Mobile robot seminar Ch4. Mobile robot

학부 연구생 이태연



Mobile Robot??

One of the most important functions of a mobile robot is to move to some place

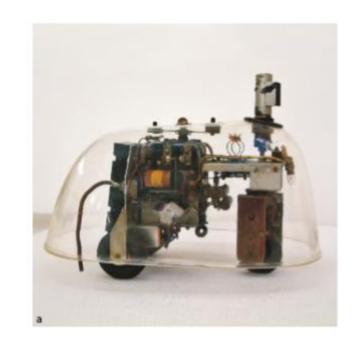
- 1. move to the light
- 2. in terms of some geometric coordinate or map reference

들어가기 전..

Mobile Robot??

Elsie the robotic tortoise (move to the light)

-> reactive approach





robot Shakey

(in terms of some geometric coordinate or map reference)

->An alternative to the reactive approach

들어가기전..

접근법의 차이

Reactive systeme robotic tortoise

지각하는 시스템은 행동과 연결되어 있어서 빠르고 단순하다.

때문에, 세계를 표현하고 유지할 resource가 필요하지 않고 추론할 능력도 필요하지 않음.

3D perception and created a map

맵을 만들고 그에 대해 추론하는 시스템은 더 많은 resource를 필요로 하지만 더 복잡한 작업을 수행할 수 있다.

These two approaches exemplify opposite ends of the spectrum for mobile robot navigation



Mobile Robot??



Mobile Robot 대표 종류

a. Floor

b. Sensor

들어가기 전..

Mobile Robot??



모바일 로봇은 지상에서만 운용되는 것이 아니다. 무인기(UAV), 자율 수중 차량(AUV), 자율 표면 차량(ASV) 로봇보트

들어가기 전..

Mobile Robot??



Mars Science Laboratory (MSL) rover, known as Curiosity/ 항만의 컨테이너 운송 차량/ 광산의 트럭/ 광대한 에이커 농업을 위한 자율주행 트랙터와 같은 현장 로봇 시스템은 이제 다양한 용도에 상업적으로 이용 가능하다.

앞으로 4장에서 다룰 내용들..

Mobile Robot의 기본 원리



Wheeled Mobile Robots



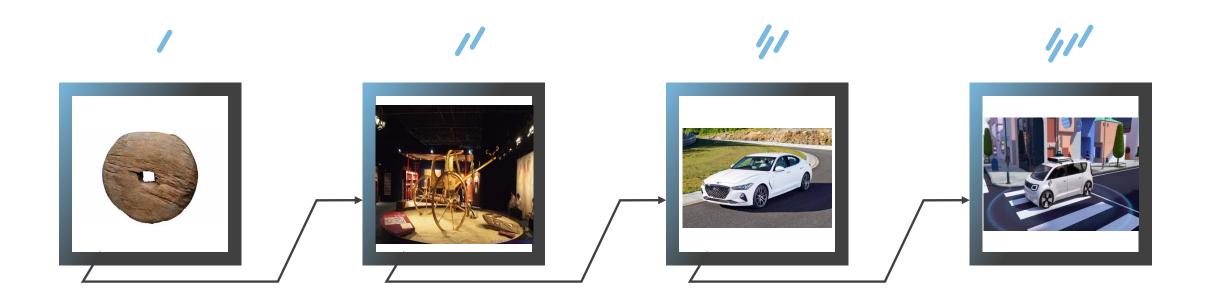
Flying Robot



Advanced Topics

Wheel mobile Robot

Enjoy your stylish business and campus life with BIZCAM



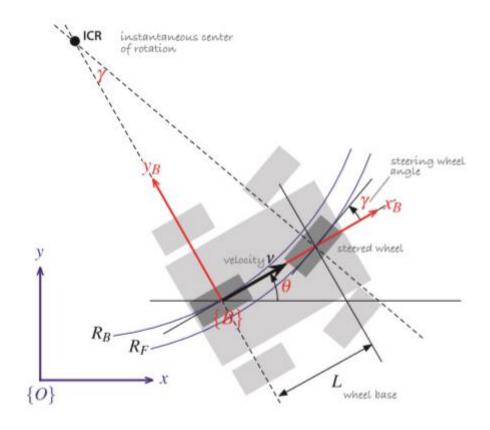
바퀴 이륜카트 사륜 자동차

Choice for Robot Platform

It's not possible to drive sideways.

Can't rotate a car on the spot.

Mobile Robot??



$$q = (x, y, \theta) \in \mathcal{C}$$
 where $\mathcal{C} \subset \mathbb{R}^2 \times \mathbb{S}^1$.

$$^{B}\mathbf{v}=(v,0)$$

{B}:The pose of the vehicle

Symbol	Description	Unit
G	configuration space of a robot with N joints: $\mathfrak{C} \subset \mathbb{R}^N$	
\mathbb{R}	set of real numbers	
\mathbb{R}^2	set of all 2-D points	
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S	Laplace transform operator	
\mathbb{S}^1	unit circle, set of angles $[0, 2\pi)$	

4.1.1 Car-Like Mobil Motion Planning 개념

Work Space(or Task Space)

2D 또는 3D 유클리드 공간에서 로봇 의 상태를 설명함.

즉, 실제 작업이 이루어 져야하는 x,y,z 의 공간을 작업공간(Task Space)라

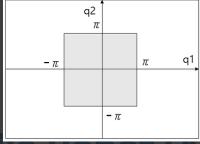
부르고,



Configuration Space of a robot with N joints: $C \subset \mathbb{R}^N$ Configuration Space(or Joint Space)

set of all 2-D points

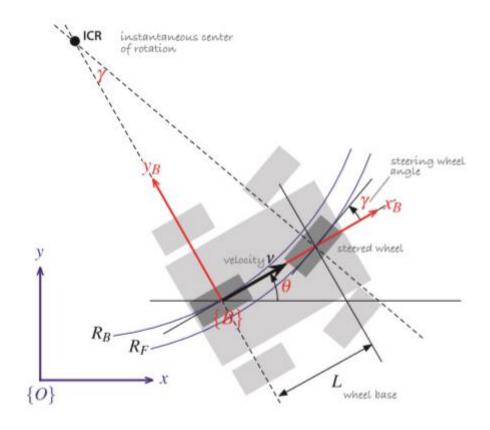
로봇이 제어되는 각 관절 각도(q1,...,qn)에 대한 공간을 관절공간(Joint Space)라고 부 릅니다.



Mobile Kopot 네표 종류

결국 로봇의 움직임 생성 문제란 "작업공간에서 잘 움직이 도록 관절공간에서 잘 입력을 넣어주는 것"이라고 일반화 (=(x,y,0) ∈ C where C ⊂ R × S) 시킬 수 있습니다.

Mobile Robot??



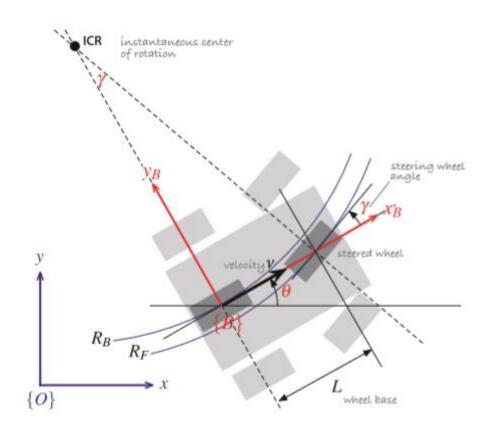
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Mobile Robot??

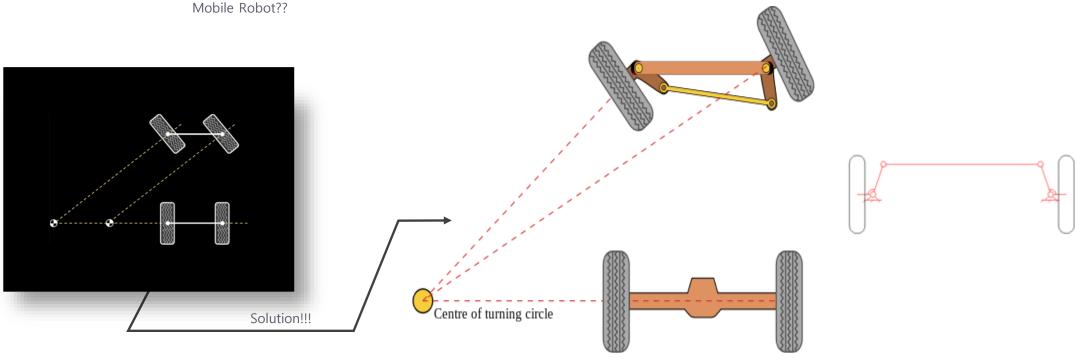


$$q = (x, y, \theta) \in \mathcal{C}$$
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$$^{B}v = (v,0)$$
 {B}:The pose of the vehicle

각속도
$$\theta = \frac{v}{R_B}$$
 회전반경 $R_B = L/\tan\gamma$ 경로길이 $R_F > R_B$

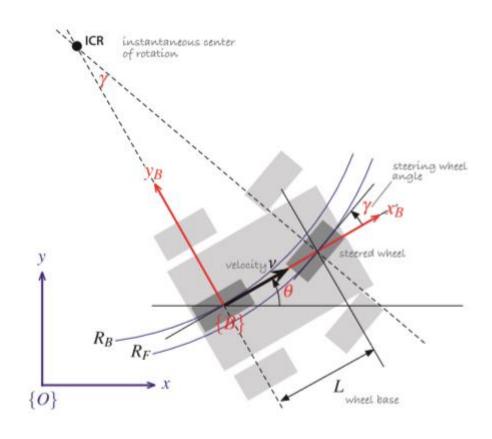
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Ackermann Steering Geometry?

When a four-wheeled vehicle goes around a corner the two steered wheels follow circular paths of different radii and therefore the angles of the steered wheels γ L and γ R should be very slightly different.

Mobile Robot??



$$q = (x, y, \theta) \in \mathcal{C}$$
 where $\mathcal{C} \subset \mathbb{R}^2 \times \mathbb{S}^1$.

 $^{B}v = (v,0)$ {B}:The pose of the vehicle

각속도
$$\dot{\theta} = \frac{v}{R_B}$$

회전반경 $R_{\rm B} = L/\tan \gamma$

경로길이 $R_{\rm F} > R_{\rm B}$

속도및

$$\dot{x} = v \cos \theta$$

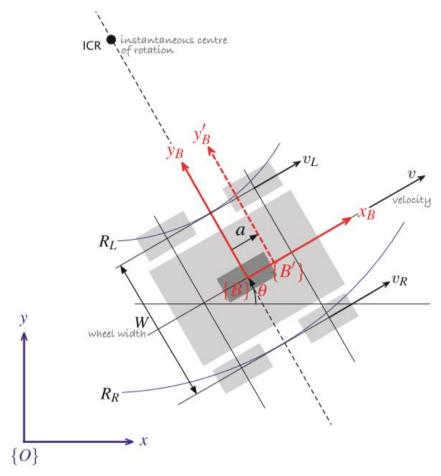
$$\dot{y} = v \sin \theta$$

$$\dot{\theta} = \frac{v}{I} \tan \gamma$$

호전육 $\dot{\theta} = \frac{v}{L} \tan \gamma$ Y방향 속도 $\dot{y} \cos \theta - \dot{x} \sin \theta \equiv 0$

Symbol	Description	Unit
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Mobile Robot??



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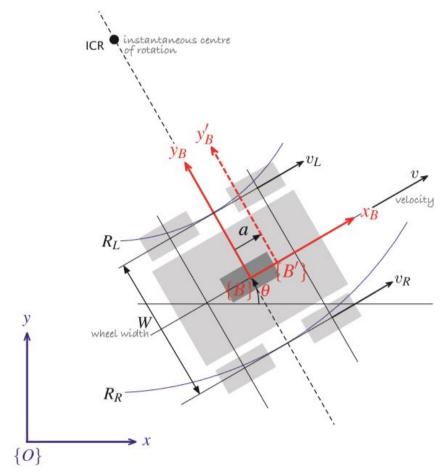
$$^{B}v=(v,0)$$

{B}:Frame, pose of the vehicle

{B'}: for trajectory tracking control

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Mobile Robot??



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$$^{B}v = (v, 0)$$

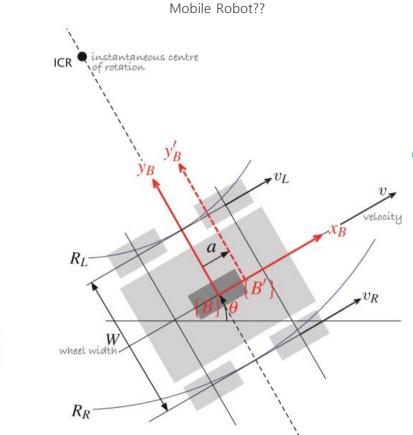
{B}:Frame, pose of the vehicle

{B'}: for trajectory tracking control

{B}에서의 각속도
$$\dot{\theta} = \frac{v_L}{R_L} = \frac{v_R}{R_R}$$

$$egin{aligned} R_R &= R_L + W \ O$$
 $\dot{ heta} &= rac{v_R - v_L}{W} \ \dot{ heta} &= rac{\dot{x} = v \cos heta}{\dot{y} = v \sin heta} \ \dot{ heta} &= rac{v_\Delta}{W} \end{aligned}$

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$$q = (x, y, \theta) \in \mathbb{C}$$
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{0}

$$^{B}v=(v,0)$$

{B}:Frame, pose of the vehicle

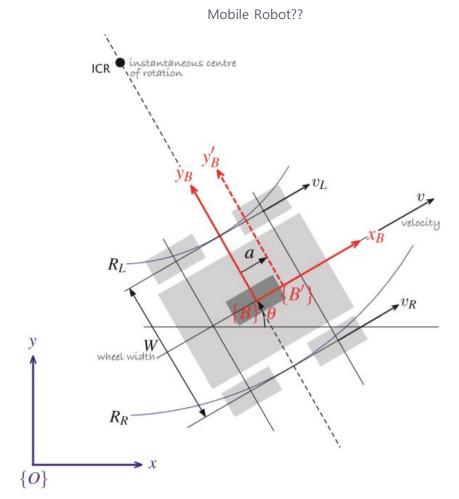
{B'}: for trajectory tracking control

{B}에서의 각속도
$$\dot{\theta} = \frac{v_L}{R_L} = \frac{v_R}{R_R}$$
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운동방정식

$$\dot{x} = v\cos\theta$$
$$\dot{y} = v\sin\theta$$
$$\dot{\theta} = \frac{v_{\Delta}}{W}$$

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$$\dot{\theta} = \frac{v_L}{R_L} = \frac{v_R}{R_R}$$
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운동방정식

유사점과 차이점?

$$\dot{x} = v\cos\theta$$

$$\dot{y} = v\sin\theta$$

$$\dot{\theta} = \frac{v_{\Delta}}{W}$$

$$\dot{x} = v\cos\theta$$

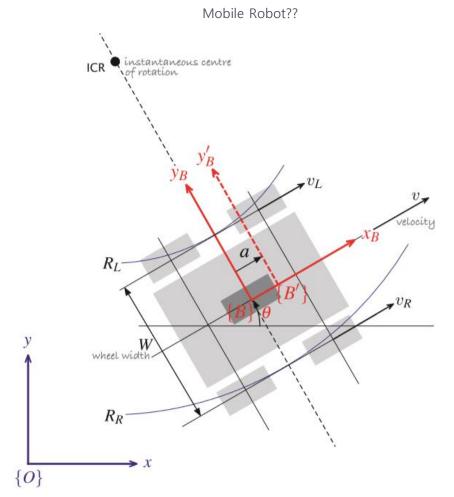
$$\dot{y} = v\sin\theta$$

$$\dot{\theta} = \frac{v_{\Delta}}{L}\tan\gamma$$

Differentially-Steered Vehicle

Car-Like Mobile Robots

Symbol	Description	Unit
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{B}에서의 각속도
$$\dot{\theta} = \frac{v_L}{R_L} = \frac{v_R}{R_R}$$
 $\dot{\theta} = \frac{v_R - v_L}{W}$

$$\dot{y}\cos\theta - \dot{x}\sin\theta \equiv 0$$

$$\dot{x} = v\cos\theta$$

$$\dot{y} = v\sin\theta$$

$$\dot{\theta} = \frac{v_{\Delta}}{W}$$

$$\dot{x} = v\cos\theta$$

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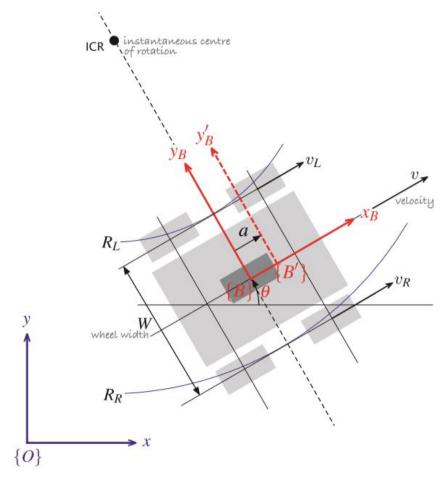
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Differentially-Steered Vehicle

Car-Like Mobile Robots

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Mobile Robot??



$$q = (x, y, \theta) \in \mathbb{C}$$
 where $\mathbb{C} \subset \mathbb{R}^2 \times \mathbb{S}^1$.

운동방정식

$$\dot{x} = v \cos \theta$$
 $\dot{y} = v \sin \theta$ — Matrix Form!! $\dot{\theta} = \frac{v_{\Delta}}{W}$

Differentially-Steered Vehicle

If we move the vehicle's reference frame to $\{B'\}$ and ignore orientation we can rewrite Eq. 4.5 in matrix form as

$$\begin{pmatrix} \dot{x} \\ \dot{y} \end{pmatrix} = \begin{pmatrix} \cos \theta & -a \sin \theta \\ \sin \theta & a \cos \theta \end{pmatrix} \begin{pmatrix} v \\ \omega \end{pmatrix}$$

and if $a \neq 0$ this can be be inverted

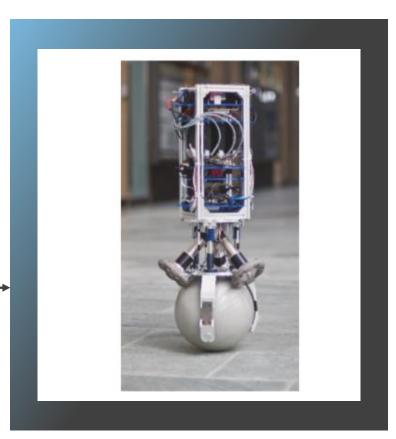
$$\begin{pmatrix} v \\ \omega \end{pmatrix} = \begin{pmatrix} \cos\theta & \sin\theta \\ -\frac{1}{a}\sin\theta & \frac{1}{a}\cos\theta \end{pmatrix} \begin{pmatrix} \dot{x} \\ \dot{y} \end{pmatrix}$$
 (4.7)

to give the required forward speed and turn rate to achieve an arbitrary velocity (\dot{x}, \dot{y}) for the origin of frame $\{B'\}$.

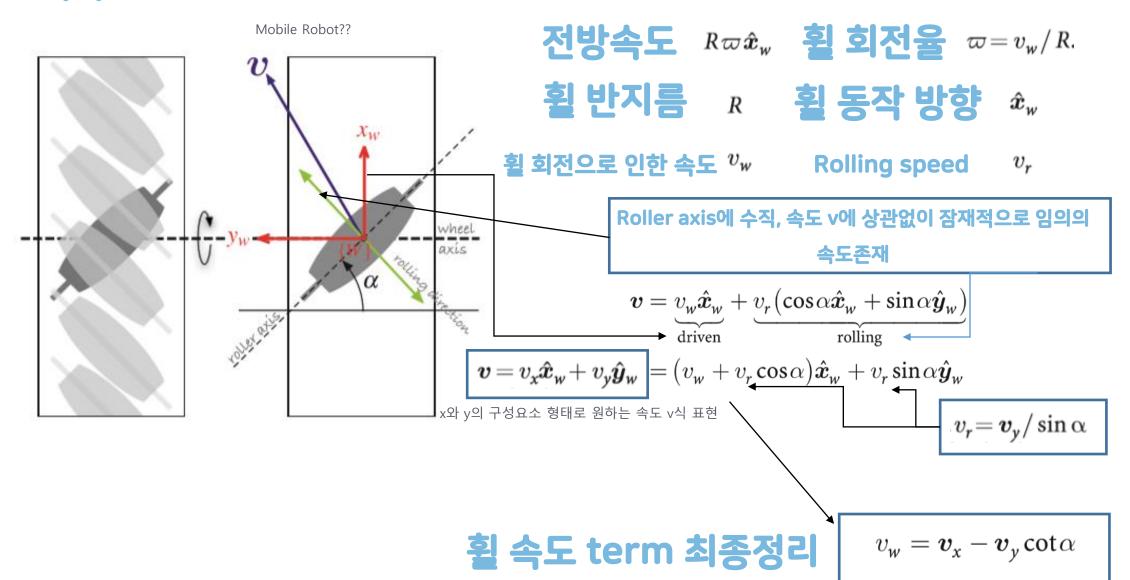
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Mobile Robot??





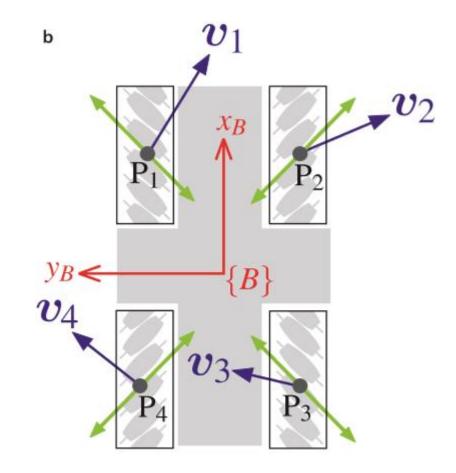
More Radical Wheel



Mobile Robot??

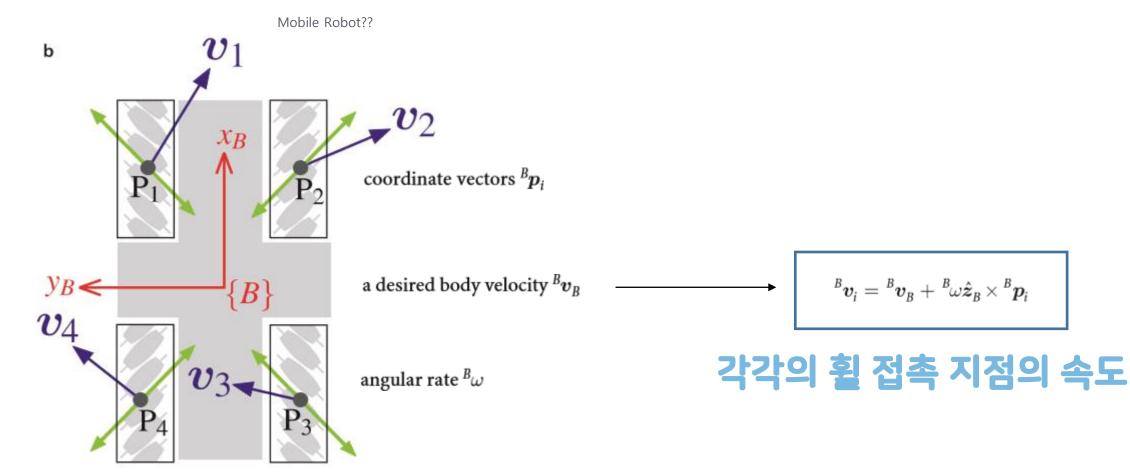


4개의 메카넘 휠이 있는 kuka youbot



kuka youbot 모델링 도식

 $q = (x, y, \theta) \in \mathcal{C}$ where $\mathcal{C} \subset \mathbb{R}^2 \times \mathbb{S}^1$



kuka youbot 모델링 도식

 $q = (x, y, \theta) \in \mathcal{C}$ where $\mathcal{C} \subset \mathbb{R}^2 \times \mathbb{S}^1$

Mobile Robot??



Flying Robots

- 1.micro air vehicles or MAVs
- 2. Fixed wing UAVs
- 3. Rotorcraft UAVs

Mobile Robot??

Flying robots differ from ground robots in some important ways

→ 1. configuration

configuration $q \in \mathbb{C}$ where $\mathbb{C} \subset \mathbb{R}^3 \times \mathbb{S}^1 \times \mathbb{S}^1 \times \mathbb{S}^1$.

2. Dynamic Model

수중 로봇과 Flying Robots의 유사점과 차이점

→ underwater equivalents (fixed wing aircraft, rotorcraft)

→ buoyancy force, drag forces added mass

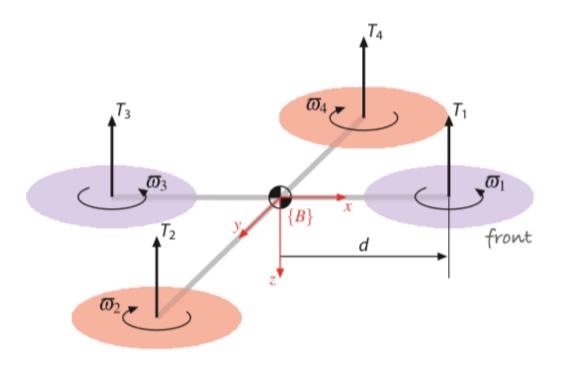
Mobile Robot??



Quadrotor modeling!

- 1. Easy to fly
- 2. does not have the complex mechanism
- 3. easier to model and control than others

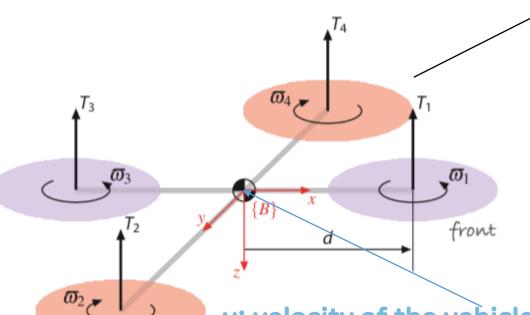
Mobile Robot??



- 1.Easy to fly
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Quadrotor Modeling 도식

Mobile Robot??



$$T_i = b \varpi_i^2, i = 1, 2, 3, 4$$

Lift constant b>0
Newton's second law

$$m\dot{m{v}} = egin{pmatrix} 0 \ 0 \ mg \end{pmatrix} - {}^0m{R}_B egin{pmatrix} 0 \ 0 \ T \end{pmatrix} - Bm{v}$$

v: velocity of the vehicle's center of mass

g:중력 가속도 m:vehicle 질량

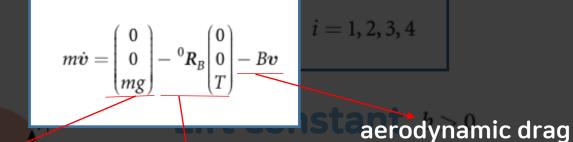
B:aerodynamic friction

 $T = \Sigma T_i$ is the total upward thrust

Quadrotor Modeling 도식

4.2 Flying Robots terms 분석





the force of gravity which acts downward in the world frame

lewton's second law

the total thrust in the vehicle frame rotated into the world coordinate rotate my

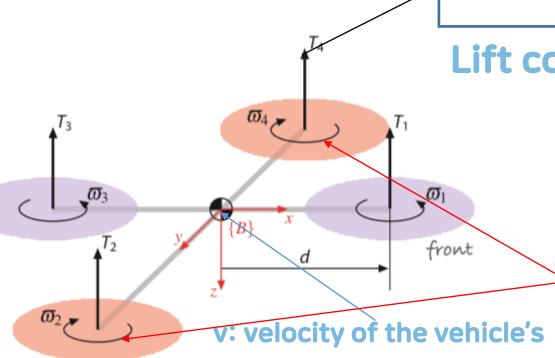
v: velocity of the vehicle's center of mass

 $T = \Sigma T_i$ is the total upward thrust

Quadrotor Modeling 도식

Mobile Robot??

Newton's second law



$$T_i = b\varpi_i^2$$
, $i = 1, 2, 3, 4$

Lift constant b > 0

$$m\dot{oldsymbol{v}} = egin{pmatrix} 0 \ 0 \ mg \end{pmatrix} - \ ^0oldsymbol{R}_Begin{pmatrix} 0 \ 0 \ T \end{pmatrix} - Boldsymbol{v}$$

g:중력 가속도 m:vehicle 질량

B:aerodynamic friction

 $T = \sum T_i$ is the total upward thrust

Rotor thrust의 차이가 vehicle을 회전하게 만든다.

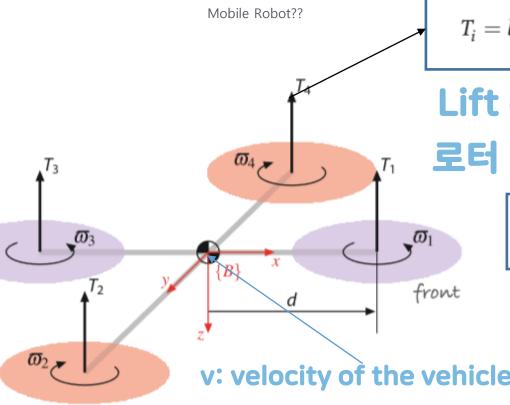
center of mass

Quadrotor Modeling 도식

$$\tau_x = dT_4 - dT_2$$

$$T_i = b \varpi_i^2, i = 1, 2, 3, 4$$

$$=> \qquad \tau_x = db \left(\varpi_4^2 - \varpi_2^2\right)$$



$$T_i = b\varpi_i^2$$
, $i = 1, 2, 3, 4$

Lift constant b > 0

로터 속도의 관점에서 토크식(x축,y축)

$$au_x = db \Big(\varpi_4^2 - \varpi_2^2 \Big)$$
 => $au_y = db \Big(\varpi_1^2 - \varpi_3^2 \Big)$

v: velocity of the vehicle's

center of mass

Quadrotor Modeling 도식

configuration $q \in \mathbb{C}$ where $\mathbb{C} \subset \mathbb{R}^3 \times \mathbb{S}^1 \times \mathbb{S}^1 \times \mathbb{S}^1$.

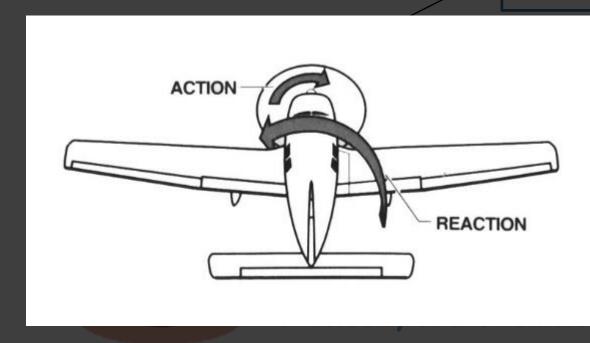
Reaction Torque???

$$Q_i = k \varpi_i^2$$

4.2 Flying Reaction Torque?

Mobile Robot?

 $T_i = b\varpi_i^2, i = 1, 2, 3, 4$



constant b > 0

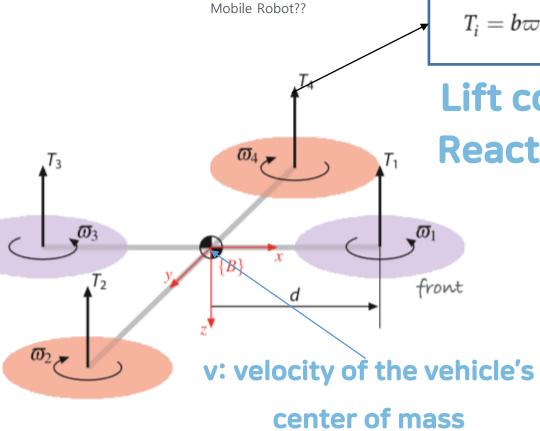
뉴턴의 운동 법칙 때문에, 엔진이 프로펠러를 회전시키기 위해 가하는 힘(토크)은 엔진에 다시 가해지는 반응적인 reactive force를 유발하고 이때 이 force는 전체 비행기에 가해지게 된다는 개념

Reaction Torque???

 $Q_i = k \varpi_i^2$

center of mass

Quadrotor Modeling 도식



configuration $q \in \mathbb{C}$ where $\mathbb{C} \subset \mathbb{R}^3 \times \mathbb{S}^1 \times \mathbb{S}^1 \times \mathbb{S}^1$.

Quadrotor Modeling 도식

$$T_i = b \varpi_i^2, i = 1, 2, 3, 4$$

Lift constant b>0 Reaction Torque

$$Q_i = k \varpi_i^2$$

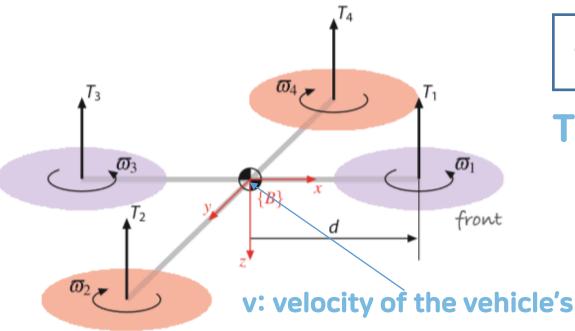
Total Reaction Torque

$$au_z = Q_1 - Q_2 + Q_3 - Q_4$$

= $k \Big(\varpi_1^2 + \varpi_3^2 - \varpi_2^2 - \varpi_4^2 \Big)$

Mobile Robot??

로터 속도의 관점에서 토크식(x축,y축)



$$\tau_x = db \left(\varpi_4^2 - \varpi_2^2\right) \quad \Longrightarrow \quad \tau_y = db \left(\varpi_1^2 - \varpi_3^2\right)$$

Total Reaction Torque(z축)

$$au_z = Q_1 - Q_2 + Q_3 - Q_4 \ = k \Big(arpi_1^2 + arpi_3^2 - arpi_2^2 - arpi_4^2 \Big)$$

center of mass

Quadrotor Modeling 도식

configuration $q \in \mathbb{C}$ where $\mathbb{C} \subset \mathbb{R}^3 \times \mathbb{S}^1 \times \mathbb{S}^1 \times \mathbb{S}^1$.

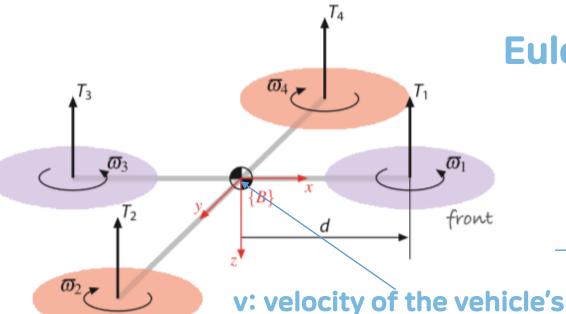
Total Torque

$$\boldsymbol{\tau} = (\tau_{x}, \tau_{y}, \tau_{z})^{T}$$

Mobile Robot??

Total Torque

$$\boldsymbol{\tau} = (\tau_x, \tau_y, \tau_z)^T$$



Euler's equations of motion

$${}^{B}\boldsymbol{J}^{B}\dot{\boldsymbol{\omega}}+{}^{B}\boldsymbol{\omega}\! imes\!\left({}^{B}\!\boldsymbol{J}^{B}\boldsymbol{\omega}
ight)\!={}^{B}\!\boldsymbol{ au}$$

→ Total Torque

$$J\dot{oldsymbol{\omega}} = -oldsymbol{\omega} imes Joldsymbol{\omega} + oldsymbol{ au}$$

center of mass

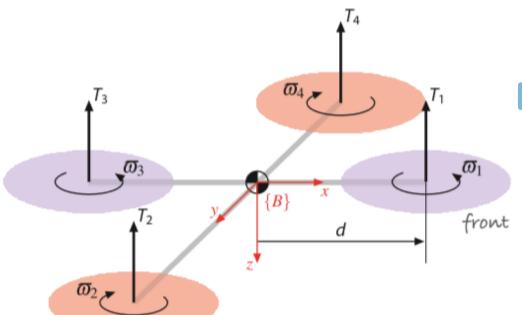
Quadrotor Modeling 도식

configuration $q \in \mathbb{C}$ where $\mathbb{C} \subset \mathbb{R}^3 \times \mathbb{S}^1 \times \mathbb{S}^1 \times \mathbb{S}^1$.

Mobile Robot??

Total Torque

$$J\dot{\omega} = -\omega imes J\omega + au$$



Dynamics by Newton's second law

$$m\dot{oldsymbol{v}} = egin{pmatrix} 0 \ 0 \ mg \end{pmatrix} - \ ^0oldsymbol{R}_Begin{pmatrix} 0 \ 0 \ T \end{pmatrix} - Boldsymbol{v}$$

Quadrotor Modeling 도식

configuration $q \in \mathbb{C}$ where $\mathbb{C} \subset \mathbb{R}^3 \times \mathbb{S}^1 \times \mathbb{S}^1 \times \mathbb{S}^1$.

Quadrotor

Motion

$$\begin{pmatrix} T \\ \boldsymbol{\tau} \end{pmatrix} = \begin{pmatrix} -b & -b & -b & -b \\ 0 & -db & 0 & db \\ db & 0 & -db & 0 \\ k & -k & k & -k \end{pmatrix} \begin{pmatrix} \varpi_1^2 \\ \varpi_2^2 \\ \varpi_3^2 \\ \varpi_4^2 \end{pmatrix} = A \begin{pmatrix} \varpi_1^2 \\ \varpi_2^2 \\ \varpi_3^2 \\ \varpi_4^2 \end{pmatrix}$$

Mobile Robot??

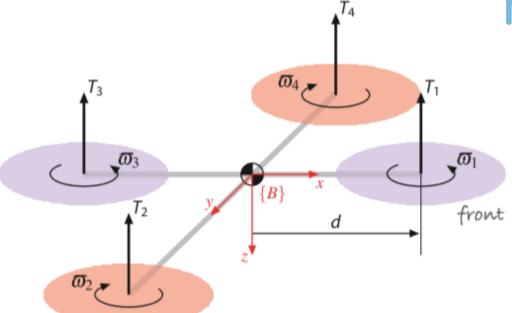
Quadrotor

Motion

$$\begin{pmatrix} T \\ \boldsymbol{\tau} \end{pmatrix} = \begin{pmatrix} -b & -b & -b & -b \\ 0 & -db & 0 & db \\ db & 0 & -db & 0 \\ k & -k & k & -k \end{pmatrix} \begin{pmatrix} \varpi_1^2 \\ \varpi_2^2 \\ \varpi_3^2 \\ \varpi_4^2 \end{pmatrix} = \boldsymbol{A} \begin{pmatrix} \varpi_1^2 \\ \varpi_2^2 \\ \varpi_3^2 \\ \varpi_4^2 \end{pmatrix}$$

역행렬!

full rank if b, k, d > 0



Quadrotor Speed

$$egin{pmatrix} arpi_1^2 \ arpi_2^2 \ arpi_3^2 \ arpi_4^2 \end{pmatrix} = m{A}^{-1} egin{pmatrix} T \ au_x \ au_y \ au_z \end{pmatrix}$$

Quadrotor Modeling 도식 configuration $q \in \mathbb{C}$ where $\mathbb{C} \subset \mathbb{R}^3 \times \mathbb{S}^1 \times \mathbb{S}^1 \times \mathbb{S}^1$.

Control of motor velocity is discussed in Sect. 9.1.6.

Mobile Robot??

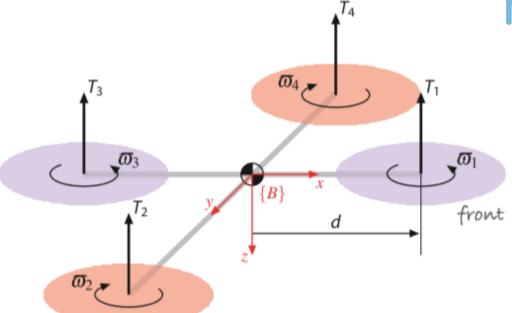
Quadrotor

Motion

$$\begin{pmatrix} T \\ \boldsymbol{\tau} \end{pmatrix} = \begin{pmatrix} -b & -b & -b & -b \\ 0 & -db & 0 & db \\ db & 0 & -db & 0 \\ k & -k & k & -k \end{pmatrix} \begin{pmatrix} \varpi_1^2 \\ \varpi_2^2 \\ \varpi_3^2 \\ \varpi_4^2 \end{pmatrix} = \boldsymbol{A} \begin{pmatrix} \varpi_1^2 \\ \varpi_2^2 \\ \varpi_3^2 \\ \varpi_4^2 \end{pmatrix}$$

역행렬!

full rank if b, k, d > 0



Quadrotor Speed

$$egin{pmatrix} arpi_1^2 \ arpi_2^2 \ arpi_3^2 \ arpi_4^2 \end{pmatrix} = m{A}^{-1} egin{pmatrix} T \ au_x \ au_y \ au_z \end{pmatrix}$$

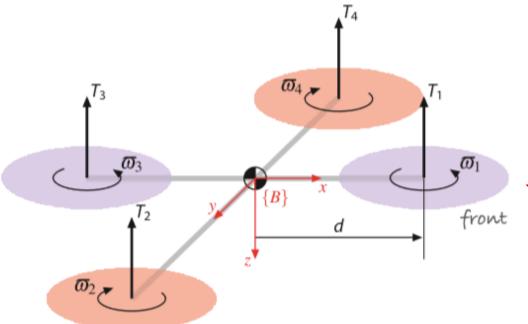
Quadrotor Modeling 도식 configuration $q \in \mathbb{C}$ where $\mathbb{C} \subset \mathbb{R}^3 \times \mathbb{S}^1 \times \mathbb{S}^1 \times \mathbb{S}^1$.

Control of motor velocity is discussed in Sect. 9.1.6.

Mobile Robot??

Quadrotor Speed

$$\begin{pmatrix} \varpi_1^2 \\ \varpi_2^2 \\ \varpi_3^2 \\ \varpi_4^2 \end{pmatrix} = \mathbf{A}^{-1} \begin{pmatrix} T \\ \tau_x \\ \tau_y \\ \tau_z \end{pmatrix}$$



a nested control structure

for pitch and

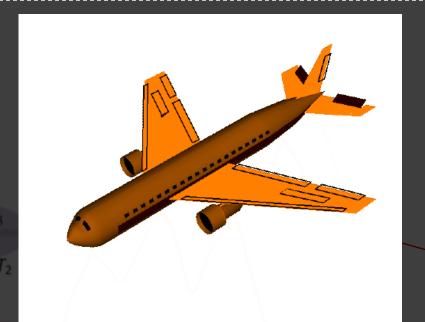
x-translational motion

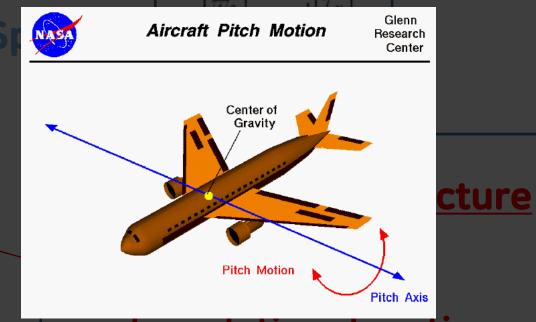
Quadrotor Modeling 도식

configuration $q \in \mathbb{C}$ where $\mathbb{C} \subset \mathbb{R}^3 \times \mathbb{S}^1 \times \mathbb{S}^1 \times \mathbb{S}^1$.

4.2 Flying RobePitch motion?

Mobile Robot??





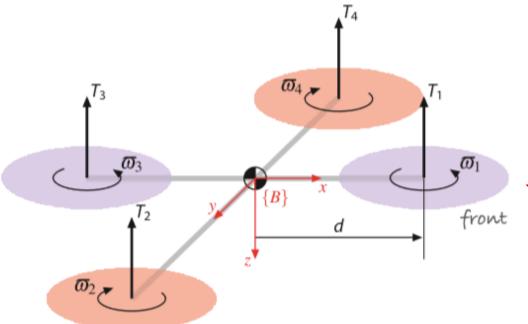
x-translational motion

항공기는 비행중 중량의 평균 위치인 무게중심을 중심으로 회전한다 이때 이 좌표계를 3차원으로 정의 한다면 각각의 주요 축을 따라 항공기 부품들의 회전량으로 항공기의 방향을 정의할 수 있다. (엘리베이터나 엔진, 의자 등을 포함한 모든 요소가 항공기 전체의 회전량에 영향을 미친다는 것) 피치 축은 항공기 중심선에 수직이며 날개 평면에 놓여 있다. 이때 Pitch motion은 그림과 같이 항공기의 코부분의 위아래 이동을 의미한다.

Mobile Robot??

Quadrotor Speed

$$\begin{pmatrix} \varpi_1^2 \\ \varpi_2^2 \\ \varpi_3^2 \\ \varpi_4^2 \end{pmatrix} = \mathbf{A}^{-1} \begin{pmatrix} T \\ \tau_x \\ \tau_y \\ \tau_z \end{pmatrix}$$



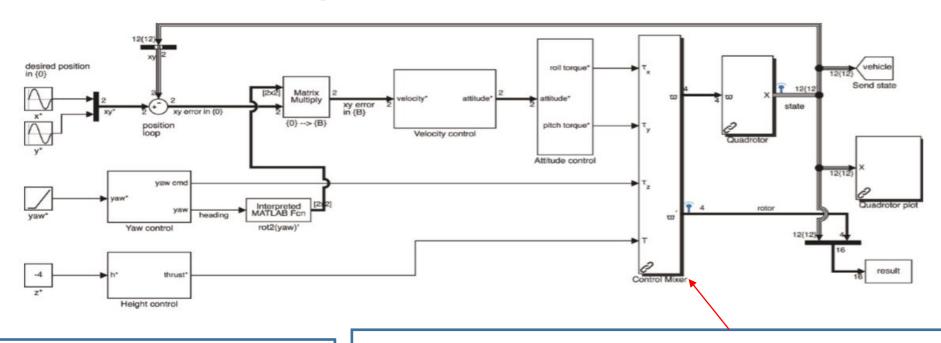
a nested control structure

for pitch and

x-translational motion

Quadrotor Modeling 도식

configuration $q \in \mathbb{C}$ where $\mathbb{C} \subset \mathbb{R}^3 \times \mathbb{S}^1 \times \mathbb{S}^1 \times \mathbb{S}^1$.



Transfer Function

 $\Theta_y(s) / \tau_y(s) = 1 / (Js^2 + Bs)$

The innermost loop uses

a PD-Controller to compute the required

pitching torque on the airframe

Mobile Robot??

PID 제어기

$$G_c(s) = K_p + \frac{K_I}{s} + K_D s$$

 $K_I = 0$

PD 제어기

$$G_c(s) = K_p + K_D s$$

 $\theta_p^{\#}$ would be estimated by an inertial navigation system $\dot{\theta}_p^{\#}$ would be derived from gyroscopic sensors.

Pitching torque
$$\tau_y^* = K_{\tau,p} \Big(\theta_p^* - \theta_p^\# \Big) + K_{\tau,d} \Big(\dot{\theta}_p^* - \dot{\theta}_p^\# \Big)$$

Quadrotor **Speed**

$$\begin{pmatrix} \varpi_1^2 \\ \varpi_2^2 \\ \varpi_3^2 \\ \varpi_4^2 \end{pmatrix} = \mathbf{A}^{-1} \begin{pmatrix} T \\ \tau_x \\ \tau_y \\ \tau_z \end{pmatrix}$$

The term $\dot{\theta}_{p}^{*}$ is commonly ignored.

Mobile Robot??

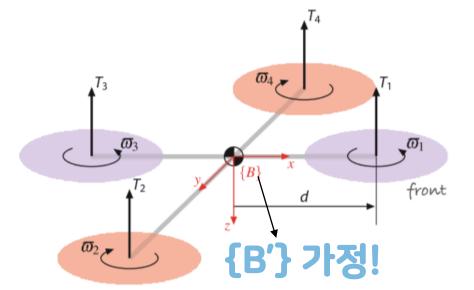
Pitching torque

Quadrotor Speed

$$egin{pmatrix} arpi_1^2 \ arpi_2^2 \ arpi_3^2 \ arpi_4^2 \end{pmatrix} = oldsymbol{A}^{-1} egin{pmatrix} T \ au_x \ au_y \ au_z \end{pmatrix}$$

$$au_y^* = K_{ au,p} \Big(heta_p^* - heta_p^\# \Big) + K_{ au,d} \Big(\dot{ heta}_p^* - \dot{ heta}_p^\# \Big)$$
 The term $\dot{ heta}_p^*$ is commonly ignored.

 $\theta_p^\#$ would be estimated by an inertial navigation system $\dot{\theta}_p^\#$ would be derived from gyroscopic sensors.



Pitching을 구해보자!

$$^{B'}\!m{f} = \mathscr{R}_yig(heta_pig)ulletig(egin{array}{c} 0 \ 0 \ T \end{matrix}ig) = egin{pmatrix} T\sin heta_p \ 0 \ T\cos heta_p \end{pmatrix}$$

$${}^{B'}\!f_{x} = T\sin\theta_{p} \approx T\theta_{p}$$

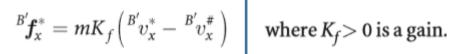
we have assumed that θ_p is small.

4.2 Flying Robots Pitching을 구해보자! {B'}-x방향의 pitching 속도 조절

$${}^{B'}\!m{f} = \mathscr{R}_{y}\!\left(heta_{p}
ight)ullet\!\left(egin{matrix} 0 \ 0 \ T \end{matrix}
ight) = egin{matrix} T\sin heta_{p} \ 0 \ T\cos heta_{p} \end{matrix}
ight)$$

$$^{B'}\mathbf{f}_{x}=T\sin\theta_{p}pprox T\theta_{p}$$

we have assumed that θ_p is small.

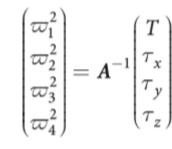


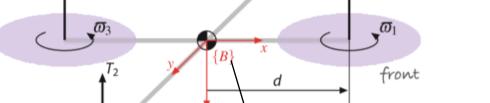
Quadrotor

Speed

desired pitch angle

$$\theta_p^* pprox rac{m}{T} K_f \Big({}^{B'}\!v_x^* - {}^{B'}\!v_x^\# \, \Big)$$



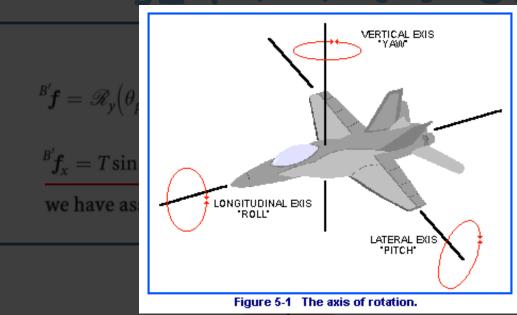


Pitching torque

$$au_y^* = K_{ au,p} ig(heta_p^* - heta_p^\# ig) + K_{ au,d} ig(\dot{ heta}_p^* - \dot{ heta}_p^\# ig)$$

4.2 Flying Robots Yaw?

Pitching을 구해보자! {B'}-x방향의 pitching 속도 조절



$$v_x^* - {}^{B'}v_x^*$$
 where $K_f > 0$ is a gain.

which is a function of the yaw angle θ_y

$$\begin{pmatrix} B'v_x \\ B'v_y \end{pmatrix} = \begin{pmatrix} \cos\theta_y & -\sin\theta_y \\ \sin\theta_y & \cos\theta_y \end{pmatrix}^T \begin{pmatrix} v_x \\ v_y \end{pmatrix}$$

$$\begin{bmatrix} \overline{w}_1^* - \overline{w}_2^* \\ \overline{w}_2^2 \\ \overline{w}_3^2 \end{bmatrix} = A^{-1} \begin{bmatrix} T \\ \tau_x \\ \tau_y \\ \overline{\tau}_z \end{bmatrix}$$

Yaw는 이동방향에 대해 수직면에 있는 축주위로의 회전을 의미합니다.
Pitch motion과 마찬가지로 제어모델링을 할 때 꼭 고려를 해줘야 하는 요소입니다.
오른쪽 그림은 Yaw angle에 대한 식입니다.

$$\tau_y^* = K_{\tau,p} \left(\theta_p^* - \theta_p^* \right) + K_{\tau,d} \left(\dot{\theta}_p^* - \dot{\theta}_p^* \right)$$

4.3 Advanced Topics

4.3.1 Nonholonomic and Under-Actuated Systems

홀로노믹(Holonomic)

Controllabe DOF = Total DOF

는 홀로노믹(NonHolonomic)

Controllabe DOF < Total DOF

리던던트(Redundant)

Controllabe DOF > Total DOF

Fully-actuated: 모든 관절에

대해서 제어를 할 수 있는 상태

DOF = Total actuator

Under-actuated: 적은 구동기로

모든 관절을 제어 할 수 있는 상태

DOF > Total actuator

Mobile robot seminar
Ch4. Mobile robot

Thanks for watching