Table 1: Parameter estimates for the N-N and Semi-N distributional models when $N=50, T=3, C=5, \sigma_{LS}=0,$ and $\sigma_e^2=0.1$

| | | | - 10 | L | | | | | | | | |
|---------------|--------|--------|--------|-------|-------|-------|--------|--------|----------|-------|-------|-------|
| | | | N-N m | odel | | | | | Semi-N ı | model | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.196 | -0.004 | -0.067 | 0.138 | 0.019 | 0.970 | 6.196 | -0.004 | -0.069 | 0.136 | 0.018 | 0.975 |
| β_{S} | 0.296 | -0.004 | -1.379 | 0.054 | 0.003 | 0.955 | 0.296 | -0.004 | -1.343 | 0.053 | 0.003 | 0.965 |
| σ_L^2 | 1.048 | 0.048 | 4.769 | 0.209 | 0.046 | 0.960 | 1.042 | 0.042 | 4.215 | 0.207 | 0.045 | 0.955 |
| σ_S^2 | 0.137 | 0.037 | 37.063 | 0.040 | 0.003 | 0.955 | 0.134 | 0.034 | 33.680 | 0.025 | 0.002 | 0.960 |
| σ_{LS} | -0.009 | -0.009 | -0.896 | 0.054 | 0.003 | 0.990 | -0.007 | -0.007 | -0.675 | 0.053 | 0.003 | 0.995 |
| σ_e^2 | 0.099 | -0.001 | -0.933 | 0.181 | 0.033 | 0.355 | 0.102 | 0.002 | 2.212 | 0.203 | 0.041 | 0.355 |
| K_e | - | - | - | - | - | - | 3.662 | - | - | 0.222 | - | - |
| α | - | - | - | - | - | - | 0.999 | -0.001 | -0.127 | 0.003 | 0.000 | 1.000 |

Table 2: Parameter estimates for the N-N and N-Semi distributional models when $N=50, T=3, C=5, \sigma_{LS}=0,$ and $\sigma_e^2=0.1$

| | | | N-N mo | odel | | | | | N-Semi ı | nodel | | |
|----------------------------|-----------------|-----------------|------------------|----------------|------------------|----------------|-----------------|-----------------|-----------------|------------------|------------------|----------------|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| $-\beta_L$ | 6.203 | 0.003 | 0.044 | 0.128 | 0.016 | 0.965 | 6.204 | 0.004 | 0.066 | 0.120 | 0.014 | 0.975 |
| β_S | 0.299 | -0.001 | -0.218 | 0.052 | 0.003 | 0.980 | 0.298 | -0.002 | -0.666 | 0.050 | 0.002 | 0.985 |
| σ_L^2 | 0.906 | -0.094 | -9.393 | 1.425 | 2.040 | 0.275 | 0.868 | -0.132 | -13.170 | 1.395 | 1.964 | 0.130 |
| $\sigma_S^2 \ \sigma_{LS}$ | 0.123 -0.031 | 0.023 -0.031 | 23.152 -3.055 | 0.086 0.196 | $0.008 \\ 0.039$ | 0.865 0.710 | 0.104 -0.032 | 0.004 -0.032 | 3.731 -3.208 | $0.086 \\ 0.192$ | $0.007 \\ 0.038$ | 0.530 0.505 |
| σ_e^2 | 0.097 | -0.003 | -3.085 | 0.017 | 0.000 | 0.910 | 0.096 | -0.004 | -4.371 | 0.016 | 0.000 | 0.915 |
| K_u | - | - | - | - | - | - | 1.892 | - | - | 0.491 | - | - |
| α | - | - | - | - | - | - | 0.978 | -0.022 | -2.214 | 0.006 | 0.001 | 1.000 |

Table 3: Parameter estimates for the N-N and Semi-Semi distributional models when $N=50, T=3, C=5, \sigma_{LS}=0,$ and $\sigma_e^2=0.1$

| | | | N-N me | odel | | | | | Semi-Sem | i model | | |
|-----------------------------|--------|--------|---------|-------|-------|-------|--------|--------|----------|---------|-------|-------|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.187 | -0.013 | -0.203 | 0.127 | 0.016 | 0.961 | 6.200 | 0.000 | -0.003 | 0.111 | 0.012 | 0.955 |
| β_S | 0.293 | -0.007 | -2.320 | 0.054 | 0.003 | 0.978 | 0.294 | -0.006 | -2.083 | 0.049 | 0.002 | 0.985 |
| σ_L^2 | 0.965 | -0.035 | -3.503 | 1.144 | 1.310 | 0.328 | 0.929 | -0.071 | -7.137 | 1.095 | 1.203 | 0.090 |
| $\sigma_S^{\overline{2}}$ | 0.131 | 0.031 | 30.850 | 0.091 | 0.009 | 0.728 | 0.109 | 0.009 | 8.848 | 0.090 | 0.008 | 0.365 |
| σ_{LS} | -0.005 | -0.005 | -0.463 | 0.198 | 0.039 | 0.694 | -0.007 | -0.007 | -0.656 | 0.186 | 0.035 | 0.435 |
| $\overset{\sigma_e^2}{K_e}$ | 0.088 | -0.012 | -12.113 | 0.068 | 0.005 | 0.294 | 0.086 | -0.014 | -13.910 | 0.063 | 0.004 | 0.305 |
| | - | - | - | - | - | - | 3.651 | - | - | 0.202 | - | - |
| K_u | - | - | - | - | - | - | 1.956 | - | - | 0.520 | - | - |
| α_1 | - | - | - | - | - | - | 0.999 | -0.001 | -0.136 | 0.003 | 0.000 | 1.000 |
| α_2 | - | - | - | - | - | - | 0.979 | -0.021 | -2.147 | 0.006 | 0.000 | 1.000 |

Table 4: Parameter estimates for the N-N and Semi-N distributional models when $N=50, T=5, C=5, \sigma_{LS}=0,$ and $\sigma_e^2=0.5$

| | | | - 10 | L | | | | | | | | |
|---------------|--------|--------|--------|-------|-------|-------|--------|--------|----------|-------|-------|-------|
| | | | N-N m | odel | | | | | Semi-N 1 | nodel | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.180 | -0.020 | -0.325 | 0.165 | 0.028 | 0.950 | 6.181 | -0.019 | -0.307 | 0.163 | 0.027 | 0.945 |
| β_S | 0.304 | 0.004 | 1.247 | 0.052 | 0.003 | 0.975 | 0.302 | 0.002 | 0.737 | 0.051 | 0.003 | 0.970 |
| σ_L^2 | 1.048 | 0.048 | 4.768 | 0.263 | 0.071 | 0.960 | 1.049 | 0.049 | 4.901 | 0.260 | 0.070 | 0.960 |
| σ_S^2 | 0.141 | 0.041 | 41.475 | 0.030 | 0.003 | 0.930 | 0.140 | 0.040 | 39.527 | 0.027 | 0.002 | 0.920 |
| σ_{LS} | -0.014 | -0.014 | -1.357 | 0.063 | 0.004 | 0.975 | -0.011 | -0.011 | -1.056 | 0.058 | 0.004 | 0.970 |
| σ_e^2 | 0.552 | 0.052 | 10.376 | 0.903 | 0.819 | 0.235 | 0.545 | 0.045 | 8.942 | 0.876 | 0.769 | 0.170 |
| K_e | - | - | - | - | - | - | 3.782 | - | - | 0.322 | - | - |
| α | - | - | - | - | - | - | 1.000 | 0.000 | 0.030 | 0.004 | 0.000 | 1.000 |

Table 5: Parameter estimates for the N-N and N-Semi distributional models when $N=50, T=5, C=5, \sigma_{LS}=0,$ and $\sigma_e^2=0.5$

| | | | N-N m | odel | | | | | N-Semi | model | | |
|-----------------------------------------|-----------------|-----------------|------------------|----------------|----------------|----------------|-----------------|-----------------|------------------|----------------|----------------|----------------|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.218 | 0.018 | 0.295 | 0.185 | 0.034 | 0.950 | 6.208 | 0.008 | 0.127 | 0.139 | 0.019 | 0.945 |
| β_S | 0.301 | 0.001 | 0.337 | 0.053 | 0.003 | 0.975 | 0.297 | -0.003 | -1.055 | 0.049 | 0.002 | 0.975 |
| σ_L^2 | 1.365 | 0.365 | 36.525 | 7.423 | 55.238 | 0.330 | 1.324 | 0.324 | 32.350 | 7.276 | 53.048 | 0.215 |
| $\sigma_S^{\overline{2}} \ \sigma_{LS}$ | 0.158 -0.001 | 0.058 -0.001 | 58.039 -0.097 | 0.341 0.799 | 0.120 0.639 | 0.855 0.765 | 0.138 -0.005 | 0.038 -0.005 | 37.758 -0.504 | 0.335 0.782 | 0.114 0.612 | 0.520 0.555 |
| σ_e^2 | 0.490 | -0.010 | -2.023 | 0.058 | 0.003 | 0.930 | 0.487 | -0.013 | -2.529 | 0.057 | 0.003 | 0.925 |
| K_u^c | - | - | - | - | - | - | 1.891 | - | - | 0.487 | - | - |
| α | - | - | - | - | - | - | 0.978 | -0.022 | -2.228 | 0.006 | 0.001 | 1.000 |

Table 6: Parameter estimates for the N-N and Semi-Semi distributional models when

 $N = 50, T = 5, C = 5, \sigma_{LS} = 0, \text{ and } \sigma_e^2 = 0.5$

| | | | N-N m | odel | | | | | Semi-Sem | i model | | |
|--------------------------------|----------------|------------------|------------------|----------------|----------------|----------------|----------------|------------------|------------------|----------------|----------------|----------------|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.191 0.298 | -0.009 -0.002 | -0.143 -0.818 | 0.164 0.057 | 0.027 0.003 | 0.950 0.985 | 6.192 0.298 | -0.008 -0.002 | -0.127 -0.537 | 0.139 0.048 | 0.019 0.002 | 0.955 0.980 |
| $\frac{\beta_S}{\sigma_L^2}$ | 1.123 | 0.123 | 12.272 | 2.066 | 4.284 | 0.983 | 1.078 | 0.078 | 7.781 | 2.023 | 4.098 | 0.980 |
| σ_S^2 | 0.145 | 0.045 | 44.530 | 0.260 | 0.070 | 0.755 | 0.123 | 0.023 | 22.847 | 0.256 | 0.066 | 0.360 |
| $\sigma_{LS} \over \sigma_e^2$ | 0.039 0.463 | 0.039 -0.037 | 3.932 -7.453 | 0.636 0.373 | 0.406 0.140 | 0.750 0.185 | 0.038 0.457 | 0.038 -0.043 | 3.789 -8.663 | 0.621 0.365 | 0.387 0.135 | 0.525 0.145 |
| K_e | - | - | - | - | - | - | 3.734 | - | - | 0.309 | - | - |
| K_u α_1 | - | - | - | - | - | - | 1.882 1.000 | 0.000 | -0.025 | 0.494 0.004 | 0.000 | 1.000 |
| α_2 | - | - | - | - | - | - | 0.978 | -0.022 | -2.197 | 0.006 | 0.001 | 1.000 |

Table 7: Parameter estimates for the N-N and Semi-N distributional models when ${\cal N}=$

 $200, T = 3, C = 5, \sigma_{LS} = 0, \text{ and } \sigma_e^2 = 0.5$

| , | - , - | -,- | LD -, | | 5 | | | | | | | |
|---------------|--------|--------|---------|-------|-------|-------|--------|--------|----------|-------|-------|-------|
| - | | | N-N m | odel | | | | | Semi-N 1 | nodel | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.203 | 0.003 | 0.049 | 0.081 | 0.007 | 0.950 | 6.204 | 0.004 | 0.065 | 0.078 | 0.006 | 0.955 |
| β_S | 0.297 | -0.003 | -0.927 | 0.038 | 0.001 | 0.955 | 0.297 | -0.003 | -0.835 | 0.036 | 0.001 | 0.955 |
| σ_L^2 | 1.030 | 0.030 | 3.017 | 0.144 | 0.022 | 0.925 | 1.029 | 0.029 | 2.875 | 0.140 | 0.020 | 0.930 |
| σ_S^2 | 0.130 | 0.030 | 30.379 | 0.032 | 0.002 | 0.925 | 0.129 | 0.029 | 29.027 | 0.029 | 0.002 | 0.935 |
| σ_{LS} | -0.014 | -0.014 | -1.406 | 0.048 | 0.002 | 0.960 | -0.013 | -0.013 | -1.339 | 0.043 | 0.002 | 0.955 |
| σ_e^2 | 0.384 | -0.116 | -23.280 | 0.291 | 0.098 | 0.140 | 0.385 | -0.115 | -23.015 | 0.293 | 0.099 | 0.125 |
| K_e | - | - | - | - | - | - | 4.295 | - | - | 0.238 | - | - |
| α | - | - | - | - | - | - | 0.999 | -0.001 | -0.105 | 0.005 | 0.000 | 1.000 |

Note. Est.: estimate; AB: absolute bias; RB: relative bias; SE: standard error; MSE: mean square error; CP: coverage probability.

Table 8: Parameter estimates for the N-N and N-Semi distributional models when $N = \frac{1}{2} \frac{2}{3} \frac{1}{3} \frac$

 $200, T = 3, C = 5, \sigma_{LS} = 0, \text{ and } \sigma_e^2 = 0.5$

| | | | N-N mo | odel | | | | | N-Semi ı | nodel | | |
|----------------------------------------|-------|--------|------------------|----------------|------------------|----------------|-----------------|-----------------|------------------|----------------|----------------|----------------|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.203 | 0.003 | 0.048 | 0.073 | 0.005 | 0.960 | 6.202 | 0.002 | 0.024 | 0.070 | 0.005 | 0.965 |
| β_{S} | 0.298 | -0.002 | -0.643 | 0.042 | 0.002 | 0.950 | 0.298 | -0.002 | -0.550 | 0.043 | 0.002 | 0.955 |
| σ_{τ}^{2} | 0.823 | -0.177 | -17.653 | 0.837 | 0.731 | 0.160 | 0.823 | -0.177 | -17.704 | 0.834 | 0.727 | 0.120 |
| $\sigma_S^{\frac{L}{2}}$ σ_{LS} | 0.135 | 0.035 | 34.916 -4.030 | 0.075 0.173 | $0.007 \\ 0.032$ | 0.845 0.650 | 0.140 -0.048 | 0.040 -0.048 | 39.809 -4.796 | 0.079 0.170 | 0.008 0.031 | 0.800 0.540 |
| σ_e^2 | 0.469 | -0.031 | -6.252 | 0.041 | 0.003 | 0.850 | 0.464 | -0.036 | -7.205 | 0.040 | 0.003 | 0.835 |
| K_u | - | - | - | - | - | - | 2.494 | - | - | 0.582 | - | - |
| α | - | - | - | - | - | - | 0.972 | -0.028 | -2.777 | 0.008 | 0.001 | 1.000 |

Table 9: Parameter estimates for the N-N and Semi-Semi distributional models when $N=200,\,T=3,\,C=5,\,\sigma_{LS}=0,$ and $\sigma_e^2=0.5$

| | | | N-N m | odel | | | | | Semi-Sem | i model | | |
|------------------------------|--------|--------|---------|-------|-------|-------|--------|--------|----------|---------|-------|-------|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.199 | -0.001 | -0.017 | 0.083 | 0.007 | 0.915 | 6.201 | 0.001 | 0.020 | 0.080 | 0.006 | 0.920 |
| β_S | 0.300 | 0.000 | 0.125 | 0.040 | 0.002 | 0.970 | 0.301 | 0.001 | 0.226 | 0.037 | 0.001 | 0.975 |
| $\frac{\beta_S}{\sigma_L^2}$ | 0.830 | -0.170 | -16.965 | 1.039 | 1.108 | 0.140 | 0.824 | -0.176 | -17.586 | 1.031 | 1.093 | 0.075 |
| σ_S^2 | 0.136 | 0.036 | 35.757 | 0.087 | 0.009 | 0.760 | 0.137 | 0.037 | 37.021 | 0.089 | 0.009 | 0.690 |
| σ_{LS} | -0.019 | -0.019 | -1.855 | 0.198 | 0.040 | 0.570 | -0.023 | -0.023 | -2.252 | 0.196 | 0.039 | 0.515 |
| σ_e^2 | 0.516 | 0.016 | 3.113 | 0.574 | 0.330 | 0.125 | 0.511 | 0.011 | 2.163 | 0.576 | 0.332 | 0.095 |
| K_e | - | - | - | - | - | - | 4.321 | - | - | 0.257 | - | - |
| K_u | - | - | - | - | - | - | 2.639 | - | - | 0.580 | - | - |
| α_1 | - | - | - | - | - | - | 1.000 | 0.000 | -0.037 | 0.005 | 0.000 | 1.000 |
| α_2 | - | - | - | - | - | - | 0.974 | -0.026 | -2.572 | 0.008 | 0.001 | 1.000 |

Table 10: Parameter estimates for the N-N and Semi-N distributional models when $N=200, T=5, C=5, \sigma_{LS}=0,$ and $\sigma_e^2=0.1$

AB 0.006 RB (% 0.090 SE 0.075 MSE 0.006 RB (%) Est 0.005 0.955 0.076 0.955 6.205 0.300 eta_L^S eta_S^S eta_L^S eta_L^S eta_L^S eta_L^S 0.079 0.006 6.206 0.000 0.024 0.001 0.950 0.300 0.000 0.144 0.024 0.001 0.950 0.113 1.011 1.107 0.011 0.960 1.013 0.013 1.255 0.105 0.011 0.960 0.011 0.105 0.940 0.960 0.107 7.192 -0.413 0.000 0.001 0.007 -0.004 7.132 -0.392 0.011 0.000 0.955 0.107 -0.004 0.007 0.011 0.025 0.001 0.970 -0.004 0.025 0.107 0.007 7.037 0.152 0.023 0.140 0.107 0.007 6.982 0.151 0.023 0.095 4.262 0.999 0.309 0.006 -0.001 -0.139 0.000 1.000

Table 11: Parameter estimates for the N-N and N-Semi distributional models when $N=200,\,T=5,\,C=5,\,\sigma_{LS}=0,$ and $\sigma_e^2=0.1$

| | | | N-N mo | odel | | | | | N-Semi ı | nodel | | |
|---------------------------|--------|--------|--------|-------|-------|-------|--------|--------|----------|-------|-------|-------|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.196 | -0.004 | -0.065 | 0.079 | 0.006 | 0.930 | 6.202 | 0.002 | 0.024 | 0.058 | 0.003 | 0.940 |
| β_S | 0.298 | -0.002 | -0.516 | 0.022 | 0.000 | 0.960 | 0.298 | -0.002 | -0.552 | 0.019 | 0.000 | 0.965 |
| σ_L^2 | 1.026 | 0.026 | 2.640 | 3.017 | 9.103 | 0.140 | 1.018 | 0.018 | 1.814 | 3.005 | 9.028 | 0.055 |
| $\sigma_S^{\overline{2}}$ | 0.095 | -0.005 | -4.958 | 0.130 | 0.017 | 0.210 | 0.090 | -0.010 | -9.618 | 0.130 | 0.017 | 0.080 |
| σ_{LS} | -0.027 | -0.027 | -2.748 | 0.349 | 0.122 | 0.270 | -0.028 | -0.028 | -2.838 | 0.347 | 0.121 | 0.145 |
| σ_e^2 | 0.099 | -0.001 | -0.532 | 0.006 | 0.000 | 0.935 | 0.099 | -0.001 | -0.719 | 0.006 | 0.000 | 0.925 |
| K_u | - | - | - | - | - | - | 2.410 | - | - | 0.594 | - | - |
| α | - | - | - | - | - | - | 0.974 | -0.026 | -2.582 | 0.008 | 0.001 | 1.000 |

Table 12: Parameter estimates for the N-N and Semi-Semi distributional models when $N=200, T=5, C=5, \sigma_{LS}=0,$ and $\sigma_e^2=0.1$

| | | | . 1 | | | | | | | | | |
|---------------------------|--------|--------|---------|-------|-------|-------|--------|--------|----------|---------|-------|-------|
| | | | N-N me | odel | | | | | Semi-Sem | i model | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.197 | -0.003 | -0.054 | 0.070 | 0.005 | 0.960 | 6.197 | -0.003 | -0.047 | 0.061 | 0.004 | 0.970 |
| β_S | 0.297 | -0.003 | -1.004 | 0.023 | 0.001 | 0.965 | 0.297 | -0.003 | -0.936 | 0.020 | 0.000 | 0.975 |
| σ_L^2 | 0.883 | -0.117 | -11.695 | 1.002 | 1.017 | 0.145 | 0.874 | -0.126 | -12.638 | 0.997 | 1.009 | 0.065 |
| $\sigma_S^{\overline{2}}$ | 0.102 | 0.002 | 1.832 | 0.130 | 0.017 | 0.105 | 0.097 | -0.003 | -3.196 | 0.130 | 0.017 | 0.025 |
| σ_{LS} | -0.018 | -0.018 | -1.783 | 0.218 | 0.048 | 0.315 | -0.018 | -0.018 | -1.800 | 0.217 | 0.048 | 0.135 |
| σ_e^2 | 0.103 | 0.003 | 3.106 | 0.125 | 0.016 | 0.100 | 0.103 | 0.003 | 3.032 | 0.125 | 0.016 | 0.070 |
| K_e | - | - | - | - | - | - | 4.271 | - | - | 0.320 | - | - |
| K_u | - | - | - | - | - | - | 2.419 | - | - | 0.660 | - | - |
| α_1 | - | - | - | - | - | - | 0.999 | -0.001 | -0.146 | 0.006 | 0.000 | 1.000 |
| α_2 | - | - | - | - | - | - | 0.975 | -0.025 | -2.539 | 0.008 | 0.001 | 1.000 |

Table 13: Parameter estimates for the N-N and Semi-N distributional models when $N=500, T=3, C=5, \sigma_{LS}=0$, and $\sigma_{e}^{2}=0.1$

| | , | - , - | -, - L D | - , . | · · · · · e | - | | | | | | |
|---------------|--------|--------|-----------------|-------|-------------|-------|--------|--------|----------|-------|-------|-------|
| | | | N-N me | odel | | | | | Semi-N ı | nodel | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| $-\beta_L$ | 6.202 | 0.002 | 0.025 | 0.049 | 0.002 | 0.925 | 6.202 | 0.002 | 0.029 | 0.049 | 0.002 | 0.925 |
| β_S | 0.302 | 0.002 | 0.613 | 0.017 | 0.000 | 0.955 | 0.302 | 0.002 | 0.526 | 0.017 | 0.000 | 0.960 |
| σ_L^2 | 1.005 | 0.005 | 0.491 | 0.077 | 0.006 | 0.935 | 1.006 | 0.006 | 0.644 | 0.078 | 0.006 | 0.930 |
| σ_S^2 | 0.105 | 0.005 | 5.098 | 0.010 | 0.000 | 0.950 | 0.105 | 0.005 | 4.914 | 0.010 | 0.000 | 0.945 |
| σ_{LS} | -0.001 | -0.001 | -0.079 | 0.018 | 0.000 | 0.960 | -0.001 | -0.001 | -0.071 | 0.018 | 0.000 | 0.960 |
| σ_e^2 | 0.101 | 0.001 | 0.831 | 0.119 | 0.014 | 0.170 | 0.101 | 0.001 | 0.777 | 0.118 | 0.014 | 0.150 |
| K_e | - | - | - | - | - | - | 4.544 | - | - | 0.212 | - | - |
| α | - | - | - | - | - | - | 0.999 | -0.001 | -0.119 | 0.006 | 0.000 | 1.000 |

Table 14: Parameter estimates for the N-N and N-Semi distributional models when $N=500,\, T=3,\, C=5,\, \sigma_{LS}=0,$ and $\sigma_e^2=0.1$

| - | , | -, - | - , - DL | , -, | · · · · · · · · · · · · · · · · · · · | _ | | | | | | |
|-----------------------------------------|------------------|------------------|----------------|----------------|---------------------------------------|----------------|----------------|----------------|----------------|----------------|------------------|----------------|
| | | | N-N m | odel | | | | | N-Semi | model | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.199 | -0.001 | -0.011 | 0.038 | 0.001 | 0.980 | 6.197 | -0.003 | -0.043 | 0.034 | 0.001 | 0.970 |
| β_{S} | 0.302 | 0.002 | 0.580 | 0.017 | 0.000 | 0.920 | 0.302 | 0.002 | 0.581 | 0.016 | 0.000 | 0.940 |
| σ_L^2 | 0.947 | -0.053 | -5.341 | 1.731 | 3.000 | 0.120 | 0.946 | -0.054 | -5.403 | 1.731 | 2.999 | 0.075 |
| $\sigma_S^{\overline{2}} \ \sigma_{LS}$ | $0.108 \\ 0.011$ | $0.008 \\ 0.011$ | 8.233 1.053 | 0.160 0.403 | $0.026 \\ 0.162$ | 0.175 0.340 | 0.109 0.009 | 0.009 0.009 | 8.734 0.852 | 0.160 0.402 | $0.026 \\ 0.162$ | 0.140 0.245 |
| σ_e^2 | 0.097 | -0.003 | -2.803 | 0.006 | 0.000 | 0.915 | 0.096 | -0.004 | -3.980 | 0.005 | 0.000 | 0.870 |
| K_u | - | - | - | - | - | - | 2.895 | - | - | 0.631 | - | - |
| α | - | - | - | - | - | - | 0.972 | -0.028 | -2.839 | 0.010 | 0.001 | 1.000 |

Table 15: Parameter estimates for the N-N and Semi-Semi distributional models when $N=500, T=3, C=5, \sigma_{LS}=0,$ and $\sigma_e^2=0.1$

| | , - | ٠, ٠ | , - DL | , ,,- | е | | | | | | | |
|-------------------------|----------|--------|--------|-------|-------|-------|--------|--------|----------|---------|-------|-------|
| | | | N-N m | odel | | | | | Semi-Sem | i model | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.200 | 0.000 | 0.000 | 0.053 | 0.003 | 0.920 | 6.202 | 0.002 | 0.033 | 0.048 | 0.002 | 0.915 |
| β_S | 0.301 | 0.001 | 0.247 | 0.015 | 0.000 | 0.980 | 0.300 | 0.000 | 0.035 | 0.014 | 0.000 | 0.970 |
| $\beta_S \\ \sigma_L^2$ | 0.938 | -0.062 | -6.151 | 1.490 | 2.223 | 0.080 | 0.937 | -0.063 | -6.319 | 1.490 | 2.223 | 0.010 |
| σ_S^2 | 0.112 | 0.012 | 11.517 | 0.177 | 0.032 | 0.185 | 0.111 | 0.011 | 11.034 | 0.178 | 0.032 | 0.135 |
| σ_{LS} | s -0.008 | -0.008 | -0.848 | 0.258 | 0.067 | 0.230 | -0.010 | -0.010 | -0.957 | 0.257 | 0.066 | 0.160 |
| σ_e^2 | 0.103 | 0.003 | 2.802 | 0.089 | 0.008 | 0.085 | 0.102 | 0.002 | 1.989 | 0.089 | 0.008 | 0.080 |
| K_e | | - | - | - | - | - | 4.558 | - | - | 0.218 | - | - |
| K_u | | - | - | - | - | - | 2.904 | - | - | 0.606 | - | - |
| α_1 | - | - | - | - | - | - | 0.999 | -0.001 | -0.063 | 0.006 | 0.000 | 1.000 |
| α_2 | - | - | - | - | - | - | 0.972 | -0.028 | -2.832 | 0.009 | 0.001 | 1.000 |
| | | | | | | | | | | | | |

Table 16: Parameter estimates for the N-N and Semi-N distributional models when $N=500,\,T=5,\,C=5,\,\sigma_{LS}=0,$ and $\sigma_e^2=0.5$

| | , - | -, - | , LD | , - | e | 0.0 | | | | | | |
|---------------|--------|--------|---------|-------|-------|-------|--------|--------|----------|-------|-------|-------|
| | | | N-N m | odel | | | | | Semi-N 1 | nodel | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.207 | 0.007 | 0.106 | 0.050 | 0.003 | 0.945 | 6.208 | 0.008 | 0.121 | 0.049 | 0.003 | 0.945 |
| β_S | 0.298 | -0.002 | -0.643 | 0.017 | 0.000 | 0.970 | 0.298 | -0.002 | -0.734 | 0.016 | 0.000 | 0.955 |
| σ_L^2 | 0.991 | -0.009 | -0.865 | 0.081 | 0.007 | 0.945 | 0.994 | -0.006 | -0.637 | 0.077 | 0.006 | 0.945 |
| σ_S^2 | 0.105 | 0.005 | 4.737 | 0.010 | 0.000 | 0.930 | 0.104 | 0.004 | 4.167 | 0.008 | 0.000 | 0.955 |
| σ_{LS} | -0.003 | -0.003 | -0.255 | 0.023 | 0.001 | 0.920 | -0.002 | -0.002 | -0.242 | 0.021 | 0.000 | 0.930 |
| σ_e^2 | 0.438 | -0.062 | -12.362 | 0.402 | 0.165 | 0.060 | 0.438 | -0.062 | -12.408 | 0.400 | 0.164 | 0.035 |
| K_e | - | - | - | - | - | - | 4.564 | - | - | 0.239 | - | - |
| α | - | - | - | - | - | - | 0.999 | -0.001 | -0.107 | 0.007 | 0.000 | 1.000 |

Table 17: Parameter estimates for the N-N and N-Semi distributional models when $N=500, T=5, C=5, \sigma_{LS}=0,$ and $\sigma_e^2=0.5$

| | | | N-N mo | odel | | | | | N-Semi ı | nodel | | |
|-----------------------------------------|-----------------|------------------|-------------------|----------------|------------------|----------------|-----------------|------------------|-------------------|----------------|------------------|----------------|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.203 | 0.003 | 0.051 | 0.049 | 0.002 | 0.960 | 6.204 | 0.004 | 0.070 | 0.042 | 0.002 | 0.955 |
| β_{S} | 0.300 | 0.000 | 0.055 | 0.018 | 0.000 | 0.920 | 0.300 | 0.000 | -0.042 | 0.017 | 0.000 | 0.940 |
| σ_L^2 | 0.925 | -0.075 | -7.483 | 1.285 | 1.658 | 0.110 | 0.926 | -0.074 | -7.357 | 1.284 | 1.653 | 0.095 |
| $\sigma_S^{\overline{2}} \ \sigma_{LS}$ | 0.089 -0.014 | -0.011 -0.014 | -10.834 -1.363 | 0.091 0.252 | $0.008 \\ 0.063$ | 0.150 0.335 | 0.089 -0.017 | -0.011 -0.017 | -10.831 -1.663 | 0.092 0.251 | $0.008 \\ 0.063$ | 0.080 0.285 |
| σ_e^2 | 0.496 | -0.004 | -0.774 | 0.018 | 0.000 | 0.950 | 0.494 | -0.006 | -1.202 | 0.018 | 0.000 | 0.915 |
| K_u | - | - | - | - | - | - | 2.802 | - | - | 0.603 | - | - |
| α | - | - | - | - | - | - | 0.970 | -0.030 | -2.991 | 0.009 | 0.001 | 1.000 |

Table 18: Parameter estimates for the N-N and Semi-Semi distributional models when $N=500, T=5, C=5, \sigma_{LS}=0,$ and $\sigma_e^2=0.5$

| | | -, - | -, | , LD | ٠, | e | 0.0 | | | | | |
|---------------------------|-------|--------|---------|-------|-------|-------|-------|--------|----------|---------|-------|-------|
| | | | N-N m | odel | | | | | Semi-Sem | i model | | |
| - | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.198 | -0.002 | -0.028 | 0.043 | 0.002 | 0.955 | 6.198 | -0.002 | -0.024 | 0.038 | 0.001 | 0.960 |
| β_S | 0.301 | 0.001 | 0.252 | 0.016 | 0.000 | 0.945 | 0.301 | 0.001 | 0.338 | 0.014 | 0.000 | 0.955 |
| σ_L^2 | 0.826 | -0.174 | -17.370 | 0.955 | 0.942 | 0.095 | 0.822 | -0.178 | -17.801 | 0.948 | 0.931 | 0.050 |
| $\sigma_S^{\overline{2}}$ | 0.121 | 0.021 | 21.221 | 0.376 | 0.142 | 0.120 | 0.119 | 0.019 | 19.155 | 0.375 | 0.141 | 0.080 |
| σ_{LS} | 0.017 | 0.017 | 1.677 | 0.368 | 0.136 | 0.295 | 0.017 | 0.017 | 1.703 | 0.367 | 0.135 | 0.245 |
| σ_e^2 | 0.530 | 0.030 | 6.038 | 0.637 | 0.407 | 0.045 | 0.530 | 0.030 | 6.081 | 0.645 | 0.417 | 0.020 |
| K_e | - | - | - | - | - | - | 4.597 | - | - | 0.220 | - | - |
| K_u | - | - | - | - | - | - | 2.877 | - | - | 0.638 | - | - |
| α_1 | - | - | - | - | - | - | 1.000 | 0.000 | 0.005 | 0.007 | 0.000 | 1.000 |
| α_2 | - | - | - | - | - | - | 0.972 | -0.028 | -2.840 | 0.010 | 0.001 | 1.000 |

Table 19: Parameter estimates for the N-N and Semi-N distributional models when $N=50,\,T=3,\,C=20,\,\sigma_{LS}=0,$ and $\sigma_e^2=0.1$

| | | | N-N mo | | | | | | Semi-N 1 | | | |
|---------------------------|--------|--------|--------|-------|-------|-------|--------|--------|----------|-------|-------|-------|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.210 | 0.010 | 0.157 | 0.144 | 0.021 | 0.955 | 6.211 | 0.011 | 0.171 | 0.144 | 0.021 | 0.970 |
| β_S | 0.303 | 0.003 | 1.138 | 0.065 | 0.004 | 0.965 | 0.303 | 0.003 | 1.139 | 0.064 | 0.004 | 0.965 |
| σ_L^2 | 1.047 | 0.047 | 4.696 | 0.225 | 0.053 | 0.955 | 1.043 | 0.043 | 4.277 | 0.223 | 0.052 | 0.950 |
| $\sigma_S^{\overline{2}}$ | 0.138 | 0.038 | 37.634 | 0.047 | 0.004 | 0.945 | 0.136 | 0.036 | 35.937 | 0.049 | 0.004 | 0.965 |
| σ_{LS} | -0.008 | -0.008 | -0.830 | 0.064 | 0.004 | 0.955 | -0.006 | -0.006 | -0.636 | 0.063 | 0.004 | 0.960 |
| σ_e^2 | 0.110 | 0.010 | 9.603 | 0.295 | 0.087 | 0.370 | 0.110 | 0.010 | 10.372 | 0.281 | 0.079 | 0.370 |
| K_e | - | - | - | - | - | - | 4.315 | - | - | 0.377 | - | - |
| α | - | - | - | - | - | - | 0.998 | -0.002 | -0.156 | 0.004 | 0.000 | 1.000 |

Table 20: Parameter estimates for the N-N and N-Semi distributional models when $N=50, T=3, C=20, \sigma_{LS}=0$, and $\sigma^2=0.1$

| 1 v — (| 0, 1 | $_{0}$, $_{0}$ $-$ | $20, \sigma_{LS}$ | $-0, \iota$ | mao_e | - 0.1 | | | | | | | |
|---------------|--------|---------------------|-------------------|-------------|---------|-------|-----|-----|--------|----------|-------|-------|-------|
| | | | N-N mo | odel | | | | | | N-Semi 1 | nodel | | |
| | Est. | AB | RB (%) | SE | MSE | CP | | st. | AB | RB (%) | SE | MSE | CP |
| $-\beta_L$ | 6.198 | -0.002 | -0.027 | 0.139 | 0.019 | 0.955 | 6. | 196 | -0.004 | -0.059 | 0.136 | 0.018 | 0.950 |
| β_S | 0.306 | 0.006 | 1.838 | 0.061 | 0.004 | 0.960 | 0.3 | 303 | 0.003 | 1.127 | 0.060 | 0.004 | 0.960 |
| σ_L^2 | 0.936 | -0.064 | -6.398 | 1.592 | 2.539 | 0.300 | 0.8 | 898 | -0.102 | -10.247 | 1.558 | 2.436 | 0.090 |
| σ_S^2 | 0.147 | 0.047 | 47.089 | 0.198 | 0.041 | 0.850 | | 127 | 0.027 | 27.380 | 0.195 | 0.039 | 0.510 |
| σ_{LS} | -0.007 | -0.007 | -0.719 | 0.304 | 0.092 | 0.685 | -0. | 009 | -0.009 | -0.941 | 0.297 | 0.088 | 0.440 |
| σ_e^2 | 0.097 | -0.003 | -3.329 | 0.017 | 0.000 | 0.925 | | 095 | -0.005 | -4.586 | 0.017 | 0.000 | 0.920 |
| K_u | - | - | - | - | - | - | | 918 | - | - | 0.559 | - | - |
| α | - | - | - | - | - | - | 0.9 | 975 | -0.025 | -2.495 | 0.006 | 0.001 | 1.000 |

Table 21: Parameter estimates for the N-N and Semi-Semi distributional models when $N=50, T=3, C=20, \sigma_{LS}=0,$ and $\sigma_e^2=0.1$

| | | | , 10 | | ее | | | | | | | |
|---------------------|--------|--------|---------|-------|-------|-------|--------|--------|----------|---------|-------|-------|
| | | | N-N m | odel | | | | | Semi-Sem | i model | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.189 | -0.011 | -0.183 | 0.128 | 0.017 | 0.930 | 6.192 | -0.008 | -0.134 | 0.120 | 0.015 | 0.925 |
| β_{S} | 0.303 | 0.003 | 1.012 | 0.058 | 0.003 | 0.960 | 0.302 | 0.002 | 0.567 | 0.056 | 0.003 | 0.965 |
| σ_{τ}^{z} | 0.868 | -0.132 | -13.165 | 0.968 | 0.955 | 0.285 | 0.830 | -0.170 | -16.954 | 0.945 | 0.922 | 0.130 |
| σ_S^2 | 0.148 | 0.048 | 47.574 | 0.169 | 0.031 | 0.770 | 0.128 | 0.028 | 27.885 | 0.171 | 0.030 | 0.445 |
| σ_{LS} | -0.003 | -0.003 | -0.314 | 0.241 | 0.058 | 0.700 | -0.006 | -0.006 | -0.568 | 0.237 | 0.056 | 0.470 |
| σ_e^2 | 0.091 | -0.009 | -8.796 | 0.084 | 0.007 | 0.350 | 0.090 | -0.010 | -10.218 | 0.077 | 0.006 | 0.320 |
| K_e | - | - | - | - | - | - | 4.317 | - | - | 0.408 | - | - |
| K_u | - | - | - | - | - | - | 2.007 | - | - | 0.609 | - | - |
| α_1 | - | - | - | - | - | - | 0.998 | -0.002 | -0.159 | 0.004 | 0.000 | 1.000 |
| α_2 | - | - | - | - | - | - | 0.976 | -0.024 | -2.409 | 0.006 | 0.001 | 1.000 |

Table 22: Parameter estimates for the N-N and Semi-N distributional models when $N=50, T=3, C=20, \sigma_{LS}=0.3,$ and $\sigma_e^2=0.5$

| | | | N-N m | odel | | | | | Semi-N | model | | |
|---------------|-------|--------|---------|-------|-------|-------|-------|--------|---------|-------|-------|-------|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.188 | -0.012 | -0.201 | 0.170 | 0.029 | 0.950 | 6.192 | -0.008 | -0.132 | 0.169 | 0.029 | 0.955 |
| β_S | 0.305 | 0.005 | 1.702 | 0.082 | 0.007 | 0.975 | 0.301 | 0.001 | 0.345 | 0.075 | 0.006 | 0.980 |
| σ_L^2 | 1.140 | 0.140 | 13.963 | 0.284 | 0.100 | 0.965 | 1.131 | 0.131 | 13.137 | 0.266 | 0.088 | 0.970 |
| σ_S^2 | 0.242 | 0.142 | 141.724 | 0.115 | 0.033 | 0.495 | 0.225 | 0.125 | 124.950 | 0.066 | 0.020 | 0.490 |
| σ_{LS} | 0.216 | -0.084 | -28.145 | 0.099 | 0.017 | 0.870 | 0.226 | -0.074 | -24.783 | 0.091 | 0.014 | 0.890 |
| σ_e^2 | 0.418 | -0.082 | -16.418 | 0.363 | 0.139 | 0.260 | 0.422 | -0.078 | -15.529 | 0.371 | 0.144 | 0.230 |
| K_e | - | - | - | - | - | - | 4.489 | - | - | 0.444 | - | - |
| α | - | - | - | - | - | - | 1.000 | 0.000 | -0.013 | 0.005 | 0.000 | 1.000 |

Table 23: Parameter estimates for the N-N and N-Semi distributional models when $N=50, T=3, C=20, \sigma_{LS}=0.3,$ and $\sigma_e^2=0.5$

| | | | N-N m | odel | | | | | N-Semi | model | | |
|---------------|-------|--------|---------|-------|-------|-------|-------|--------|---------|-------|-------|-------|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.191 | -0.009 | -0.153 | 0.155 | 0.024 | 0.960 | 6.199 | -0.001 | -0.020 | 0.157 | 0.025 | 0.950 |
| β_S | 0.298 | -0.002 | -0.809 | 0.079 | 0.006 | 0.980 | 0.296 | -0.004 | -1.486 | 0.079 | 0.006 | 0.970 |
| σ_L^2 | 0.962 | -0.038 | -3.776 | 0.805 | 0.649 | 0.495 | 0.934 | -0.066 | -6.646 | 0.788 | 0.625 | 0.295 |
| σ_S^2 | 0.228 | 0.128 | 127.618 | 0.102 | 0.027 | 0.665 | 0.222 | 0.122 | 122.016 | 0.107 | 0.026 | 0.560 |
| σ_{LS} | 0.159 | -0.141 | -46.916 | 0.265 | 0.090 | 0.330 | 0.143 | -0.157 | -52.464 | 0.255 | 0.090 | 0.175 |
| σ_e^2 | 0.449 | -0.051 | -10.218 | 0.077 | 0.009 | 0.875 | 0.442 | -0.058 | -11.520 | 0.077 | 0.009 | 0.860 |
| K_u | - | - | - | - | - | - | 2.523 | - | - | 0.542 | - | - |
| α | - | - | - | - | - | - | 0.981 | -0.019 | -1.924 | 0.005 | 0.000 | 1.000 |

Table 24: Parameter estimates for the N-N and Semi-Semi distributional models when $N=50, T=3, C=20, \sigma_{LS}=0.3,$ and $\sigma_e^2=0.5$

| | / | | - , - DL | | | e | | | | | | |
|------------------------------|-------|--------|----------|-------|-------|-------|-------|--------|----------|---------|-------|-------|
| | | | N-N m | odel | | | | | Semi-Sem | i model | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.195 | -0.005 | -0.087 | 0.166 | 0.028 | 0.980 | 6.196 | -0.004 | -0.060 | 0.147 | 0.021 | 0.970 |
| β_S | 0.300 | 0.000 | 0.161 | 0.079 | 0.006 | 0.980 | 0.298 | -0.002 | -0.526 | 0.073 | 0.005 | 0.980 |
| σ_L^2 | 1.098 | 0.098 | 9.841 | 1.258 | 1.592 | 0.425 | 1.051 | 0.051 | 5.126 | 1.220 | 1.491 | 0.295 |
| $\sigma_S^{\overline{2}}$ | 0.247 | 0.147 | 147.283 | 0.300 | 0.112 | 0.710 | 0.217 | 0.117 | 116.946 | 0.151 | 0.037 | 0.635 |
| σ_{LS} | 0.157 | -0.143 | -47.786 | 0.440 | 0.214 | 0.275 | 0.163 | -0.137 | -45.702 | 0.351 | 0.142 | 0.165 |
| $\stackrel{\sigma_e^2}{K_e}$ | 0.550 | 0.050 | 10.086 | 0.907 | 0.826 | 0.285 | 0.543 | 0.043 | 8.606 | 0.959 | 0.922 | 0.230 |
| K_e | - | - | - | - | - | - | 4.501 | - | - | 0.420 | - | - |
| K_u | - | - | - | - | - | - | 2.416 | - | - | 0.584 | - | - |
| α_1 | - | - | - | - | - | - | 1.000 | 0.000 | 0.016 | 0.004 | 0.000 | 1.000 |
| α_2 | - | - | - | - | - | - | 0.980 | -0.020 | -2.007 | 0.006 | 0.000 | 1.000 |

Table 25: Parameter estimates for the N-N and Semi-N distributional models when $N=50, T=5, C=20, \sigma_{LS}=0$, and $\sigma_{c}^{2}=0.5$

| | / | - , - | -, - L D | - , . | · · · · · e | | | | | | | |
|---------------------------|--------|--------|-----------------|-------|-------------|-------|--------|--------|----------|-------|-------|-------|
| | | | N-N me | odel | | | | | Semi-N ı | nodel | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.208 | 0.008 | 0.129 | 0.157 | 0.025 | 0.955 | 6.206 | 0.006 | 0.102 | 0.157 | 0.025 | 0.945 |
| β_S | 0.301 | 0.001 | 0.176 | 0.052 | 0.003 | 0.980 | 0.300 | 0.000 | 0.071 | 0.050 | 0.003 | 0.985 |
| σ_L^2 | 1.044 | 0.044 | 4.402 | 0.287 | 0.084 | 0.930 | 1.041 | 0.041 | 4.074 | 0.271 | 0.075 | 0.935 |
| $\sigma_S^{\overline{2}}$ | 0.138 | 0.038 | 38.268 | 0.029 | 0.002 | 0.935 | 0.137 | 0.037 | 37.058 | 0.027 | 0.002 | 0.945 |
| σ_{LS} | -0.021 | -0.021 | -2.059 | 0.062 | 0.004 | 0.975 | -0.019 | -0.019 | -1.878 | 0.059 | 0.004 | 0.975 |
| σ_e^2 | 0.423 | -0.077 | -15.398 | 0.306 | 0.100 | 0.175 | 0.420 | -0.080 | -15.964 | 0.305 | 0.099 | 0.135 |
| K_e | - | - | - | - | - | - | 4.470 | - | - | 0.550 | - | - |
| α | - | - | - | - | - | - | 1.000 | 0.000 | -0.035 | 0.005 | 0.000 | 1.000 |

Table 26: Parameter estimates for the N-N and N-Semi distributional models when $N=50, T=5, C=20, \sigma_{LS}=0,$ and $\sigma_e^2=0.5$

| | , - | ٠, ٠ | - · , · LD | -, - | e | 0.0 | | | | | | |
|---------------|--------|--------|------------|-------|-------|-------|--------|--------|----------|-------|-------|-------|
| | | | N-N me | odel | | | | | N-Semi 1 | nodel | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.185 | -0.015 | -0.249 | 0.151 | 0.023 | 0.950 | 6.188 | -0.012 | -0.186 | 0.142 | 0.020 | 0.955 |
| β_S | 0.299 | -0.001 | -0.305 | 0.050 | 0.003 | 0.980 | 0.298 | -0.002 | -0.759 | 0.050 | 0.002 | 0.985 |
| σ_L^2 | 0.756 | -0.244 | -24.368 | 0.680 | 0.522 | 0.400 | 0.727 | -0.273 | -27.279 | 0.667 | 0.519 | 0.270 |
| σ_S^2 | 0.117 | 0.017 | 17.240 | 0.078 | 0.006 | 0.870 | 0.098 | -0.002 | -2.486 | 0.078 | 0.006 | 0.455 |
| σ_{LS} | -0.031 | -0.031 | -3.109 | 0.166 | 0.028 | 0.810 | -0.034 | -0.034 | -3.450 | 0.162 | 0.028 | 0.620 |
| σ_e^2 | 0.498 | -0.002 | -0.348 | 0.056 | 0.003 | 0.940 | 0.496 | -0.004 | -0.872 | 0.055 | 0.003 | 0.940 |
| K_u | - | - | - | - | - | - | 1.843 | - | - | 0.495 | - | - |
| α | - | - | - | - | - | - | 0.974 | -0.026 | -2.579 | 0.005 | 0.001 | 1.000 |

Table 27: Parameter estimates for the N-N and Semi-Semi distributional models when $N=50, T=5, C=20, \sigma_{LS}=0$, and $\sigma_e^2=0.5$

| | , - | -, - | -0,0 LL | , ,,- | e | 0.0 | | | | | | |
|----------------------------|-----------------|-----------------|------------------|----------------|-------------|----------------|-----------------|------------------|------------------|----------------|-------|----------------|
| | | | N-N m | odel | | | | | Semi-Sem | i model | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| $-\beta_L$ | 6.183 | -0.017 | -0.269 | 0.153 | 0.024 | 0.950 | 6.182 | -0.018 | -0.291 | 0.145 | 0.021 | 0.955 |
| β_S | 0.297 | -0.003 | -0.945 | 0.049 | 0.002 | 0.975 | 0.297 | -0.003 | -0.838 | 0.047 | 0.002 | 0.980 |
| $\beta_S \\ \sigma_L^2$ | 0.909 | -0.091 | -9.114 | 1.005 | 1.019 | 0.380 | 0.875 | -0.125 | -12.533 | 0.990 | 0.997 | 0.235 |
| σ_S^2 | 0.120 -0.047 | 0.020 -0.047 | 19.767 -4.733 | 0.090 0.259 | 0.008 0.069 | 0.800 0.755 | 0.098 -0.048 | -0.002 -0.048 | -1.620 -4.781 | 0.090 0.256 | 0.008 | 0.415 0.555 |
| $\sigma_{LS} = \sigma_e^2$ | 0.481 | -0.019 | -3.835 | 0.460 | 0.212 | 0.733 | 0.472 | -0.028 | -5.565 | 0.230 | 0.195 | 0.145 |
| K_e | - | - | - | - | - | - | 4.482 | - | - | 0.606 | - | - |
| K_u | - | - | - | - | - | - | 1.869 | - | - | 0.494 | - | - |
| α_1 | - | - | - | - | - | - | 1.000 | 0.000 | 0.007 | 0.006 | 0.000 | 1.000 |
| α_2 | - | - | - | - | - | - | 0.974 | -0.026 | -2.558 | 0.005 | 0.001 | 1.000 |
| | | | | | | | | | | | | |

Table 28: Parameter estimates for the N-N and Semi-N distributional models when $N=50, T=5, C=20, \sigma_{LS}=0.3,$ and $\sigma_{e}^{2}=0.1$

| | , - | ٠, ٠ | - · , · D, | , | ,, | e | | | | | | |
|---------------|-------|--------|------------|-------|-------|-------|-------|--------|---------|-------|-------|-------|
| | | | N-N m | odel | | | | | Semi-N | model | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.192 | -0.008 | -0.136 | 0.142 | 0.020 | 0.955 | 6.190 | -0.010 | -0.167 | 0.140 | 0.020 | 0.950 |
| β_S | 0.296 | -0.004 | -1.210 | 0.043 | 0.002 | 0.970 | 0.295 | -0.005 | -1.513 | 0.043 | 0.002 | 0.980 |
| σ_L^2 | 1.040 | 0.040 | 4.044 | 0.186 | 0.036 | 0.970 | 1.041 | 0.041 | 4.116 | 0.187 | 0.037 | 0.975 |
| σ_S^2 | 0.133 | 0.033 | 33.442 | 0.023 | 0.002 | 0.890 | 0.133 | 0.033 | 32.660 | 0.022 | 0.002 | 0.895 |
| σ_{LS} | 0.287 | -0.013 | -4.499 | 0.057 | 0.003 | 0.960 | 0.288 | -0.012 | -4.050 | 0.057 | 0.003 | 0.960 |
| σ_e^2 | 0.089 | -0.011 | -10.735 | 0.086 | 0.007 | 0.170 | 0.088 | -0.012 | -11.749 | 0.084 | 0.007 | 0.100 |
| K_e | - | - | - | - | - | - | 4.350 | - | - | 0.548 | - | - |
| α | - | - | - | - | - | - | 0.999 | -0.001 | -0.137 | 0.006 | 0.000 | 1.000 |

Table 29: Parameter estimates for the N-N and N-Semi distributional models when $N=50, T=5, C=20, \sigma_{LS}=0.3,$ and $\sigma_e^2=0.1$

| | 00, - | ٠, ٠ | N-N m | | , што | e 0.1 | | | N-Semi | | | |
|---------------------------|-------|--------|--------|-------|-------|-------|-------|--------|---------|-------|-------|-------|
| | | | | | | | | | | | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.193 | -0.007 | -0.112 | 0.142 | 0.020 | 0.930 | 6.195 | -0.005 | -0.075 | 0.128 | 0.016 | 0.930 |
| β_S | 0.304 | 0.004 | 1.295 | 0.046 | 0.002 | 0.970 | 0.304 | 0.004 | 1.335 | 0.042 | 0.002 | 0.970 |
| σ_L^2 | 1.029 | 0.029 | 2.876 | 2.144 | 4.597 | 0.280 | 0.988 | -0.012 | -1.175 | 2.098 | 4.402 | 0.105 |
| $\sigma_S^{\overline{2}}$ | 0.131 | 0.031 | 31.195 | 0.181 | 0.034 | 0.575 | 0.108 | 0.008 | 8.417 | 0.178 | 0.032 | 0.125 |
| σ_{LS} | 0.276 | -0.024 | -8.162 | 0.609 | 0.372 | 0.275 | 0.269 | -0.031 | -10.179 | 0.596 | 0.356 | 0.035 |
| σ_e^2 | 0.095 | -0.005 | -5.178 | 0.010 | 0.000 | 0.910 | 0.095 | -0.005 | -5.362 | 0.010 | 0.000 | 0.910 |
| K_u | - | - | - | - | - | - | 1.476 | - | - | 0.307 | - | - |
| α | - | - | - | - | - | - | 0.971 | -0.029 | -2.918 | 0.004 | 0.001 | 1.000 |

Table 30: Parameter estimates for the N-N and Semi-Semi distributional models when

 $N = 50, T = 5, C = 20, \sigma_{LS} = 0.3, \text{ and } \sigma_e^2 = 0.1$

| | | | N-N m | odel | | | | | Semi-Sem | i model | | |
|---------------|-------|--------|---------|-------|-------|-------|-------|--------|----------|---------|-------|-------|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.208 | 0.008 | 0.129 | 0.144 | 0.021 | 0.955 | 6.205 | 0.005 | 0.088 | 0.123 | 0.015 | 0.950 |
| eta_S | 0.305 | 0.005 | 1.565 | 0.045 | 0.002 | 0.980 | 0.303 | 0.003 | 1.100 | 0.039 | 0.002 | 0.985 |
| σ_L^2 | 0.887 | -0.113 | -11.343 | 1.137 | 1.306 | 0.250 | 0.849 | -0.151 | -15.114 | 1.115 | 1.266 | 0.085 |
| σ_S^2 | 0.118 | 0.018 | 17.835 | 0.113 | 0.013 | 0.540 | 0.095 | -0.005 | -5.343 | 0.110 | 0.012 | 0.145 |
| σ_{LS} | 0.238 | -0.062 | -20.578 | 0.340 | 0.120 | 0.220 | 0.234 | -0.066 | -22.002 | 0.333 | 0.115 | 0.035 |
| σ_e^2 | 0.089 | -0.011 | -11.355 | 0.078 | 0.006 | 0.205 | 0.088 | -0.012 | -12.393 | 0.076 | 0.006 | 0.160 |
| K_e | - | - | - | - | - | - | 4.326 | - | - | 0.579 | - | - |
| K_u | - | - | - | - | - | - | 1.465 | - | - | 0.342 | - | - |
| α_1 | - | - | - | - | - | - | 0.999 | -0.001 | -0.149 | 0.006 | 0.000 | 1.000 |
| α_2 | - | - | - | - | - | - | 0.971 | -0.029 | -2.949 | 0.004 | 0.001 | 1.000 |

Table 31: Parameter estimates for the N-N and Semi-N distributional models when

 $N = 200, T = 3, C = 20, \sigma_{LS} = 0, \text{ and } \sigma_e^2 = 0.5$

| | , | -, - | - , · L | - , | | | | | | | | |
|---------------------------|--------|--------|---------|-------|-------|-------|--------|--------|----------|-------|-------|-------|
| | | | N-N m | odel | | | | | Semi-N i | nodel | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.201 | 0.001 | 0.009 | 0.082 | 0.007 | 0.960 | 6.201 | 0.001 | 0.008 | 0.081 | 0.007 | 0.955 |
| β_S | 0.303 | 0.003 | 0.845 | 0.041 | 0.002 | 0.980 | 0.302 | 0.002 | 0.620 | 0.039 | 0.001 | 0.970 |
| σ_L^2 | 1.016 | 0.016 | 1.576 | 0.138 | 0.019 | 0.970 | 1.014 | 0.014 | 1.395 | 0.134 | 0.018 | 0.970 |
| $\sigma_S^{\overline{2}}$ | 0.135 | 0.035 | 35.280 | 0.035 | 0.002 | 0.910 | 0.132 | 0.032 | 31.663 | 0.028 | 0.002 | 0.940 |
| σ_{LS} | -0.022 | -0.022 | -2.157 | 0.058 | 0.004 | 0.905 | -0.019 | -0.019 | -1.899 | 0.053 | 0.003 | 0.945 |
| σ_e^2 | 0.475 | -0.025 | -5.076 | 0.365 | 0.134 | 0.240 | 0.476 | -0.024 | -4.835 | 0.364 | 0.133 | 0.215 |
| K_e | - | - | - | - | - | - | 5.800 | - | - | 0.653 | - | - |
| α | - | - | - | - | - | - | 0.999 | -0.001 | -0.069 | 0.006 | 0.000 | 1.000 |

Note. Est.: estimate; AB: absolute bias; RB: relative bias; SE: standard error; MSE: mean square error; CP: coverage probability.

Table 32: Parameter estimates for the N-N and N-Semi distributional models when

 $N = 200, T = 3, C = 20, \sigma_{LS} = 0, \text{ and } \sigma_e^2 = 0.5$

| | 700, 1 | - 0, 0 | - 20, 0 L | | una o e | . — 0.0 | | | | | | |
|---------------|--------|--------|-----------|-------|---------|---------|--------|--------|----------|-------|-------|-------|
| | | | N-N mo | oaei | | | | | N-Semi ı | noaei | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.211 | 0.011 | 0.172 | 0.084 | 0.007 | 0.955 | 6.209 | 0.009 | 0.144 | 0.078 | 0.006 | 0.960 |
| β_S | 0.295 | -0.005 | -1.668 | 0.044 | 0.002 | 0.950 | 0.296 | -0.004 | -1.356 | 0.042 | 0.002 | 0.955 |
| σ_L^2 | 1.160 | 0.160 | 15.959 | 2.310 | 5.360 | 0.205 | 1.158 | 0.158 | 15.847 | 2.301 | 5.320 | 0.165 |
| σ_S^2 | 0.139 | 0.039 | 38.534 | 0.094 | 0.010 | 0.855 | 0.145 | 0.045 | 45.319 | 0.097 | 0.012 | 0.765 |
| σ_{LS} | -0.080 | -0.080 | -7.990 | 0.336 | 0.120 | 0.605 | -0.088 | -0.088 | -8.837 | 0.335 | 0.120 | 0.545 |
| σ_e^2 | 0.472 | -0.028 | -5.684 | 0.043 | 0.003 | 0.865 | 0.465 | -0.035 | -6.910 | 0.042 | 0.003 | 0.825 |
| K_u | - | - | - | - | - | - | 2.710 | - | - | 0.697 | - | - |
| α | - | - | - | - | - | - | 0.970 | -0.030 | -3.033 | 0.007 | 0.001 | 1.000 |

Table 33: Parameter estimates for the N-N and Semi-Semi distributional models when $N=200, T=3, C=20, \sigma_{LS}=0,$ and $\sigma_e^2=0.5$

| | , _ | ٠, ٠ | - · , · L | | · · · · · · · · | , | | | | | | |
|-------------------------|----------------|-----------------|------------------|----------------|-----------------|----------------|------|----------|------------------|----------------|----------------|----------------|
| | | | N-N m | odel | | | | | Semi-Sem | i model | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.191 | -0.009 | -0.138 | 0.072 | 0.005 | 0.945 | 6.19 | 3 -0.007 | -0.114 | 0.067 | 0.005 | 0.950 |
| β_S | 0.303 | 0.003 | 1.033 | 0.043 | 0.002 | 0.970 | 0.30 | 4 0.004 | 1.276 | 0.041 | 0.002 | 0.960 |
| σ_I^2 | 0.822 | -0.178 | -17.779 | 0.859 | 0.769 | 0.135 | 0.81 | 8 -0.182 | -18.167 | 0.857 | 0.767 | 0.075 |
| σ_S^2 | | 0.044 -0.061 | 44.172 -6.071 | 0.148 0.225 | 0.024 0.054 | 0.750 0.565 | 0.14 | | 47.325 -6.640 | 0.151 0.223 | 0.025 0.054 | 0.650 0.500 |
| σ_L σ_e^2 | 0.511 | 0.011 | 2.204 | 0.512 | 0.262 | 0.110 | 0.50 | 4 0.004 | 0.855 | 0.508 | 0.258 | 0.105 |
| K_{ϵ}^{e} | | - | - | - | - | - | 5.84 | | - | 0.587 | - | - |
| K_{i} | _L - | - | - | - | - | - | 2.73 | | - | 0.759 | - | - |
| α_1 | - | - | - | - | - | - | 1.00 | | -0.036 | 0.006 | 0.000 | 1.000 |
| α_2 | - | - | - | - | - | - | 0.97 | 0 -0.030 | -2.986 | 0.008 | 0.001 | 1.000 |

Table 34: Parameter estimates for the N-N and Semi-N distributional models when $N=200, T=3, C=20, \sigma_{LS}=0.3,$ and $\sigma_e^2=0.1$

| | , | | | _~ | | C | | | | | | |
|------------------|-------|--------|---------|-------|-------|-------|-------|--------|---------|-------|-------|-------|
| | | | N-N m | odel | | | | | Semi-N | model | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.207 | 0.007 | 0.116 | 0.074 | 0.006 | 0.965 | 6.210 | 0.010 | 0.154 | 0.074 | 0.006 | 0.965 |
| β_S | 0.299 | -0.001 | -0.211 | 0.027 | 0.001 | 0.955 | 0.300 | 0.000 | 0.089 | 0.026 | 0.001 | 0.955 |
| σ_{L}^{2} | 1.028 | 0.028 | 2.821 | 0.103 | 0.011 | 0.970 | 1.026 | 0.026 | 2.649 | 0.102 | 0.011 | 0.980 |
| σ_S^2 | 0.126 | 0.026 | 25.828 | 0.018 | 0.001 | 0.710 | 0.124 | 0.024 | 24.416 | 0.016 | 0.001 | 0.725 |
| σ_{LS} | 0.281 | -0.019 | -6.435 | 0.034 | 0.002 | 0.895 | 0.282 | -0.018 | -5.916 | 0.033 | 0.001 | 0.900 |
| σ_e^2 | 0.086 | -0.014 | -14.006 | 0.066 | 0.005 | 0.105 | 0.087 | -0.013 | -13.360 | 0.069 | 0.005 | 0.080 |
| K_e | - | - | - | - | - | - | 5.731 | - | - | 0.642 | - | - |
| α | - | - | - | - | - | - | 0.999 | -0.001 | -0.142 | 0.006 | 0.000 | 1.000 |

Table 35: Parameter estimates for the N-N and N-Semi distributional models when $N=200, T=3, C=20, \sigma_{LS}=0.3,$ and $\sigma_e^2=0.1$

| | | | N-N n | nodel | | | | | N-Semi | model | | |
|---------------|-------|--------|---------|-------|--------|-------|-------|--------|---------|-------|--------|-------|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.198 | -0.002 | -0.027 | 0.067 | 0.005 | 0.940 | 6.201 | 0.001 | 0.014 | 0.057 | 0.003 | 0.955 |
| β_S | 0.300 | 0.000 | -0.155 | 0.026 | 0.001 | 0.970 | 0.300 | 0.000 | 0.127 | 0.023 | 0.001 | 0.980 |
| σ_L^2 | 1.534 | 0.534 | 53.358 | 8.174 | 67.094 | 0.135 | 1.523 | 0.523 | 52.305 | 8.142 | 66.561 | 0.050 |
| σ_S^2 | 0.168 | 0.068 | 68.334 | 0.693 | 0.484 | 0.385 | 0.165 | 0.065 | 64.643 | 0.690 | 0.481 | 0.235 |
| σ_{LS} | 0.422 | 0.122 | 40.770 | 2.374 | 5.650 | 0.150 | 0.419 | 0.119 | 39.602 | 2.364 | 5.603 | 0.055 |
| σ_e^2 | 0.087 | -0.013 | -12.573 | 0.007 | 0.000 | 0.575 | 0.087 | -0.013 | -12.954 | 0.007 | 0.000 | 0.570 |
| K_u | - | - | - | - | - | - | 2.021 | - | - | 0.504 | - | - |
| α | - | - | - | - | - | - | 0.963 | -0.037 | -3.676 | 0.005 | 0.001 | 1.000 |

Table 36: Parameter estimates for the N-N and Semi-Semi distributional models when $N=200, T=3, C=20, \sigma_{LS}=0.3,$ and $\sigma_e^2=0.1$

| | | | N-N m | odel | | | | | Semi-Sem | i model | | |
|------------------------------|-------|--------|---------|-------|-------|-------|-------|--------|----------|---------|-------|-------|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.200 | 0.000 | 0.000 | 0.070 | 0.005 | 0.950 | 6.201 | 0.001 | 0.023 | 0.064 | 0.004 | 0.950 |
| β_S | 0.299 | -0.001 | -0.460 | 0.023 | 0.001 | 0.975 | 0.300 | 0.000 | -0.166 | 0.022 | 0.001 | 0.975 |
| σ_L^2 | 0.988 | -0.012 | -1.174 | 1.329 | 1.768 | 0.135 | 0.978 | -0.022 | -2.169 | 1.323 | 1.750 | 0.050 |
| $\sigma_S^{\overline{2}}$ | 0.119 | 0.019 | 19.016 | 0.118 | 0.014 | 0.330 | 0.113 | 0.013 | 13.410 | 0.118 | 0.014 | 0.185 |
| σ_{LS} | 0.258 | -0.042 | -14.032 | 0.377 | 0.144 | 0.115 | 0.257 | -0.043 | -14.399 | 0.375 | 0.142 | 0.030 |
| $\stackrel{\sigma_e^2}{K_e}$ | 0.091 | -0.009 | -8.980 | 0.109 | 0.012 | 0.110 | 0.091 | -0.009 | -8.928 | 0.109 | 0.012 | 0.090 |
| K_e | - | - | - | - | - | - | 5.711 | - | - | 0.588 | - | - |
| K_u | - | - | - | - | - | - | 1.989 | - | - | 0.510 | - | - |
| α_1 | - | - | - | - | - | - | 0.998 | -0.002 | -0.170 | 0.006 | 0.000 | 1.000 |
| α_2 | - | - | - | - | - | - | 0.963 | -0.037 | -3.728 | 0.005 | 0.001 | 1.000 |

Table 37: Parameter estimates for the N-N and Semi-N distributional models when $N=200, T=5, C=20, \sigma_{LS}=0,$ and $\sigma_e^2=0.1$

| | | | N-N m | odel | | <u> </u> | | | Semi-N | model | | |
|---------------------------|-------|--------|--------|-------|-------|----------|-------|--------|--------|-------|-------|-------|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.206 | 0.006 | 0.101 | 0.072 | 0.005 | 0.950 | 6.206 | 0.006 | 0.100 | 0.071 | 0.005 | 0.950 |
| β_S | 0.300 | 0.000 | -0.157 | 0.023 | 0.001 | 0.945 | 0.300 | 0.000 | -0.044 | 0.023 | 0.001 | 0.950 |
| σ_L^2 | 1.002 | 0.002 | 0.197 | 0.108 | 0.012 | 0.940 | 1.003 | 0.003 | 0.344 | 0.108 | 0.012 | 0.935 |
| $\sigma_S^{\overline{2}}$ | 0.105 | 0.005 | 5.030 | 0.010 | 0.000 | 0.965 | 0.105 | 0.005 | 5.239 | 0.010 | 0.000 | 0.950 |
| σ_{LS} | 0.002 | 0.002 | 0.207 | 0.023 | 0.001 | 0.955 | 0.002 | 0.002 | 0.154 | 0.023 | 0.001 | 0.950 |
| σ_e^2 | 0.094 | -0.006 | -6.108 | 0.139 | 0.019 | 0.070 | 0.094 | -0.006 | -6.337 | 0.138 | 0.019 | 0.060 |
| K_e | - | - | - | - | - | - | 5.572 | - | - | 0.802 | - | - |
| α | - | - | - | - | - | - | 0.997 | -0.003 | -0.290 | 0.008 | 0.000 | 1.000 |

Table 38: Parameter estimates for the N-N and N-Semi distributional models when $N=200, T=5, C=20, \sigma_{LS}=0, \text{ and } \sigma_e^2=0.1$

| | , _ | ٠, ٠ | , - L | (D) | e | | | | | | | |
|--------------|-------|--------|---------|-------|-------|-------|--------|--------|----------|-------|-------|-------|
| | | | N-N m | odel | | | | | N-Semi i | nodel | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.200 | 0.000 | 0.005 | 0.054 | 0.003 | 0.985 | 6.199 | -0.001 | -0.020 | 0.051 | 0.003 | 0.975 |
| β_S | 0.299 | -0.001 | -0.457 | 0.021 | 0.000 | 0.970 | 0.298 | -0.002 | -0.699 | 0.019 | 0.000 | 0.965 |
| σ_L^2 | 0.836 | -0.164 | -16.353 | 1.304 | 1.726 | 0.120 | 0.829 | -0.171 | -17.113 | 1.299 | 1.715 | 0.050 |
| σ_S^2 | 0.094 | -0.006 | -6.150 | 0.098 | 0.010 | 0.195 | 0.089 | -0.011 | -10.798 | 0.098 | 0.010 | 0.055 |
| σ_{L} | | -0.009 | -0.919 | 0.244 | 0.060 | 0.345 | -0.010 | -0.010 | -1.015 | 0.243 | 0.059 | 0.135 |
| σ_e^2 | | -0.001 | -0.529 | 0.005 | 0.000 | 0.955 | 0.099 | -0.001 | -0.737 | 0.005 | 0.000 | 0.950 |
| K_{i} | | - | - | - | - | - | 2.418 | - | - | 0.789 | - | - |
| α | - | - | - | - | - | - | 0.967 | -0.033 | -3.309 | 0.008 | 0.001 | 1.000 |

Table 39: Parameter estimates for the N-N and Semi-Semi distributional models when $N=200, T=5, C=20, \sigma_{LS}=0,$ and $\sigma_e^2=0.1$

| | | ٠, ٠ | , - L | ,,, | | | | | | | | |
|------------------------------|--------|--------|---------|-------|-------|-------|--------|--------|----------|-------|-------|-------|
| | | | N-N m | odel | | | | | Semi-Sem | model | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.200 | 0.000 | 0.006 | 0.066 | 0.004 | 0.975 | 6.202 | 0.002 | 0.027 | 0.060 | 0.004 | 0.965 |
| β_S | 0.298 | -0.002 | -0.757 | 0.027 | 0.001 | 0.955 | 0.298 | -0.002 | -0.627 | 0.020 | 0.000 | 0.955 |
| $\frac{\beta_S}{\sigma_L^2}$ | 0.822 | -0.178 | -17.805 | 0.820 | 0.705 | 0.140 | 0.813 | -0.187 | -18.682 | 0.817 | 0.703 | 0.050 |
| $\sigma_S^{\overline{2}}$ | 0.133 | 0.033 | 32.614 | 0.281 | 0.080 | 0.160 | 0.128 | 0.028 | 27.502 | 0.280 | 0.079 | 0.055 |
| σ_{LS} | -0.011 | -0.011 | -1.105 | 0.242 | 0.059 | 0.305 | -0.011 | -0.011 | -1.140 | 0.241 | 0.058 | 0.135 |
| σ_e^2 | 0.089 | -0.011 | -11.194 | 0.067 | 0.005 | 0.150 | 0.089 | -0.011 | -11.437 | 0.067 | 0.005 | 0.115 |
| K_e | - | - | - | - | - | - | 5.776 | - | - | 0.713 | - | - |
| K_u | - | - | - | - | - | - | 2.425 | - | - | 0.780 | - | - |
| α_1 | - | - | - | - | - | - | 0.999 | -0.001 | -0.103 | 0.007 | 0.000 | 1.000 |
| α_2 | - | - | - | - | - | - | 0.967 | -0.033 | -3.316 | 0.007 | 0.001 | 1.000 |
| | | | | | | | | | | | | |

Table 40: Parameter estimates for the N-N and Semi-N distributional models when $N=200, T=5, C=20, \sigma_{LS}=0.3,$ and $\sigma_e^2=0.5$

| | | ٠, ٠ | ,-, | JD - | , | e | | | | | | |
|---------------|-------|--------|---------|-------|-------|-------|-------|--------|--------|-------|-------|-------|
| | | | N-N m | odel | | | | | Semi-N | model | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.210 | 0.010 | 0.167 | 0.084 | 0.007 | 0.945 | 6.210 | 0.010 | 0.160 | 0.084 | 0.007 | 0.940 |
| β_S | 0.299 | -0.001 | -0.274 | 0.028 | 0.001 | 0.950 | 0.300 | 0.000 | 0.093 | 0.028 | 0.001 | 0.955 |
| σ_L^2 | 1.064 | 0.064 | 6.447 | 0.146 | 0.026 | 0.950 | 1.054 | 0.054 | 5.404 | 0.129 | 0.020 | 0.950 |
| σ_S^2 | 0.127 | 0.027 | 27.291 | 0.020 | 0.001 | 0.660 | 0.125 | 0.025 | 25.049 | 0.018 | 0.001 | 0.660 |
| σ_{LS} | 0.266 | -0.034 | -11.220 | 0.039 | 0.003 | 0.850 | 0.271 | -0.029 | -9.511 | 0.036 | 0.002 | 0.900 |
| σ_e^2 | 0.574 | 0.074 | 14.861 | 0.877 | 0.774 | 0.105 | 0.576 | 0.076 | 15.268 | 0.882 | 0.785 | 0.065 |
| K_e | - | - | - | - | - | - | 5.816 | - | - | 0.771 | - | - |
| α | - | - | - | - | - | - | 0.999 | -0.001 | -0.060 | 0.007 | 0.000 | 1.000 |

Table 41: Parameter estimates for the N-N and N-Semi distributional models when $N=200,\,T=5,\,C=20,\,\sigma_{LS}=0.3,$ and $\sigma_e^2=0.5$

| | | | | -2 | | - C | | | | | | |
|-----------------------------------------|----------------|-----------------|------------------|----------------|------------------|----------------|--------------|----------|------------------|----------------|------------------|----------------|
| | | | N-N m | odel | | | | | N-Semi | model | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est | . AB | RB (%) | SE | MSE | CP |
| β_L | 6.195 | -0.005 | -0.089 | 0.075 | 0.006 | 0.964 | 6.20 | 3 0.003 | 0.047 | 0.070 | 0.005 | 0.960 |
| β_S | 0.300 | 0.000 | 0.007 | 0.024 | 0.001 | 0.979 | 0.30 | 0.000 | 0.012 | 0.022 | 0.000 | 0.990 |
| σ_L^2 | 0.883 | -0.117 | -11.720 | 1.057 | 1.131 | 0.164 | 0.86 | 0 -0.140 | -13.981 | 0.944 | 0.910 | 0.110 |
| $\sigma_S^{\overline{2}} \ \sigma_{LS}$ | 0.106 0.204 | 0.006 -0.096 | 5.927 -31.950 | 0.090 0.293 | $0.008 \\ 0.095$ | 0.321 0.100 | 0.10 0.19 | | 1.660 -34.727 | 0.085 0.265 | $0.007 \\ 0.081$ | 0.200 0.035 |
| σ_e^2 | 0.476 | -0.024 | -4.789 | 0.024 | 0.001 | 0.814 | 0.47 | 6 -0.024 | -4.897 | 0.024 | 0.001 | 0.825 |
| K_u^e | - | - | - | - | - | - | 2.02 | .7 - | - | 0.481 | - | - |
| α | - | - | - | - | - | - | 0.96 | 3 -0.037 | -3.685 | 0.005 | 0.001 | 1.000 |

Table 42: Parameter estimates for the N-N and Semi-Semi distributional models when

 $N=200, T=5, C=20, \sigma_{LS}=0.3, \text{ and } \sigma_e^2=0.5$

| | | | N-N m | odel | | | | | Semi-Sem | i model | | |
|---------------------------|-------|--------|---------|-------|-------|-------|-------|--------|----------|---------|-------|-------|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.196 | -0.004 | -0.063 | 0.083 | 0.007 | 0.945 | 6.198 | -0.002 | -0.032 | 0.071 | 0.005 | 0.945 |
| β_{S} | 0.300 | 0.000 | 0.150 | 0.033 | 0.001 | 0.960 | 0.301 | 0.001 | 0.406 | 0.027 | 0.001 | 0.965 |
| $\sigma_{\c L}^2$ | 1.169 | 0.169 | 16.915 | 1.767 | 3.151 | 0.185 | 1.155 | 0.155 | 15.469 | 1.760 | 3.120 | 0.110 |
| $\sigma_S^{\overline{2}}$ | 0.133 | 0.033 | 33.053 | 0.162 | 0.027 | 0.355 | 0.128 | 0.028 | 28.036 | 0.163 | 0.027 | 0.195 |
| σ_{LS} | 0.299 | -0.001 | -0.361 | 0.515 | 0.266 | 0.120 | 0.298 | -0.002 | -0.718 | 0.512 | 0.263 | 0.025 |
| σ_e^2 | 0.450 | -0.050 | -10.010 | 0.740 | 0.551 | 0.120 | 0.449 | -0.051 | -10.146 | 0.740 | 0.550 | 0.090 |
| K_e | - | - | - | - | - | - | 5.921 | - | - | 0.831 | - | - |
| K_u | - | - | - | - | - | - | 1.975 | - | - | 0.558 | - | - |
| α_1 | - | - | - | - | - | - | 1.000 | 0.000 | 0.043 | 0.008 | 0.000 | 1.000 |
| α_2 | - | - | - | - | - | - | 0.963 | -0.037 | -3.743 | 0.006 | 0.001 | 1.000 |

Table 43: Parameter estimates for the N-N and Semi-N distributional models when

 $N=500, T=3, C=20, \sigma_{LS}=0, ext{ and } \sigma_e^2=0.1$

| | | | N-N mo | odel | | | | | Semi-N ı | nodel | | |
|---------------------------|--------|--------|---------|-------|-------|-------|--------|--------|----------|-------|-------|-------|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.199 | -0.001 | -0.015 | 0.047 | 0.002 | 0.955 | 6.199 | -0.001 | -0.009 | 0.047 | 0.002 | 0.950 |
| β_S | 0.302 | 0.002 | 0.744 | 0.018 | 0.000 | 0.940 | 0.302 | 0.002 | 0.651 | 0.017 | 0.000 | 0.960 |
| σ_L^2 | 0.995 | -0.005 | -0.463 | 0.067 | 0.005 | 0.955 | 0.996 | -0.004 | -0.433 | 0.067 | 0.005 | 0.960 |
| $\sigma_S^{\overline{2}}$ | 0.105 | 0.005 | 4.970 | 0.010 | 0.000 | 0.925 | 0.104 | 0.004 | 4.189 | 0.009 | 0.000 | 0.925 |
| σ_{LS} | -0.002 | -0.002 | -0.167 | 0.018 | 0.000 | 0.965 | -0.001 | -0.001 | -0.091 | 0.017 | 0.000 | 0.960 |
| σ_e^2 | 0.086 | -0.014 | -13.546 | 0.065 | 0.004 | 0.115 | 0.087 | -0.013 | -12.984 | 0.065 | 0.004 | 0.110 |
| K_e | - | - | - | - | - | - | 6.593 | - | - | 0.758 | - | - |
| α | - | - | - | - | - | - | 0.998 | -0.002 | -0.173 | 0.007 | 0.000 | 1.000 |

Note. Est.: estimate; AB: absolute bias; RB: relative bias; SE: standard error; MSE: mean square error; CP: coverage probability.

Table 44: Parameter estimates for the N-N and N-Semi distributional models when

 $N = 500, T = 3, C = 20, \sigma_{LS} = 0, \text{ and } \sigma_e^2 = 0.1$

| ± • | 000, 1 | 0, 0 | $=0, \circ_L$ | ω, | una e | | | | | | | |
|---------------|---------------|--------|---------------|-------|-------|-------|--------|--------|----------|-------|-------|-------|
| | | | N-N m | odel | | | | | N-Semi ı | nodel | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.200 | 0.000 | -0.007 | 0.053 | 0.003 | 0.940 | 6.200 | 0.000 | 0.007 | 0.039 | 0.001 | 0.965 |
| β_S | 0.300 | 0.000 | -0.122 | 0.019 | 0.000 | 0.940 | 0.300 | 0.000 | -0.123 | 0.015 | 0.000 | 0.965 |
| σ_L^2 | 1.167 | 0.167 | 16.709 | 2.957 | 8.771 | 0.115 | 1.166 | 0.166 | 16.622 | 2.956 | 8.763 | 0.045 |
| σ_S^2 | 0.099 | -0.001 | -1.129 | 0.116 | 0.013 | 0.155 | 0.099 | -0.001 | -0.563 | 0.117 | 0.014 | 0.100 |
| σ_{LS} | | -0.014 | -1.435 | 0.345 | 0.119 | 0.285 | -0.016 | -0.016 | -1.633 | 0.345 | 0.119 | 0.215 |
| σ_e^2 | 0.098 | -0.002 | -2.071 | 0.006 | 0.000 | 0.915 | 0.097 | -0.003 | -3.354 | 0.006 | 0.000 | 0.875 |
| K_u | - | - | - | - | - | - | 2.793 | - | - | 0.841 | - | - |
| α | - | - | - | - | - | - | 0.962 | -0.038 | -3.771 | 0.009 | 0.001 | 1.000 |

Table 45: Parameter estimates for the N-N and Semi-Semi distributional models when $N=500,\,T=3,\,C=20,\,\sigma_{LS}=0,$ and $\sigma_e^2=0.1$

| | , | , | , 1 | , | e | | | | | | | |
|------------------------------|--------|--------|--------|-------|-------|-------|--------|--------|----------|---------|-------|-------|
| | | | N-N m | odel | | | | | Semi-Sem | i model | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.199 | -0.001 | -0.018 | 0.045 | 0.002 | 0.940 | 6.199 | -0.001 | -0.011 | 0.037 | 0.001 | 0.940 |
| $\frac{\beta_S}{\sigma_I^2}$ | 0.301 | 0.001 | 0.302 | 0.018 | 0.000 | 0.950 | 0.301 | 0.001 | 0.276 | 0.016 | 0.000 | 0.960 |
| σ_L^2 | 0.962 | -0.038 | -3.825 | 1.350 | 1.823 | 0.100 | 0.959 | -0.041 | -4.053 | 1.349 | 1.821 | 0.020 |
| σ_S^2 | 0.112 | 0.012 | 11.563 | 0.146 | 0.022 | 0.140 | 0.111 | 0.011 | 10.508 | 0.146 | 0.022 | 0.085 |
| $\sigma_{LS}^{\ \ \ \ \ }$ | -0.013 | -0.013 | -1.286 | 0.265 | 0.071 | 0.330 | -0.013 | -0.013 | -1.344 | 0.265 | 0.070 | 0.235 |
| σ_e^2 | 0.104 | 0.004 | 3.552 | 0.155 | 0.024 | 0.135 | 0.103 | 0.003 | 2.910 | 0.156 | 0.024 | 0.130 |
| K_e | - | - | - | - | - | - | 6.494 | - | - | 0.876 | - | - |
| K_u | - | - | - | - | - | - | 2.789 | - | - | 0.811 | - | - |
| α_1 | - | - | - | - | - | - | 0.997 | -0.003 | -0.264 | 0.008 | 0.000 | 1.000 |
| α_2 | - | - | - | - | - | - | 0.962 | -0.038 | -3.784 | 0.008 | 0.002 | 1.000 |

Table 46: Parameter estimates for the N-N and Semi-N distributional models when $N=500, T=3, C=20, \sigma_{LS}=0.3,$ and $\sigma_e^2=0.1$

| | | | N-N m | odel | | | | | Semi-N | model | | |
|---------------|-------|--------|---------|-------|-------|-------|-------|--------|---------|-------|-------|-------|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.200 | 0.000 | -0.002 | 0.047 | 0.002 | 0.935 | 6.200 | 0.000 | -0.007 | 0.047 | 0.002 | 0.955 |
| β_S | 0.300 | 0.000 | -0.143 | 0.019 | 0.000 | 0.940 | 0.299 | -0.001 | -0.307 | 0.018 | 0.000 | 0.945 |
| σ_L^2 | 1.018 | 0.018 | 1.766 | 0.068 | 0.005 | 0.960 | 1.017 | 0.017 | 1.674 | 0.068 | 0.005 | 0.960 |
| σ_S^2 | 0.117 | 0.017 | 16.562 | 0.012 | 0.000 | 0.655 | 0.115 | 0.015 | 15.369 | 0.011 | 0.000 | 0.660 |
| σ_{LS} | 0.287 | -0.013 | -4.399 | 0.022 | 0.001 | 0.940 | 0.289 | -0.011 | -3.709 | 0.020 | 0.001 | 0.950 |
| σ_e^2 | 0.088 | -0.012 | -12.356 | 0.084 | 0.007 | 0.090 | 0.088 | -0.012 | -11.571 | 0.086 | 0.008 | 0.085 |
| K_e | - | - | - | - | - | - | 6.609 | - | - | 0.873 | - | - |
| α | - | - | - | - | - | - | 0.998 | -0.002 | -0.163 | 0.009 | 0.000 | 1.000 |

Table 47: Parameter estimates for the N-N and N-Semi distributional models when $N=500, T=3, C=20, \sigma_{LS}=0.3,$ and $\sigma_e^2=0.1$

| | | | N-N m | odel | | | | | N-Semi | model | | |
|---------------------------|-------|--------|---------|-------|-------|-------|-------|--------|---------|-------|-------|-------|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.195 | -0.005 | -0.084 | 0.047 | 0.002 | 0.950 | 6.196 | -0.004 | -0.068 | 0.040 | 0.002 | 0.965 |
| β_S | 0.301 | 0.001 | 0.495 | 0.017 | 0.000 | 0.955 | 0.301 | 0.001 | 0.480 | 0.016 | 0.000 | 0.960 |
| σ_L^2 | 0.970 | -0.030 | -3.020 | 1.354 | 1.833 | 0.075 | 0.968 | -0.032 | -3.153 | 1.354 | 1.833 | 0.025 |
| $\sigma_S^{\overline{2}}$ | 0.113 | 0.013 | 12.612 | 0.130 | 0.017 | 0.185 | 0.112 | 0.012 | 12.014 | 0.130 | 0.017 | 0.120 |
| σ_{LS} | 0.266 | -0.034 | -11.445 | 0.403 | 0.164 | 0.095 | 0.264 | -0.036 | -11.915 | 0.403 | 0.164 | 0.040 |
| σ_e^2 | 0.090 | -0.010 | -9.732 | 0.005 | 0.000 | 0.450 | 0.090 | -0.010 | -10.273 | 0.005 | 0.000 | 0.415 |
| K_u | - | - | - | - | - | - | 2.170 | - | - | 0.612 | - | - |
| α | - | - | - | - | - | - | 0.956 | -0.044 | -4.381 | 0.007 | 0.002 | 1.000 |

Table 48: Parameter estimates for the N-N and Semi-Semi distributional models when $N=500, T=3, C=20, \sigma_{LS}=0.3,$ and $\sigma_e^2=0.1$

| | | | | | | C | | | | | | |
|---------------------------|-------|--------|---------|-------|-------|-------|-------|--------|----------|---------|-------|-------|
| | | | N-N m | odel | | | | | Semi-Sem | i model | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.194 | -0.006 | -0.098 | 0.042 | 0.002 | 0.940 | 6.194 | -0.006 | -0.098 | 0.037 | 0.001 | 0.950 |
| β_{S} | 0.299 | -0.001 | -0.304 | 0.015 | 0.000 | 0.975 | 0.299 | -0.001 | -0.381 | 0.014 | 0.000 | 0.972 |
| σ_L^2 | 0.883 | -0.117 | -11.697 | 1.381 | 1.922 | 0.075 | 0.876 | -0.124 | -12.352 | 1.377 | 1.912 | 0.039 |
| $\sigma_S^{\overline{2}}$ | 0.109 | 0.009 | 8.623 | 0.190 | 0.036 | 0.205 | 0.107 | 0.007 | 7.165 | 0.195 | 0.038 | 0.117 |
| σ_{LS} | 0.251 | -0.049 | -16.286 | 0.503 | 0.255 | 0.070 | 0.251 | -0.049 | -16.191 | 0.508 | 0.261 | 0.022 |
| σ_e^2 | 0.085 | -0.015 | -15.297 | 0.062 | 0.004 | 0.105 | 0.085 | -0.015 | -14.641 | 0.064 | 0.004 | 0.072 |
| K_e | - | - | - | - | - | - | 6.689 | - | - | 0.879 | - | - |
| K_u | - | - | - | - | - | - | 2.200 | - | - | 0.551 | - | - |
| α_1 | - | - | - | - | - | - | 0.999 | -0.001 | -0.106 | 0.009 | 0.000 | 1.000 |
| α_2 | - | - | - | - | - | - | 0.957 | -0.043 | -4.345 | 0.006 | 0.002 | 1.000 |

Table 49: Parameter estimates for the N-N and Semi-N distributional models when $N=500,\,T=5,\,C=20,\,\sigma_{LS}=0,$ and $\sigma_e^2=0.5$

| | , - | ٠, ٠ | , - 1 | 00 0 | , | e | | | | | | |
|---------------------------|-------|--------|---------|-------|-------|-------|-------|--------|---------|-------|-------|-------|
| | | | N-N m | odel | | | | | Semi-N | model | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.195 | -0.005 | -0.075 | 0.047 | 0.002 | 0.970 | 6.196 | -0.004 | -0.067 | 0.047 | 0.002 | 0.965 |
| β_S | 0.299 | -0.001 | -0.266 | 0.016 | 0.000 | 0.940 | 0.299 | -0.001 | -0.280 | 0.016 | 0.000 | 0.940 |
| σ_L^2 | 1.002 | 0.002 | 0.193 | 0.088 | 0.008 | 0.915 | 1.005 | 0.005 | 0.473 | 0.083 | 0.007 | 0.930 |
| $\sigma_S^{\overline{2}}$ | 0.104 | 0.004 | 3.870 | 0.009 | 0.000 | 0.945 | 0.103 | 0.003 | 3.471 | 0.009 | 0.000 | 0.945 |
| σ_{LS} | 0.000 | 0.000 | 0.002 | 0.020 | 0.000 | 0.930 | 0.000 | 0.000 | -0.015 | 0.019 | 0.000 | 0.945 |
| σ_e^2 | 0.441 | -0.059 | -11.825 | 0.349 | 0.126 | 0.095 | 0.441 | -0.059 | -11.879 | 0.349 | 0.125 | 0.075 |
| K_e | - | - | - | - | - | - | 6.911 | - | - | 0.906 | - | - |
| α | - | - | - | - | - | - | 1.001 | 0.001 | 0.119 | 0.009 | 0.000 | 1.000 |

Table 50: Parameter estimates for the N-N and N-Semi distributional models when $N=500,\,T=5,\,C=20,\,\sigma_{LS}=0,$ and $\sigma_e^2=0.5$

| | | | | 1.1 | , | C | | | | | | | | |
|---------------|-------|--------|--------|-------|-------|-------|--------------|--------|--------|-------|-------|-------|--|--|
| | | | N-N m | odel | | | N-Semi model | | | | | | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP | | |
| β_L | 6.199 | -0.001 | -0.021 | 0.050 | 0.002 | 0.950 | 6.198 | -0.002 | -0.030 | 0.047 | 0.002 | 0.950 | | |
| β_S | 0.299 | -0.001 | -0.487 | 0.014 | 0.000 | 0.985 | 0.298 | -0.002 | -0.598 | 0.014 | 0.000 | 0.985 | | |
| σ_L^2 | 1.001 | 0.001 | 0.109 | 1.569 | 2.463 | 0.100 | 1.003 | 0.003 | 0.252 | 1.568 | 2.460 | 0.065 | | |
| σ_S^2 | 0.101 | 0.001 | 0.784 | 0.131 | 0.017 | 0.185 | 0.101 | 0.001 | 0.633 | 0.131 | 0.017 | 0.160 | | |
| σ_{LS} | 0.019 | 0.019 | 1.898 | 0.284 | 0.081 | 0.325 | 0.016 | 0.016 | 1.599 | 0.283 | 0.080 | 0.255 | | |
| σ_e^2 | 0.497 | -0.003 | -0.648 | 0.019 | 0.000 | 0.935 | 0.495 | -0.005 | -1.060 | 0.019 | 0.000 | 0.930 | | |
| K_u | - | - | - | - | - | - | 2.858 | - | - | 0.780 | - | - | | |
| α | - | - | - | - | - | - | 0.963 | -0.037 | -3.675 | 0.007 | 0.001 | 1.000 | | |

Table 51: Parameter estimates for the N-N and Semi-Semi distributional models when

 $\frac{N=500, T=5, C=20, \sigma_{LS}=0, \text{ and } \sigma_e^2=0.5}{\frac{\text{N-N model}}{\text{ESL}} \frac{\text{N-RB}\left(\%\right) \text{ SE MSE CP}}}$

| | N-N model | | | | | | | Semi-Semi model | | | | | | |
|------------------------------------|-----------|--------|--------|-------|-------|-------|--------|-----------------|--------|-------|-------|-------|--|--|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP | | |
| β_L | 6.192 | -0.008 | -0.127 | 0.049 | 0.002 | 0.945 | 6.194 | -0.006 | -0.094 | 0.042 | 0.002 | 0.955 | | |
| β_S | 0.302 | 0.002 | 0.543 | 0.021 | 0.000 | 0.955 | 0.301 | 0.001 | 0.190 | 0.018 | 0.000 | 0.955 | | |
| $\frac{\beta_S}{\sigma_L^2}$ | 0.985 | -0.015 | -1.523 | 1.312 | 1.722 | 0.095 | 0.982 | -0.018 | -1.829 | 1.313 | 1.725 | 0.055 | | |
| σ_S^2 | 0.127 | 0.027 | 26.656 | 0.242 | 0.059 | 0.125 | 0.125 | 0.025 | 24.758 | 0.242 | 0.059 | 0.070 | | |
| σ_{LS} | -0.056 | -0.056 | -5.633 | 0.401 | 0.164 | 0.295 | -0.056 | -0.056 | -5.647 | 0.400 | 0.163 | 0.250 | | |
| $\sigma_{LS} \\ \sigma_e^2 \\ K_e$ | 0.489 | -0.011 | -2.162 | 0.368 | 0.136 | 0.060 | 0.489 | -0.011 | -2.287 | 0.369 | 0.136 | 0.040 | | |
| K_e | - | - | - | - | - | - | 6.790 | - | - | 0.983 | - | - | | |
| K_u | - | - | - | - | - | - | 2.889 | - | - | 0.886 | - | - | | |
| α_1 | - | - | - | - | - | - | 1.000 | 0.000 | 0.009 | 0.009 | 0.000 | 1.000 | | |
| α_2 | - | - | - | - | - | - | 0.964 | -0.036 | -3.612 | 0.010 | 0.001 | 1.000 | | |

Table 52: Parameter estimates for the N-N and Semi-N distributional models when $N=500, T=5, C=20, \sigma_{LS}=0.3$, and $\sigma_{c}^{2}=0.5$

| 4 1 | 000, 1 | 0, 0 | - 0, 0 1 | 79 C | .o, una | e 0.0 | | | | | | |
|---------------|--------|--------|-----------------|-------|---------|--------------|-------|--------|---------|-------|-------|-------|
| | | | N-N m | odel | | Semi-N model | | | | | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.195 | -0.005 | -0.079 | 0.047 | 0.002 | 0.965 | 6.195 | -0.005 | -0.076 | 0.046 | 0.002 | 0.955 |
| β_S | 0.298 | -0.002 | -0.720 | 0.016 | 0.000 | 0.970 | 0.298 | -0.002 | -0.647 | 0.015 | 0.000 | 0.965 |
| σ_L^2 | 1.044 | 0.044 | 4.403 | 0.088 | 0.010 | 0.905 | 1.041 | 0.041 | 4.092 | 0.085 | 0.009 | 0.915 |
| σ_S^2 | 0.115 | 0.015 | 15.442 | 0.011 | 0.000 | 0.650 | 0.114 | 0.014 | 13.531 | 0.010 | 0.000 | 0.680 |
| σ_{LS} | 0.279 | -0.021 | -6.881 | 0.025 | 0.001 | 0.785 | 0.282 | -0.018 | -5.847 | 0.024 | 0.001 | 0.815 |
| σ_e^2 | 0.424 | -0.076 | -15.130 | 0.340 | 0.121 | 0.060 | 0.426 | -0.074 | -14.774 | 0.344 | 0.124 | 0.040 |
| K_e | - | - | - | - | - | - | 6.939 | - | - | 0.946 | - | - |
| α | - | - | - | - | - | - | 1.001 | 0.001 | 0.148 | 0.009 | 0.000 | 1.000 |

Table 53: Parameter estimates for the N-N and N-Semi distributional models when $N=500, T=5, C=20, \sigma_{LS}=0.3,$ and $\sigma_e^2=0.5$

| | / | - , - | | 10 - | -, | - е | | | | | | | | | | |
|---------------|-----------|--------|---------|-------|-------|-------|-------|--------|--------------|-------|-------|-------|--|--|--|--|
| | N-N model | | | | | | | | N-Semi model | | | | | | | |
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP | | | | |
| β_L | 6.196 | -0.004 | -0.062 | 0.054 | 0.003 | 0.945 | 6.195 | -0.005 | -0.082 | 0.049 | 0.002 | 0.945 | | | | |
| β_S | 0.297 | -0.003 | -0.875 | 0.016 | 0.000 | 0.975 | 0.297 | -0.003 | -0.960 | 0.015 | 0.000 | 0.965 | | | | |
| σ_L^2 | 1.053 | 0.053 | 5.340 | 1.520 | 2.314 | 0.125 | 1.054 | 0.054 | 5.381 | 1.519 | 2.311 | 0.090 | | | | |
| σ_S^2 | 0.111 | 0.011 | 10.783 | 0.134 | 0.018 | 0.175 | 0.110 | 0.010 | 10.455 | 0.134 | 0.018 | 0.135 | | | | |
| σ_{LS} | 0.264 | -0.036 | -12.104 | 0.432 | 0.188 | 0.065 | 0.260 | -0.040 | -13.169 | 0.431 | 0.187 | 0.020 | | | | |
| σ_e^2 | 0.480 | -0.020 | -3.938 | 0.017 | 0.001 | 0.765 | 0.479 | -0.021 | -4.205 | 0.017 | 0.001 | 0.725 | | | | |
| K_u | - | - | - | - | - | - | 2.508 | - | - | 0.516 | - | - | | | | |
| α | - | - | - | - | - | - | 0.960 | -0.040 | -3.966 | 0.005 | 0.002 | 1.000 | | | | |

Table 54: Parameter estimates for the N-N and Semi-Semi distributional models when $N=500, T=5, C=20, \sigma_{LS}=0.3, \text{ and } \sigma_e^2=0.5$

| | | | N-N m | odel | | Semi-Semi model | | | | | | |
|---------------------------|-------|--------|--------|-------|-------|-----------------|-------|--------|--------|-------|-------|-------|
| | Est. | AB | RB (%) | SE | MSE | CP | Est. | AB | RB (%) | SE | MSE | CP |
| β_L | 6.195 | -0.005 | -0.078 | 0.053 | 0.003 | 0.960 | 6.196 | -0.004 | -0.071 | 0.040 | 0.002 | 0.970 |
| β_S | 0.298 | -0.002 | -0.589 | 0.018 | 0.000 | 0.960 | 0.299 | -0.001 | -0.476 | 0.014 | 0.000 | 0.975 |
| $rac{eta_S}{\sigma_L^2}$ | 1.126 | 0.126 | 12.568 | 1.854 | 3.454 | 0.075 | 1.119 | 0.119 | 11.930 | 1.852 | 3.445 | 0.035 |
| σ_S^{L} | 0.137 | 0.037 | 36.898 | 0.262 | 0.070 | 0.155 | 0.134 | 0.034 | 34.302 | 0.262 | 0.070 | 0.080 |
| σ_{LS} | 0.318 | 0.018 | 6.113 | 0.680 | 0.463 | 0.070 | 0.319 | 0.019 | 6.382 | 0.679 | 0.461 | 0.025 |
| σ_e^2 | 0.475 | -0.025 | -4.944 | 0.363 | 0.133 | 0.060 | 0.476 | -0.024 | -4.846 | 0.366 | 0.134 | 0.025 |
| K_e | - | - | - | - | - | - | 6.809 | - | - | 0.957 | - | - |
| K_u | - | - | - | - | - | - | 2.463 | - | - | 0.731 | - | - |
| α_1 | - | - | - | - | - | - | 1.000 | 0.000 | 0.024 | 0.009 | 0.000 | 1.000 |
| α_2 | - | - | - | - | - | - | 0.961 | -0.039 | -3.944 | 0.009 | 0.002 | 1.000 |