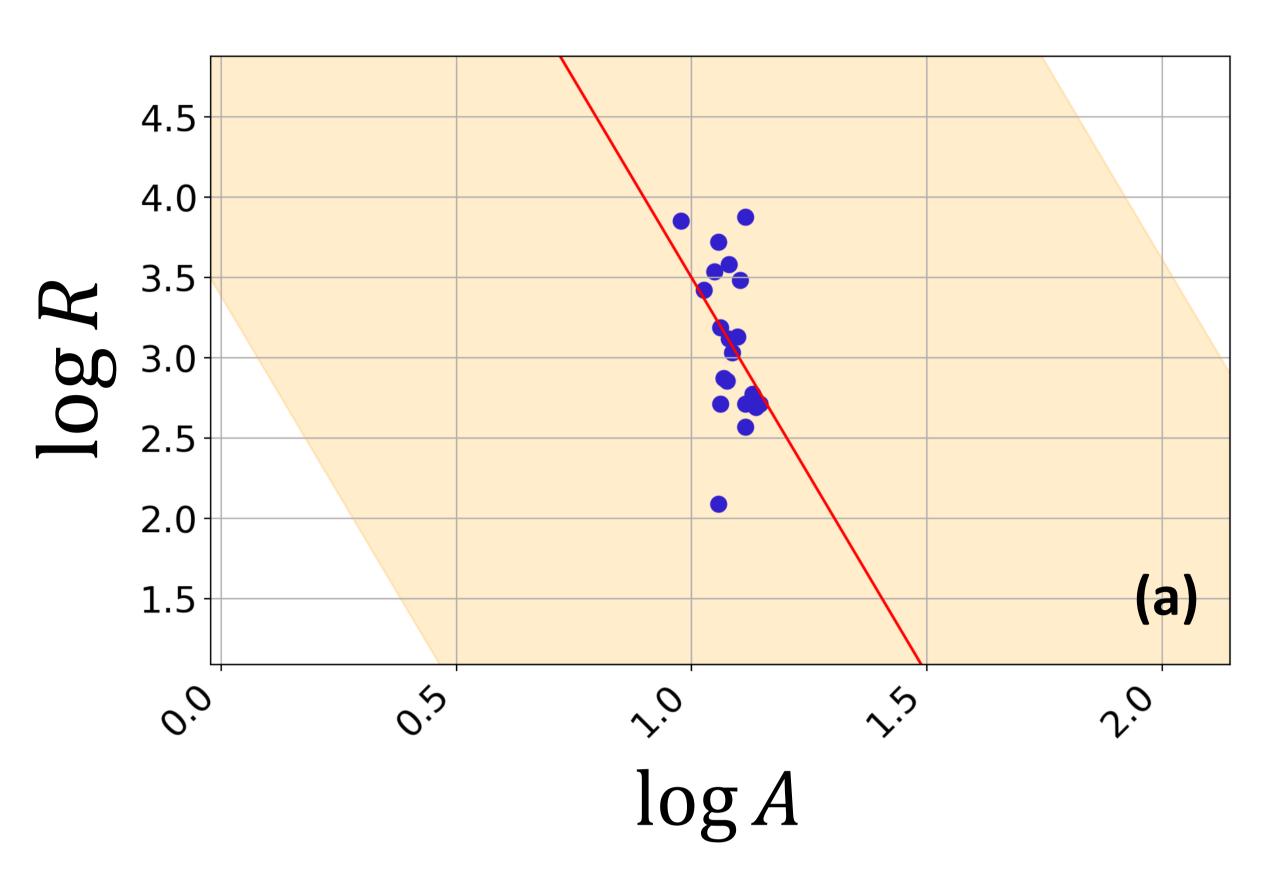
— Revealed by GAIA

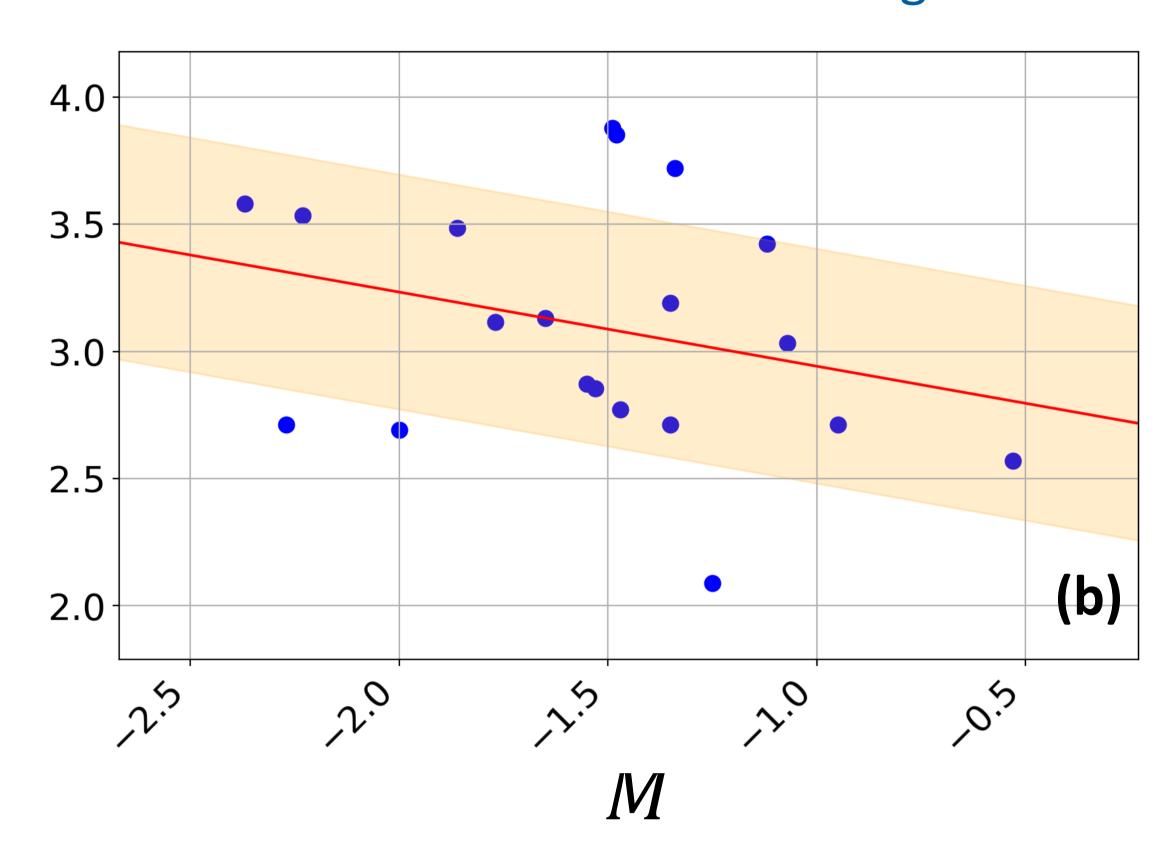
Cheng-You Ho, Taiwan

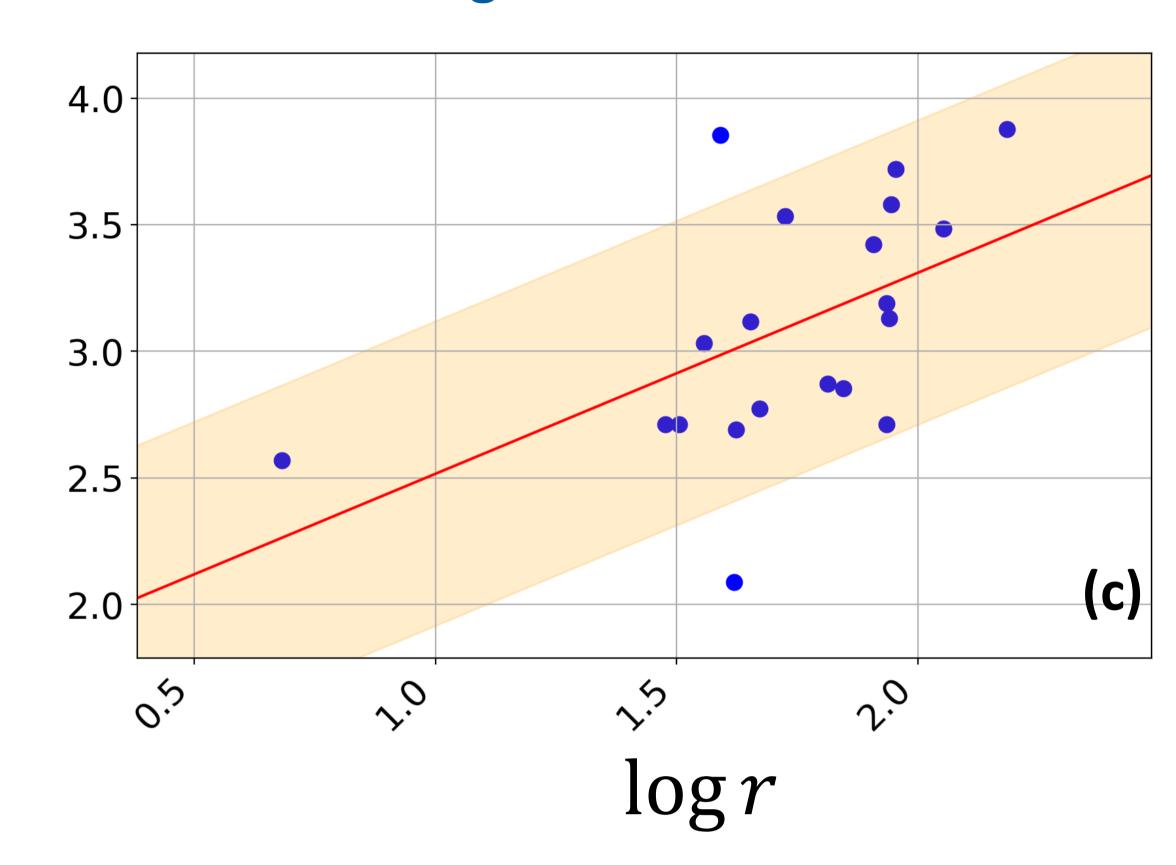
Results









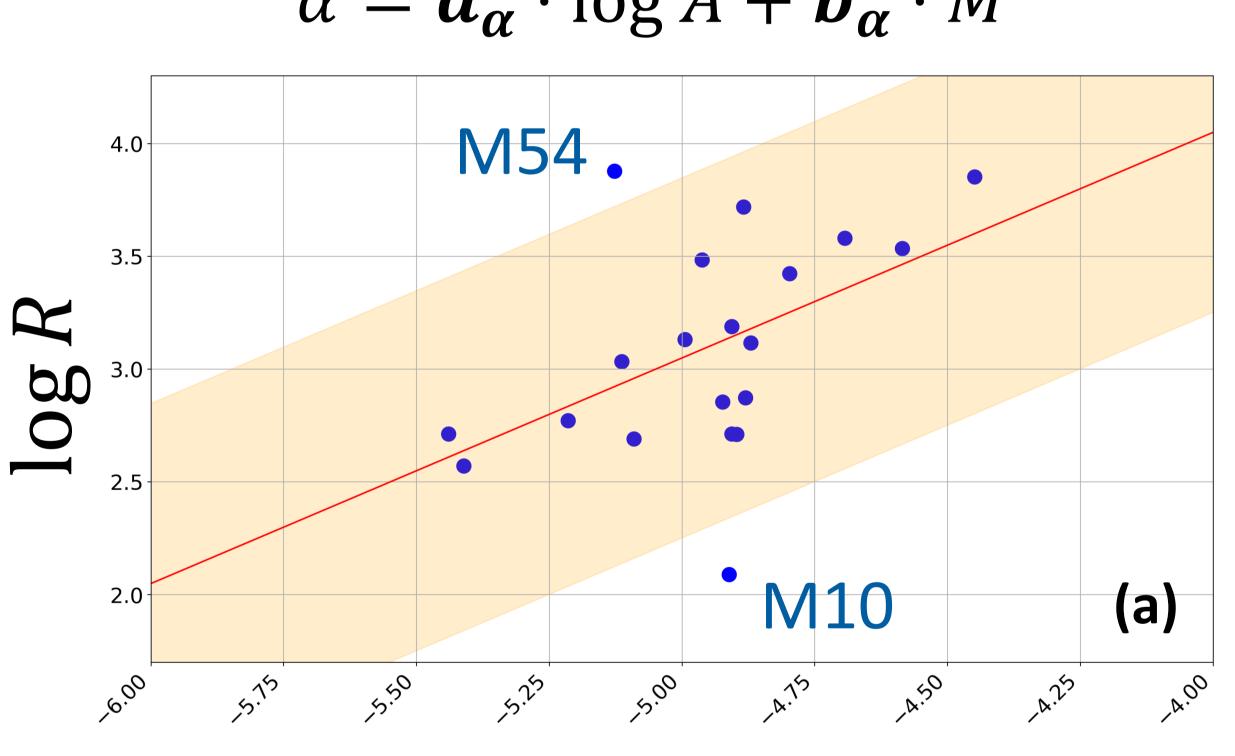


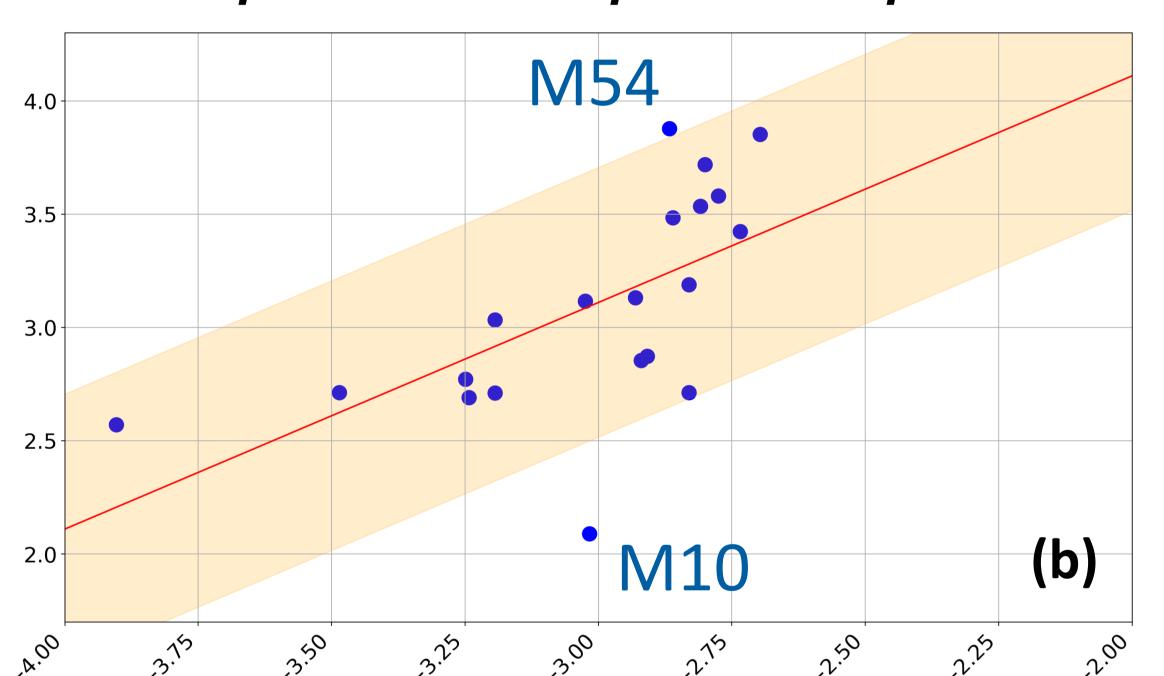
Plots of (a) $\log R$ vs. $\log A$, (b) $\log R$ vs. M, and (c) $\log R$ vs. $\log r$. Each blue dot represents a globular cluster. Age and metallicity are Figure 5 negatively correlated to the membership ratio, while radius is positively correlated to it.

 $\alpha = \boldsymbol{a}_{\alpha} \cdot \log A + \boldsymbol{b}_{\alpha} \cdot M$

$$\beta = a_{\beta} \cdot \log A + b_{\beta} \cdot M + c_{\beta} \cdot \log r$$







Plots of (a) $\log R$ vs. α and (b) $\log R$ vs. β . Each blue dot represents a globular cluster. Figure 6 The slope is normalized to 1. Most clusters fall inside the 95% confidence interval.

- The dots in the plot of log R vs. β is more concentrated than in the plot of $\log R$ vs. α .
- The area of the 95% confidence interval in the plot of $\log R$ vs. β is 25% smaller.
- The correlation between $\log R$ and β is greater than that between $\log R$ and α , which means radius is an essential factor in understanding star cluster evolution.
- Clusters M54 and M10 have a high and low Rrespectively.

Table 1 Optimal coefficients and correlation coefficient between α , β and $\log R$.

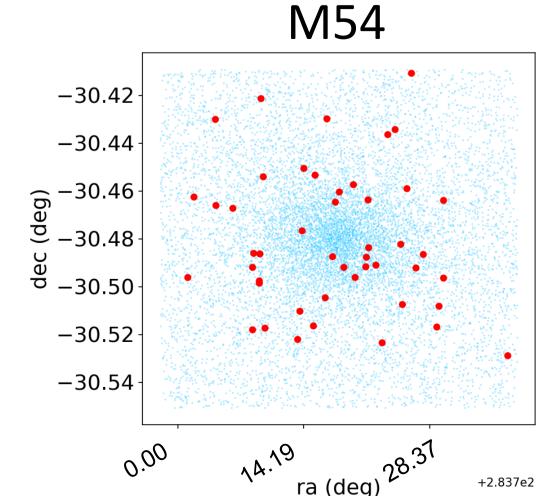
Quantity	\boldsymbol{a}	b	C	Correlation Coefficient	
α	-6.26	-0.37	_	0.501	
β	-7.11	-0.21	1.11	0.613	

Relative significance of $\log A$, $\log r$ and M. Relative significance is estimated by Table 2 the product of a parameter's coefficient in β and its median value.

Parameter	Value Range	Median Value	Coefficient in β	Relative Significance
log A	0.978~1.152	1.08	-7.11	~1
$\log r$	0.681~2.185	1.77	1.11	~0.26
M	-2.37~-0.95	-1.51	-0.21	~0.04

Interpretations

High R: M54 Cluster

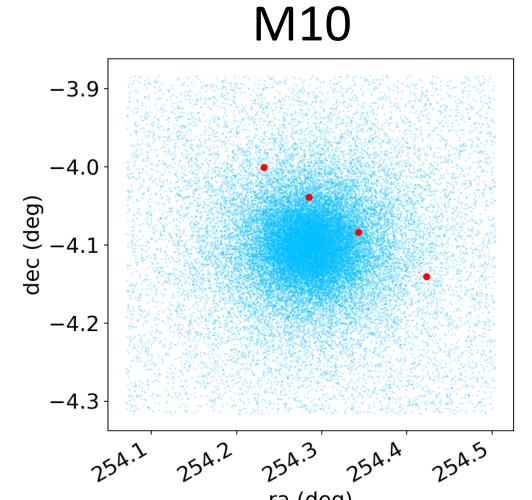


Red dots: RRLs

M54 has a high R:

- M54 belongs to the Sagittarius Dwarf Galaxy while others are in the Milky Way.
- The formation of RRLs may be influenced by its home galaxy.

Low R: M10 Cluster



Red dots: RRLs

M10 has a significantly small R. In agreement with past research [1][2]:

- There may be variations on its Red Giant Branch evolution [2].
- M10 may have an unique mass loss due to collision with another cluster.

[Fe/H] and the Instability Strip

Negative correlation of membership ratio of RRLs with [Fe/H] can be explained with the instability strip:

- The instability strip is narrower when the metallicity is higher [3].
- Therefore less variable stars populate the instability strip, causing a smaller R.

Table 3 Parameters and weights of previous result and this research.

	Previous Result [4]			This Work		
Parameter	\boldsymbol{A}	M	7	\boldsymbol{A}	M	7
Weight	= 1	2	NA	= 1	3	2

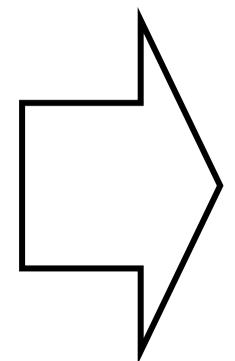
NA: Not Applicable A: Age M: Metallicity r: Half-Light Radius

Tidal force ∝ Radius

RRL membership ratio has **positive correlation** with radius

Mass-loss plays a role in the formation of RRLs [2]

Tidal force influences mass loss of GC



The formation of RRLs may be correlated with tidal forces.

Conclusions

- 20 globular clusters were analyzed using GAIA Data Release 3.
- I found that **radius** is a key factor that must be considered in understanding star cluster evolution. The impact of radius is mainly from the **mass-loss** and **tidal forces**.
- The instability strip explains how metallicity affects the RR Lyrae membership ratio.
- In addition to age and metallicity, I found that **radius** is even more essential than metallicity in analyzing the membership ratio of RR Lyrae stars.

Future Prospects

- Similar analyses could be conducted on open clusters, given that member stars can be properly distinguished from background and foreground stars.
- Applying this method to consider the effect from radius to other star clusters.

References

- [1] K. Braun, M. Mateo, K. Chiboucas, A. Athey, and D. Hurley-Keller, "Photometry Results for the Globular Clusters M10 and M12: Extinction Maps, Color-Magnitude Diagrams, and Variable Star Candidates," *Astron J.*, 124(4), 2067–2082, 2002.
- [2] A. Ferro *et al.*, "The globular cluster M10: reassessment of stellar membership, distance, and age using its variable and HB stars," *Mon Not R Astron Soc*, 499(3), 4026–4039, 2020.
- [3] P. Demarque, R. Zinn, Y.-W. Lee, and S. Yi, "The Metallicity Dependence of RR Lyrae Absolute Magnitudes from Synthetic Horizontal-Branch Models," *Astron J.*, 119(3), 1398, 2000.
- [4] R. Gratton, A. Bragaglia, E. Carretta, V. D'Orazi, S. Lucatello, and A. Sollima, "What is a globular cluster? An observational perspective," *Astron Astrophys Rev.*, 27(1), 1–136, 2019.