546.1.1 546 summany 1

Good. Focusing on shake space nodels (SSMs) summerze the doodlopment from sequential importance sompling to anothery postule. Ellow.

Covered setting

SSM, Morkey model for state xt, xt, xt, s)

state Xt | Xt, = xt, ~ p (xt | xt, | 0)

wensue out t | Xt = xt ~ p (xt | xt, | 0)

Typically two distributions of interest

filleng distribution p (xt | x, t, 0)

joint filleng distribution p (xt | x, t, 0)

The lads that p(xo; y|0) = p (xy | xy, t, 0)

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The lads that p(xo; y|0) = p (xy | xy, t, 0) p(xo|0) p(xo; y|0) = 11 p (xt | xt, y, 0) p(xo|0) p(xo; y|0)

p(x+1, | y=1,0) = S ρ(x+1, x+ | y,1, | σ)dx= = S ρ(x+1 | x+ρ)ρ(x+ | y,1,ρ)dx+

(0, 1-4 | x, 1-1, 0) = (x+1 | x | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x, 1 | x, 1-1, 0) = (x+ | x

Additionally: (and powerless from now or) $\rho(x_0, x_1, \chi_1, y_2) = \rho(x_1, \chi_2 + |x_0, y_2, |\chi_1, y_2, |) \rho(x_2 + |\chi_1, y_2, |) \rho(x_2 + |\chi_1, y_2, |) \rho(x_2 + |\chi_2, y_2, |) \rho(x_2 + |\chi_2, y_2, |) \rho(x_2 + |\chi_2, |\chi_2, |) = \rho(x_2 + |\chi_2, |\chi$

Sout filled & Lechon

p(x1; 1 | x1; 1) = p(x1; 1, x1 | x1; 1) = p(x1; 1, x1 | x1; 1) = p(x1; 1, x1 | x1; 1) = p(x1 | x1; 1) =

The joint filtering distribution has a some chot casion secursion than the filtery distribution

unomelized density and I is the nomelisation constant, (et #(x) = 8(x) , Mare # is a golf, & is the By clossing an appropriate proposal classify or Important sampling Le com orponxionele

= /2 S P(K) · J(K) · M(K) dx ETET3 = 2 5 9(x) x(x) dx =

It also holds that 2 = 5 w(x)y, (x)dx.

There integuls and be solved via Monte Carlo methods by replacing of (x) by 2 & Exi(x) where X' ~ y(x).

This Recolo to

E+C+3 = 2 & f(xi) ~ (xi) and

2 ~ 2 ~ (xi).
Self-normalising IS. Replace & by approximation

[f] & Z S(x') P(x') (nonnelized)
whose S(x')= Z S(x') (nonnelized)

p(x+ 1x12) & p(x+ 1x+) (p(x+ 1x+1) p(x+1 1/x+1) dx+1 Replace p(x0) ~ p(x,1x,1) = wo p(x,1xo). Here: 8,1(x,) of p(x,1|x,1) 2 20 p(x,1|x0) We want to use the secursive propart of Applying this idea to police by it): (1) p(x0 | x1,0) = p(x0) = 20(x0) the tough downity;

(hoose proposed m_1 , then $\omega_{\lambda} = \frac{\chi_{\lambda}(x_{\lambda})}{\chi_{\lambda}(x_{\lambda})} \quad \text{there} \quad \chi_{\lambda} \sim \chi_{\lambda}(\cdot)$ $\text{the coin closse } \chi_{\lambda}(x_{\lambda}) = \frac{N}{2} \widetilde{\omega}_{\delta} \, \rho(x_{\lambda}|x_{\delta}).$ That, bowers, is known as the boolship This introduces terempty and propagation. pendide filler. Applying the IS idea to SMC. 1.3

the joint filting distribution: p(xxx | xxx)

Ty to make use of recursion again:

p(xxx | xxx) & p(xx | xxx) p(xxxxx)

1) $p(x_0, | x_0) = p(x_0)$, given

Choose $n_0(x_0) = p(x_0)$ then $p(x_0) = \sum_{i \ge 1} z_i \delta_{x_i}(x_0)$ δ_i , now all sed wights

2) p(xo;1 | x;1) & p(x,1x,1) p(x,1x0) p(x0) Assume m, (xo;1) = m(x,1x0) vo(x0)

but re-using the existing policities) $\rho(x_0)$ $\rho(x_0)$

In good! If for all and (xul xu-1) 72 mm (xo; n-1)

Hen wi = P(xul xi) p(xil | xu-1)

Hen wi = P(xul xi) p(xil | xu-1)

= xu(xil | xi|)

= xu(xii | xi|)

As we have soen, this look to the degenerary of the wights: Most of them almost zone and only one or very few close to 1.

Irobben: Wi = &u (x,,, x,) uis

Resompting from Exiters & according to of Enry our customer

that Exercis is approximately climbiled as $p(x_0, ..., | x_{in-1}), in kad of the registed somple 1001, xoin.]$ Somple then xi ~ m(xx | xoin.). We get that $(x_0, x_{in}, x_i) ~ m(xx | x_0, x_{in}). We get that
<math display="block">(x_0, x_{in}, x_i) ~ m(xx | x_0, x_{in}) p(x_{in} | x_{in}).$ This baste to p(yx | xi) p(xi | xoin) $m(x_i | x_i) = m(x_i | x_i).$ This gets tid of win.

This algorithm is some times called

We arrived at a matural SUC.1.4

proposal for the filtering problem, that lead to the travel filter and already contained recomply to the complete filter and already contained to the case of the joint filtering problem we had to introduce another step, the recompling step,

In case of the joint filtering problem, we inhoduced a posempling step as a Cat(1 wint) and used

the proposed yn(xoin) = yn(xulxun) p(xoinn | ynun)

i.e. xi ~ m.(| xun) p(xoinn | ynun)

Mehing the resempting explicit, re got m (xo:u, au) = m (xn | an) p(an) = = mu(xn | xnm) p(xo:nm) p (xo:nm) · win

is a proposed for p (xu | xu) p (xu | xun) p (au).

p (xo, u, ou | xy, u) a p (yu | xu) p (xu | xun) p (u).

Alles some non greatly in the proposed for the MPF:

and in SIR.

nu (xen, an) = nu (xu | xun) cun p(xen, | xun)

We Rengol for the ren weights popularily place | xil) | xil) place | xil) |

This makes the partide fill alonghus used to downty exactly equal. as well as the joint filling

Exemple Teathole Filter
Choose vin x win p(xh | xhin) | i= 1,-, N

The win = 2 for all in 1, N and all is

Then win = 2 for all is 1,-, N and all is

The glang poly (xu, ouly, un) p(xu, ouly, un) = = p(xu, xu) p(xu, ouly, un) = = p(xu, xu) p(xu, xu, ouly, un) p(xu, xu, ouly, un) = = p(xu, xu) p(xu, xu, ouly, un) p(xu, xu, ouly, un) = = p(xu, xu) p(xu, xu, ouly, un) p(xu, xu, ouly, un) p(xu, xu, ouly, un) p(xu, xu, ouly, un) p(xu, xu, ouly, ouly, un) p(xu, xu, ouly, ouly,

The idea baland the arrivary particle filts is to incoposate the arcestor intex into the postlem and to antone
that we can close past stoke only from the analaste

over, thus bailing to a shyldly differed drups distribution

For large N both thould salve the same postlem.