

Table 1: Mean squared errors and coverage probabilities for different data and models ($T = 3$, $C = 5$, $\sigma_{LS} = 0$, $\sigma_e^2 = 0.1$)

		N=50				N=200				N=500			
		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi	
		MSE	CP			MSE	CP			MSE	CP		
Semi-N data	MSE	0.014	0.014	0.013		0.004	0.004	0.004		0.002	0.002	0.002	
	CP	0.970	0.803	0.816		0.955	0.792	0.804		0.944	0.794	0.799	
N-Semi data	MSE	0.009	0.006	0.006		0.065	0.001	0.001		0.006	0.000	0.000	
	CP	0.937	0.958	0.940		0.900	0.933	0.915		0.897	0.927	0.902	
Semi-Semi data	MSE	0.009	0.007	0.007		0.003	0.002	0.002		0.001	0.001	0.001	
	CP	0.965	0.970	0.970		0.968	0.975	0.965		0.953	0.945	0.943	

Note. MSE: mean square error; CP: coverage probability. In the table, on the rows are the different types of generated data with sample size = 50, 200, and 500. On the columns are the four types of distributional models used to analyze the generated data. For each type of the generated data, four distributional models are fitted to them. The average MSE and CP for the six model parameters (β_L , β_S , σ_L^2 , σ_S^2 , σ_{LS} , σ_e^2) are obtained, as displayed in the table.

Table 2: Mean squared errors and coverage probabilities for different data and models ($T = 3$, $C = 5$, $\sigma_{LS} = 0$, $\sigma_e^2 = 0.5$)

		N=50				N=200				N=500			
		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi	
Semi-N data	MSE	0.031	0.055	0.033		0.006	0.007	0.007		0.003	0.005	0.003	
	CP	0.955	0.849	0.876		0.946	0.869	0.879		0.942	0.842	0.879	
N-Semi data	MSE	0.016	0.013	0.013		0.004	0.003	0.003		0.060	0.002	0.002	
	CP	0.893	0.913	0.872		0.882	0.918	0.872		0.827	0.860	0.802	
Semi-Semi data	MSE	0.012	0.012	0.012		0.004	0.004	0.004		0.001	0.001	0.001	
	CP	0.983	0.975	0.983		0.948	0.943	0.948		0.955	0.950	0.955	

Table 3: Mean squared errors and coverage probabilities for different data and models ($T = 3$, $C = 5$, $\sigma_{LS} = 0.3$, $\sigma_e^2 = 0.1$)

		N=50				N=200				N=500			
		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi	
		MSE	CP										
Semi-N data	MSE	0.019	0.018	0.018		0.004	0.005	0.004		0.002	0.002	0.002	
	CP	0.915	0.672	0.684		0.894	0.636	0.637		0.881	0.604	0.614	
N-Semi data	MSE	0.007	0.006	0.006		0.002	0.001	0.001		0.002	0.001	0.001	
	CP	0.905	0.923	0.907		0.782	0.832	0.777		0.712	0.753	0.692	
Semi-Semi data	MSE	0.013	0.011	0.011		0.003	0.003	0.003		0.001	0.001	0.001	
	CP	0.958	0.970	0.965		0.948	0.950	0.948		0.943	0.943	0.950	

Table 4: Mean squared errors and coverage probabilities for different data and models ($T = 3$, $C = 5$, $\sigma_{LS} = 0.3$, $\sigma_e^2 = 0.5$)

		N=50				N=200				N=500			
		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi	
Semi-N data	MSE	0.030	0.060	0.030		0.008	0.016	0.009		0.004	0.010	0.004	
	CP	0.859	0.706	0.719		0.804	0.636	0.655		0.779	0.597	0.626	
N-Semi data	MSE	0.040	0.014	0.014		0.028	0.003	0.003		0.010	0.002	0.002	
	CP	0.897	0.928	0.888		0.840	0.893	0.828		0.775	0.818	0.735	
Semi-Semi data	MSE	0.023	0.022	0.021		0.004	0.004	0.004		0.001	0.001	0.001	
	CP	0.965	0.968	0.970		0.953	0.955	0.950		0.970	0.968	0.963	

Table 5: Mean squared errors and coverage probabilities for different data and models ($T = 5$, $C = 5$, $\sigma_{LS} = 0$, $\sigma_e^2 = 0.1$)

		N=50				N=200				N=500			
		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi	
Semi-N data	MSE	0.016	0.015	0.015		0.004	0.004	0.004		0.002	0.002	0.002	
	CP	0.957	0.672	0.674		0.953	0.677	0.686		0.934	0.642	0.642	
N-Semi data	MSE	0.009	0.007	0.007		0.003	0.001	0.001		0.001	0.001	0.001	
	CP	0.892	0.940	0.885		0.882	0.943	0.893		0.903	0.948	0.907	
Semi-Semi data	MSE	0.013	0.008	0.008		0.003	0.002	0.002		0.001	0.001	0.001	
	CP	0.965	0.973	0.970		0.968	0.975	0.973		0.943	0.960	0.955	

Table 6: Mean squared errors and coverage probabilities for different data and models ($T = 5$, $C = 5$, $\sigma_{LS} = 0$, $\sigma_e^2 = 0.5$)

		N=50				N=200				N=500			
		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi	
		MSE	CP										
Semi-N data	MSE	0.021	0.021	0.020		0.006	0.006	0.006		0.002	0.002	0.002	
	CP	0.953	0.845	0.841		0.939	0.822	0.819		0.946	0.833	0.827	
N-Semi data	MSE	0.018	0.008	0.008		0.003	0.002	0.002		0.002	0.001	0.001	
	CP	0.870	0.948	0.872		0.868	0.938	0.865		0.872	0.937	0.870	
Semi-Semi data	MSE	0.015	0.011	0.011		0.004	0.003	0.003		0.001	0.001	0.001	
	CP	0.970	0.968	0.968		0.948	0.960	0.953		0.953	0.960	0.958	

Table 7: Mean squared errors and coverage probabilities for different data and models ($T = 5$, $C = 5$, $\sigma_{LS} = 0.3$, $\sigma_e^2 = 0.1$)

		N=50				N=200				N=500			
		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi	
Semi-N data	MSE	0.017	0.016	0.016		0.004	0.012	0.003		0.002	0.002	0.002	
	CP	0.934	0.598	0.594		0.946	0.608	0.608		0.937	0.587	0.587	
N-Semi data	MSE	0.006	0.005	0.005		0.002	0.001	0.001		0.001	0.001	0.001	
	CP	0.877	0.938	0.877		0.817	0.913	0.827		0.752	0.852	0.737	
Semi-Semi data	MSE	0.010	0.009	0.008		0.003	0.002	0.002		0.001	0.001	0.001	
	CP	0.958	0.960	0.958		0.948	0.950	0.948		0.955	0.958	0.955	

Table 8: Mean squared errors and coverage probabilities for different data and models ($T = 5$, $C = 5$, $\sigma_{LS} = 0.3$, $\sigma_e^2 = 0.5$)

		N=50				N=200				N=500			
		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi	
		MSE	CP										
Semi-N data	MSE	0.024	0.024	0.022		0.005	0.006	0.005		0.002	0.035	0.002	
	CP	0.907	0.696	0.704		0.882	0.677	0.687		0.884	0.647	0.672	
N-Semi data	MSE	0.013	0.008	0.008		0.005	0.002	0.002		0.007	0.001	0.001	
	CP	0.888	0.962	0.887		0.812	0.935	0.807		0.757	0.865	0.753	
Semi-Semi data	MSE	0.010	0.009	0.009		0.005	0.003	0.002		0.001	0.001	0.001	
	CP	0.975	0.975	0.973		0.965	0.955	0.958		0.960	0.983	0.975	

Table 9: Mean squared errors and coverage probabilities for different data and models ($T = 3$, $C = 20$, $\sigma_{LS} = 0$, $\sigma_e^2 = 0.1$)

		N=50				N=200				N=500			
		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi	
		MSE	CP			0.017	0.016	0.016		0.004	0.004	0.004	
Semi-N data	MSE	0.962	0.784	0.792		0.951	0.784	0.793		0.951	0.784	0.791	
	CP												
N-Semi data	MSE	0.009	0.007	0.007		0.010	0.002	0.002		0.020	0.001	0.001	
	CP	0.925	0.943	0.932		0.897	0.922	0.900		0.872	0.935	0.910	
Semi-Semi data	MSE	0.010	0.009	0.009		0.003	0.002	0.002		0.001	0.001	0.001	
	CP	0.940	0.948	0.945		0.955	0.955	0.958		0.948	0.950	0.950	

Note. MSE: mean square error; CP: coverage probability. In the table, on the rows are the different types of generated data with sample size = 50, 200, and 500. On the columns are the four types of distributional models used to analyze the generated data. For each type of the generated data, four distributional models are fitted to them. The average MSE and CP for the six model parameters ($\beta_L, \beta_S, \sigma_L^2, \sigma_S^2, \sigma_{LS}, \sigma_e^2$) are obtained, as displayed in the table.

Table 10: Mean squared errors and coverage probabilities for different data and models ($T = 3$, $C = 20$, $\sigma_{LS} = 0$, $\sigma_e^2 = 0.5$)

		N=50				N=200				N=500			
		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi	
		MSE	CP			MSE	CP			MSE	CP		
Semi-N data	MSE	0.034	0.045	0.036		0.006	0.009	0.006		0.003	0.004	0.003	
	CP	0.957	0.863	0.877		0.956	0.874	0.894		0.942	0.843	0.876	
N-Semi data	MSE	0.024	0.011	0.011		0.028	0.004	0.004		0.007	0.001	0.001	
	CP	0.923	0.947	0.913		0.868	0.913	0.875		0.855	0.888	0.832	
Semi-Semi data	MSE	0.014	0.014	0.012		0.003	0.003	0.003		0.002	0.001	0.001	
	CP	0.978	0.980	0.983		0.948	0.953	0.955		0.943	0.948	0.945	

Table 11: Mean squared errors and coverage probabilities for different data and models ($T = 3$, $C = 20$, $\sigma_{LS} = 0.3$, $\sigma_e^2 = 0.1$)

		N=50				N=200				N=500			
		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi	
Semi-N data	MSE	0.016	0.015	0.015		0.004	0.004	0.004		0.002	0.002	0.002	
	CP	0.910	0.670	0.674		0.905	0.662	0.659		0.894	0.617	0.609	
N-Semi data	MSE	0.019	0.007	0.007		0.012	0.001	0.001		0.005	0.001	0.001	
	CP	0.895	0.913	0.895		0.775	0.835	0.777		0.747	0.780	0.728	
Semi-Semi data	MSE	0.009	0.008	0.008		0.003	0.002	0.002		0.001	0.001	0.001	
	CP	0.985	0.980	0.980		0.960	0.965	0.963		0.973	0.958	0.961	

Table 12: Mean squared errors and coverage probabilities for different data and models ($T = 3, C = 20, \sigma_{LS} = 0.3, \sigma_e^2 = 0.5$)

		N=50			N=200			N=500		
		Semi-N	N-Semi	Semi-Semi	Semi-N	N-Semi	Semi-Semi	Semi-N	N-Semi	Semi-Semi
		MSE	CP							
Semi-N data	MSE	0.031	0.038	0.032	0.007	0.014	0.008	0.004	0.010	0.005
	CP	0.857	0.705	0.714	0.819	0.649	0.671	0.772	0.614	0.617
N-Semi data	MSE	0.015	0.013	0.013	0.042	0.003	0.003	0.009	0.002	0.002
	CP	0.887	0.927	0.873	0.857	0.897	0.833	0.791	0.833	0.755
Semi-Semi data	MSE	0.016	0.014	0.013	0.003	0.003	0.003	0.002	0.002	0.002
	CP	0.975	0.980	0.975	0.963	0.968	0.958	0.956	0.955	0.955

Table 13: Mean squared errors and coverage probabilities for different data and models ($T = 5$, $C = 20$, $\sigma_{LS} = 0$, $\sigma_e^2 = 0.1$)

		N=50				N=200				N=500			
Semi-N data	MSE CP	Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi	
		0.016 0.950	0.015 0.675	0.015 0.684		0.004 0.947	0.004 0.683	0.004 0.676		0.001 0.944	0.001 0.655	0.001 0.659	
N-Semi data	MSE	0.010	0.005	0.005		0.034	0.001	0.001		0.025	0.001	0.001	
	CP	0.903	0.958	0.908		0.930	0.963	0.927		0.878	0.952	0.900	
Semi-Semi data	MSE	0.009	0.007	0.007		0.003	0.002	0.002		0.001	0.001	0.001	
	CP	0.978	0.973	0.978		0.953	0.958	0.960		0.960	0.960	0.963	

Table 14: Mean squared errors and coverage probabilities for different data and models ($T = 5$, $C = 20$, $\sigma_{LS} = 0$, $\sigma_e^2 = 0.5$)

		N=50				N=200				N=500			
		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi	
		MSE											
Semi-N data	MSE	0.022	0.022	0.021		0.005	0.007	0.005		0.002	0.002	0.002	
	CP	0.957	0.836	0.831		0.951	0.840	0.852		0.945	0.835	0.838	
N-Semi data	MSE	0.010	0.009	0.008		0.103	0.002	0.002		0.024	0.001	0.001	
	CP	0.900	0.960	0.900		0.865	0.941	0.870		0.863	0.955	0.880	
Semi-Semi data	MSE	0.013	0.012	0.012		0.004	0.003	0.003		0.001	0.001	0.001	
	CP	0.968	0.963	0.968		0.935	0.940	0.938		0.958	0.948	0.955	

Table 15: Mean squared errors and coverage probabilities for different data and models ($T = 5$, $C = 20$, $\sigma_{LS} = 0.3$, $\sigma_e^2 = 0.1$)

		N=50			N=200			N=500		
		Semi-N	N-Semi	Semi-Semi	Semi-N	N-Semi	Semi-Semi	Semi-N	N-Semi	Semi-Semi
Semi-N data	MSE	0.013	0.012	0.012	0.004	0.004	0.004	0.001	0.002	0.001
	CP	0.952	0.613	0.609	0.936	0.604	0.607	0.938	0.614	0.611
N-Semi data	MSE	0.008	0.006	0.006	0.015	0.003	0.005	0.003	0.001	0.001
	CP	0.855	0.937	0.865	0.813	0.922	0.804	0.767	0.867	0.753
Semi-Semi data	MSE	0.011	0.009	0.008	0.002	0.002	0.002	0.001	0.001	0.001
	CP	0.968	0.960	0.968	0.960	0.958	0.968	0.968	0.958	0.963

Table 16: Mean squared errors and coverage probabilities for different data and models ($T = 5$, $C = 20$, $\sigma_{LS} = 0.3$, $\sigma_e^2 = 0.5$)

		N=50				N=200				N=500			
		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi		Semi-N	N-Semi	Semi-Semi	
		MSE	CP										
Semi-N data	MSE	0.022	0.023	0.020		0.006	0.009	0.006		0.002	0.003	0.002	
	CP	0.889	0.690	0.695		0.881	0.656	0.671		0.866	0.649	0.664	
N-Semi data	MSE	0.009	0.009	0.009		0.003	0.002	0.002		0.003	0.001	0.001	
	CP	0.872	0.948	0.870		0.831	0.925	0.832		0.775	0.878	0.755	
Semi-Semi data	MSE	0.012	0.011	0.010		0.004	0.003	0.003		0.001	0.001	0.001	
	CP	0.990	0.985	0.988		0.958	0.948	0.955		0.970	0.973	0.973	