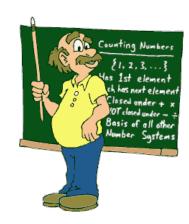


# **MSYS**

Microcontroller Systems

Lektion 9
Aritmetiske og logiske instruktioner



Version: 26-9-2017, Henning Hargaard

### Binær addition

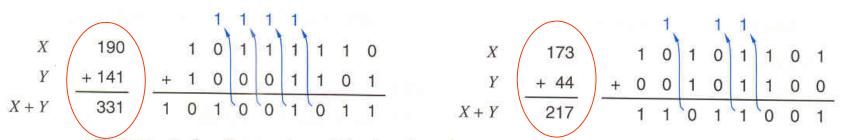
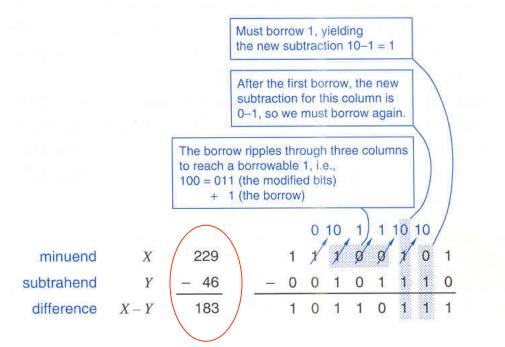


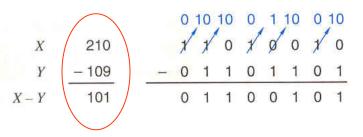
Figure 2-1 Examples of decimal and corresponding binary additions.

### Binær subtraktion



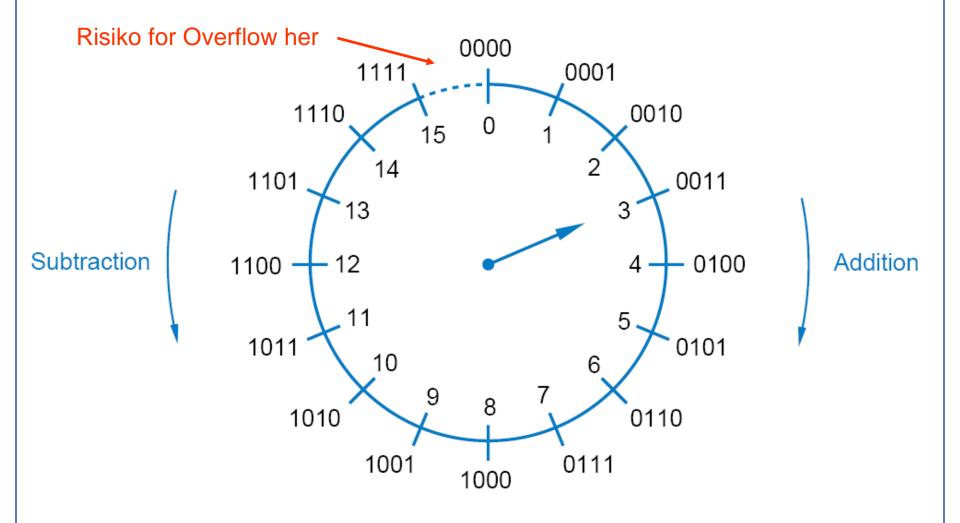
#### Figure 2-2

Examples of decimal and corresponding binary subtractions.





## Unsigned addition / subtraktion





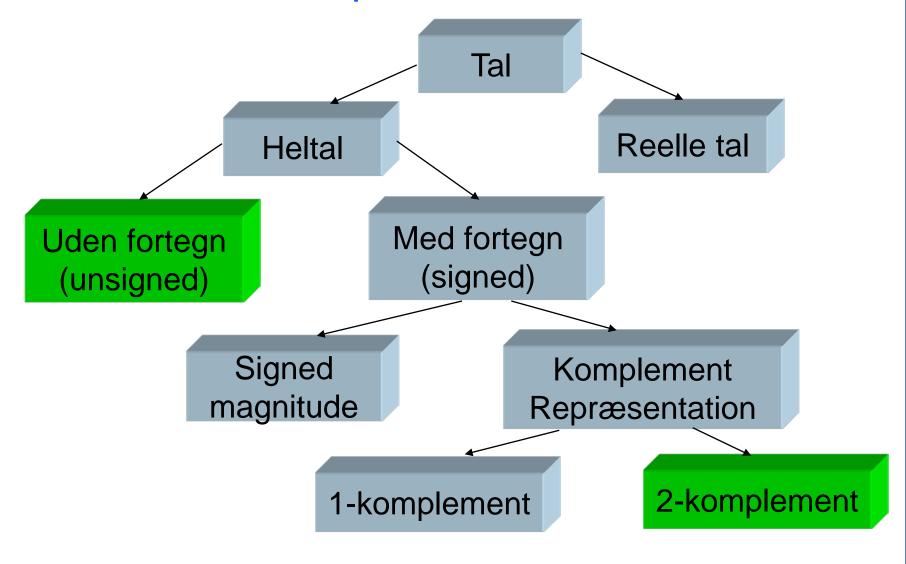
## Nemt med 16 fingre:

C	1 1 0 0	1	1	0	0
X	1 9 B 9 <sub>16</sub> + C 7 E 6 <sub>16</sub> +	1	9	11	9
Y	+ C 7 E 6 <sub>16</sub> +	12	7	14	6
X + Y	E 1 9 F <sub>16</sub>	14	17	25	15
		14	16+1	16+9	15
		E	1	9	F





## Tal-repræsentationer





## Signed magnitude

Vi anvender typisk MSB til at repræsentere fortegnet.

$$01010101_2 = +85_{10}$$

$$011111111_2 = +127_{10}$$

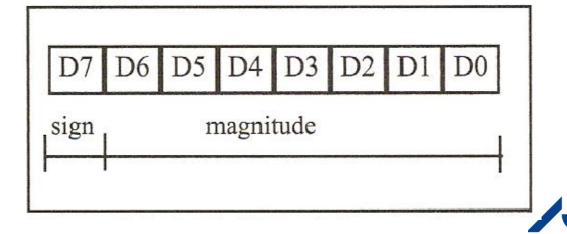
$$00000000_2 = +0_{10}$$

$$11010101_2 = -85_{10}$$

$$111111111_2 = -127_{10}$$

$$100000000_2 = -0_{10}$$

Bemærk, at vi har 2 værdier, der begge repræsenterer 0!



## Dannelse af 1-komplement

$$17_{10} = 00010001_{2}$$
  $-99_{10} = 10011100_{2}$   $\downarrow$ 
 $11101110_{2} = -17_{10}$   $01100011_{2} = 99_{10}$ 
 $119_{10} = 01110111_{2}$   $-127_{10} = 10000000_{2}$   $\downarrow$ 
 $10001000_{2} = -119_{10}$   $01111111_{2} = 127_{10}$ 
 $0_{10} = 00000000_{2}$  (positive zero)
 $\downarrow$ 
 $11111111_{2} = 0_{10}$  (negative zero)

Bemærk: 2 værdier for 0!



## Dannelse af 2-komplement

$$17_{10} = 00010001_{2} \qquad -99_{10} = 10011101_{2}$$

$$\downarrow \qquad \text{complement bits}$$

$$11101110 \qquad \qquad 1100010$$

$$\frac{+1}{11101111_{2}} = -17_{10} \qquad \frac{+1}{01100011_{2}} = 99_{10}$$

$$119_{10} = 01110111_{2} \qquad -127_{10} = 10000001_{2}$$

$$\downarrow \qquad \text{complement bits}$$

$$10001000 \qquad \qquad 01111110$$

$$\frac{+1}{10001001_{2}} = -119_{10} \qquad \frac{+1}{01111111_{2}} = 127_{10}$$

$$0_{10} = 00000000_{2} \qquad -128_{10} = 10000000_{2}$$

$$\downarrow \qquad \text{complement bits}$$

$$111111111 \qquad \qquad -11$$

$$\frac{+1}{100000000_{2}} = 0_{10} \qquad 0000000_{2} = -128_{10}$$

Regel: Inverter alle bit og læg en til.



## Nummer systemer

Table 2-6 Decimal and 4-bit numbers.

Decimal	Two's Complement	Ones' Complement	Signed Magnitude
-8	1000	_	_
-7	1001	1000	1111
-6	1010	1001	1110
-5	1011	1010	1101
-4	1100	1011	1100
-3	1101	1100	1011
-2	1110	1101	1010
-1	1111	1110	1001
0	0000	1111 or 0000	1000 or 0000
1	0001	0001	0001
2	0010	0010	0010
3	0011	0011	0011
4	0100	0100	0100
5	0101	0101	0101
6	0110	0110	0110
7	0111	0111	0111



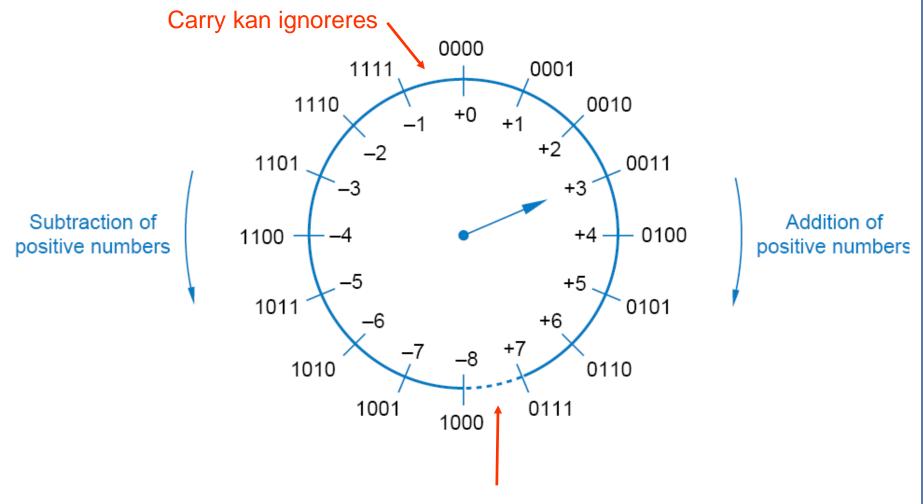
## 2-komplement addition

 Bemærk : Samme hardware / instruktioner som ved unsigned behandling.

Det er blot vores måde at kode tal på, der er anderledes!



## "2-komplement – uret"



Risiko for Overflow her

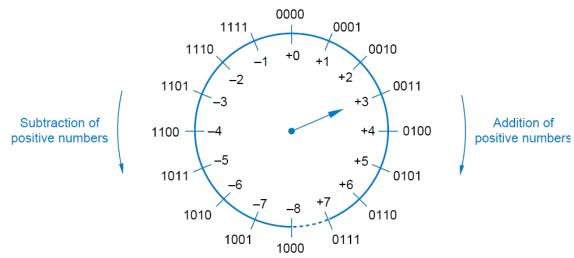


## 2-komplement Overflow

$$\begin{array}{rrr} -3 & 1101 \\ + & -6 & + 1010 \\ \hline -9 & 10111 = +7 \end{array}$$

$$\begin{array}{rrr}
-8 & 1000 \\
+ & -8 & + 1000 \\
\hline
-16 & 10000 = +0
\end{array}$$

$$\begin{array}{rrr} +7 & 0111 \\ + & +7 & +0111 \\ \hline +14 & & 1110 = -2 \end{array}$$





Hvordan gemmes tallet -5 (= minus 5) i "signed magnitude" formatet ?

A: 0b00000101

B: 0b10000101

C: 0b11111010

D: 0b11111011



Hvordan gemmes tallet -5 (= minus 5) i "1's complement" formatet ?

A: 0b00000101

B: 0b10000101

C: 0b11111010

D: 0b11111011



Hvordan gemmes tallet -5 (= minus 5) i "2's complement" formatet ?

A: 0b00000101

B: 0b10000101

C: 0b11111010

D: 0b11111011



### Additions Instruktioner

ADD Rd,Rr ;Rd = Rd + Rr

ADC Rd,Rr ;Rd = Rd + Rr + C

ADIW Rd:Rd,K ;Rd+1:Rd = Rd+1:Rd + K



## ADD (Add without Carry)

#### **Description:**

Adds two registers without the C Flag and places the result in the destination register Rd.

#### Operation:

(i)  $Rd \leftarrow Rd + Rr$ 

Syntax:

Operands:

**Program Counter:** 

(i) ADD Rd,Rr

 $0 \le d \le 31, \ 0 \le r \le 31$ 

 $PC \leftarrow PC + 1$ 

#### 16-bit Opcode:

0000	11rd	dddd	rrrr

#### Example:



## ADC (Add with Carry)

#### **Description:**

Adds two registers and the contents of the C Flag and places the result in the destination register Rd.

#### Operation:

(i)  $Rd \leftarrow Rd + Rr + C$ 

Syntax:

#### Operands:

**Program Counter:** 

(i) ADC Rd,Rr

$$0 \le d \le 31, \ 0 \le r \le 31$$

#### PC ← PC + 1

#### Example:

; Add R1:R0 to R3:R2

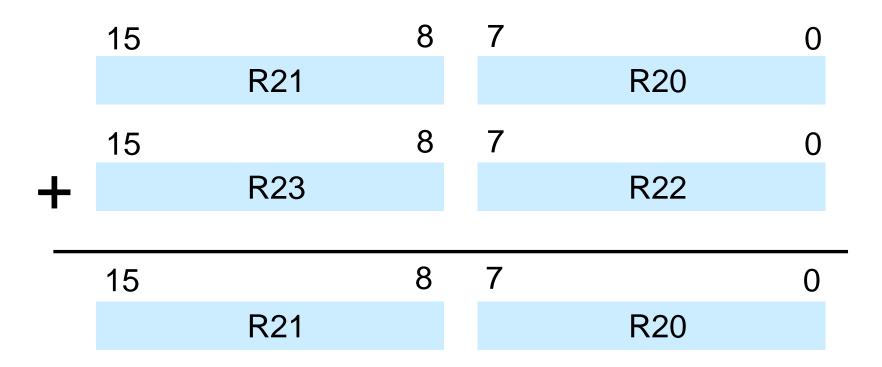
add r2,r0 ; Add low byte

adc r3,r1 ; Add with carry high byte



### Addition af 16 bit tal

OPGAVE: Skriv kode, der lægger to 16 bit tal sammen.



Hint: Gør brug af instruktionerne ADD og ADC.



### Subtraktions Instruktioner

SUB Rd,Rr ; Rd = Rd - Rr

SBC Rd,Rr ;Rd = Rd - Rr - C

SUBI Rd,K ; Rd = Rd - K

SBCI Rd,K ;Rd = Rd - K - C

SBIW Rd:Rd,K ;Rd+1:Rd = Rd+1:Rd - K

Vores microcontroller anvender denne metode for subtraktion ( den "lægger sammen for at trække fra" ).

- 1. Danner 2-komplementet af tallet, der skal subtraheres.
- 2. Adderer de to tal.
- 3. Inverterer Carry-flaget.



## Multiplikation

Table 5-1: Multiplication Summary

Multiplication	Application	Byte1	Byte2	High byte of result	Low byte of result
MUL Rd, Rr	Unsigned numbers	Rd	Rr	R1	R0
MULS Rd, Rr	Signed numbers	Rd	Rr	R1	R0
MULSU Rd, Rr	Unsigned numbers with signed numbers	Rd	Rr	R1	R0

The following example multiplies 25H by 65H.

```
LDI R23,0x25 ;load 25H to R23

LDI R24,0x65 ;load 65H to R24

MUL R23,R24 ;25H * 65H = E99 where

;R1 = 0EH and R0 = 99H
```

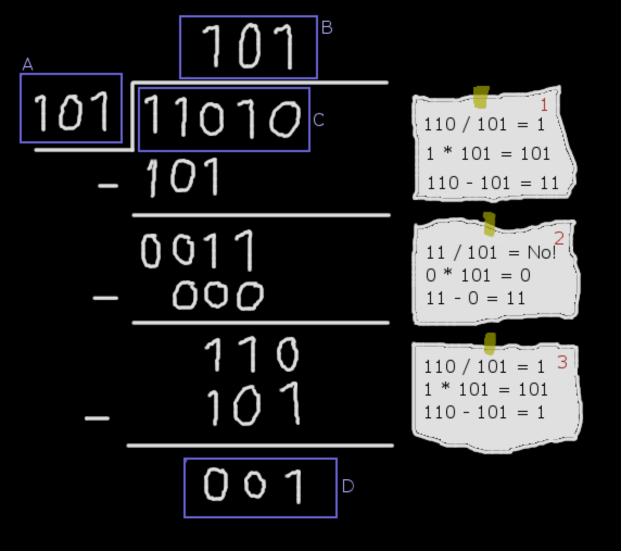


## Eksempel på divisions-algoritme (s.167)

```
.DEF
     NUM = R20
.DEF DENOMINATOR = R21
.DEF QUOTIENT = R22
     LDI
           NUM, 95
                             ; NUM = 95
     LDI DENOMINATOR, 10 ; DENOMINATOR = 10
     CLR QUOTIENT
                             ;QUOTIENT = 0
L1:
     INC QUOTIENT
     SUB
           NUM, DENOMINATOR
     BRCC
           L.1
                             ;branch if C is zero
     DEC
           OUOTIENT
                        ; once too many
     ADD
           NUM, DENOMINATOR ; add back to it
HERE: JMP HERE
                             ; stay here forever
```



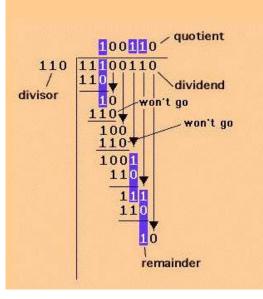
### Binær division med shift / subtract





### Binær division med shift / subtract

- Set quotient to 0
- Align leftmost digits in dividend and divisor
- · Repeat
  - o If that portion of the dividend above the divisor is greater than or equal to the divisor
    - Then subtract divisor from that portion of the dividend and
    - Concatentate 1 to the right hand end of the quotient
    - Else concatentate 0 to the right hand end of the quotient
  - o Shift the divisor one place right
- · Until dividend is less than the divisor
- quotient is correct, dividend is remainder
- STOP





### AND Rd,Rr (Rd = Rd AND Rr)

### **Logical AND Function**

Inputs		Output
X	Y	X AND Y
0	0	0
0	1	0
1	0	0
1	1	1

Velegnet til at NULSTILLE bestemte bit.

Også muligt at AND'e med en konstant:

ANDI Rd,K; rd = Rd AND K



## AND eksempel

```
Example 5-18
Show the results of the following.
     LDI R20,0x35 ; R20 = 35H
     ANDI R20,0x0F ; R20 = R20 AND 0FH (now R20 = 05)
Solution:
           35H 0011 0101
          OFH 0000 1111
      AND
                                  ;35H AND OFH = 05H, Z = 0, N = 0
            05H 0000 0101
```



### OR Rd, Rr (Rd = Rd OR Rr)

### **Logical OR Function**

Inp	uts	Output		
X	Y	X OR Y		
0	0	0		
0	1	1		
1	0	1		
1	1	1		

Velegnet til at SÆTTE bestemte bit.

Også muligt at OR'e med en konstant: ORI Rd,K ;rd = Rd OR K



## **OR** eksempel

#### Example 5-19

(a) Show the results of the following:

LDI R20,0 $\times$ 04 ; R20 = 04 ORI R20,0 $\times$ 30 ; now R20 = 34H

(b) Assume that PB2 is used to control an outdoor light, and PB5 to control a light inside a building. Show how to turn "on" the outdoor light and turn "off" the inside one.

#### Solution:

```
04H 0000 0100
(a)
           30H 0011 0000
     OR
           34H 0011 0100 04 OR 30 = 34H, Z = 0 and N = 0
(b)
     SBI
          DDRB, 2 ;bit 2 of Port B is output
     SBI
          DDRB, 5
                           ; bit 5 of Port B is output
           R20, PORTB
                           ; move PORTB to R20. (Notice that we read
     IN
                           ; the value of PORTB instead of PINB
                           ; because we want to know the last value
                            ; of PORTB, not the value of the AVR
                           ; chip pins.)
           R20, 0b00000100
     ORI
                           ; set bit 2 of R20 to one
     ANDI R20, 0b11011111
                           ;clear bit 5 of R20 to zero
     OUT
           PORTB, R20
                            ; out R20 to PORTB
HERE: JMP HERE
                            ; stop here
```

EOR Rd, Rr (Rd = Rd XOR Rr)

Inp	uts	Output
A	В	A XOR B
0	0	0
0	1	1
1	0	1
1	1	0

Velegnet til at INVERTERE bestemte bit.



## EOR eksempel

Snow the re	sults of	the foll	owing:						
LDI		0x54							
LDI	R21,	0x78							
EOR	R20,	R21							
Solution:									
	54H	0101	0100						
			1000						
XOR	78H	0111	1000						
XOR	78H	0111	1000						



Hvordan kan man <u>nulstille bit 7</u> i R16 (uden at ændre på resten af bittene) ?

A: LDI R17, 0b10000000 AND R16, R17

B: LDI R17, 0b01111111 EOR R16, R17

C: LDI R17, 0b10000000 OR R16, R17

D: LDI R17, 0b01111111 AND R16, R17



Hvordan kan man <u>sætte bit 7</u> i R16 (uden at ændre på resten af bittene) ?

A: LDI R17, 0b10000000 AND R16, R17

B: LDI R17, 0b01111111 EOR R16, R17

C: LDI R17, 0b10000000 OR R16, R17

D: LDI R17, 0b01111111 AND R16, R17



Hvordan kan man <u>invertere / toggle bit 7</u> i R16 (uden at ændre på resten af bittene) ?

A: LDI R17, 0b10000000 AND R16, R17

B: LDI R17, 0b10000000 EOR R16, R17

C: LDI R17, 0b10000000 OR R16, R17

D: LDI R17, 0b01111111 AND R16, R17



## COM og NEG

### COM (complement)

This instruction complements the contents of a register. The complement action changes the 0s to 1s, and the 1s to 0s. This is also called *I's complement*.

## Logical Inverter

Input	Output
X	NOT X
0	1
1	0

### X — NOT X

### **NEG** (negate)

This instruction takes the 2's complement of a register. See Example 5-23.

#### Example 5-23

Find the 2's complement of the value 85H. Notice that 85H is -123.

#### Solution:



## **SWAP** Register

Eksempel: SWAP R16

before:	D7-D4	D3-D0	after: SWAP	D3-D0	D7-D4
before:	0111	0010	after: SWAP	0010	0111



### Compare

CP Rd,Rr ;Rd sammenlignes med Rr

CPI Rd,K ;Rd sammenlignes med konstanten K

Table 5-2: AVR Compare Instructions

The second secon		
BREQ	Branch if equal	Branch if $Z = 1$
BRNE	Branch if not equal	Branch if $Z = 0$
BRSH	Branch if same or higher	Branch if $C = 0$
BRLO	Branch if lower	Branch if $C = 1$
BKLI	Branch if less than (signed)	Branch if $S = 1$
BRGE	Branch if greater than or equal (signed)	Branch if $S = 0$
BRVS	Branch if Overflow flag set	Branch if $V = 1$
BRVC		



## Conditional branch og flagene

Test	Boolean	Mnemonic	Complementary	Boolean	Mnemonic	Comment
Rd > Rr	Z•(N ⊕ V) = 0	BRLT <sup>(1)</sup>	Rd≤Rr	Z+(N ⊕ V) = 1	BRGE*	Signed
Rd ≥ Rr	(N ⊕ V) = 0	BRGE	Rd < Rr	(N ⊕ V) = 1	BRLT	Signed
Rd = Rr	Z = 1	BREQ	Rd ≠ Rr	Z = 0	BRNE	Signed
Rd ≤ Rr	Z+(N ⊕ V) = 1	BRGE <sup>(1)</sup>	Rd > Rr	Z•(N ⊕ V) = 0	BRLT*	Signed
Rd < Rr	(N ⊕ V) = 1	BRLT	Rd ≥ Rr	(N ⊕ V) = 0	BRGE	Signed
Rd > Rr	C + Z = 0	BRLO <sup>(1)</sup>	Rd≤Rr	C + Z = 1	BRSH*	Unsigned
Rd ≥ Rr	C = 0	BRSH/BRCC	Rd < Rr	C = 1	BRLO/BRCS	Unsigned
Rd = Rr	Z = 1	BREQ	Rd ≠ Rr	Z = 0	BRNE	Unsigned
Rd≤Rr	C + Z = 1	BRSH <sup>(1)</sup>	Rd > Rr	C + Z = 0	BRLO*	Unsigned
Rd < Rr	C = 1	BRLO/BRCS	Rd ≥ Rr	C = 0	BRSH/BRCC	Unsigned
Carry	C = 1	BRCS	No carry	C = 0	BRCC	Simple
Negative	N = 1	BRMI	Positive	N = 0	BRPL	Simple
Overflow	V = 1	BRVS	No overflow	V = 0	BRVC	Simple
Zero	Z = 1	BREQ	Not zero	Z = 0	BRNE	Simple

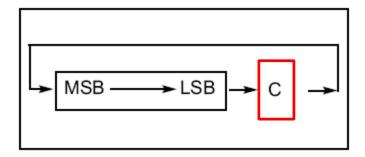
Note: 1. Interchange Rd and Rr in the operation before the test, i.e., CP Rd,Rr → CP Rr,Rd



#### ROR instruction

ROR Rd ;Rd (only flags are set)

In ROR, as bits are rotated from left to right, the carry flag enters the MSB and the LSB exits to the carry flag. In other words, in ROR the C is moved to the MSB, and the LSB is moved to the C.



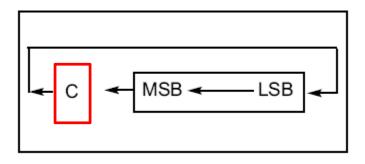
See what happens to 0010 0110 after running 3 ROR instructions:

CLC		;make $C = 0$ (carry is 0)
LDI	R20, 0x26	;R20 = 0010 0110
ROR	R20	;R20 = 0001 0011 C = 0
ROR	R20	;R20 = 0000 1001 C = 1
ROR	R20	$;R20 = 1000\ 0100\ C = 1$

#### ROL instruction

ROL Rd ;Rd (only flags are set)

ROL. In ROL, as bits are shifted from right to left, the carry flag enters the LSB and the MSB exits to the carry flag. In other words, in ROL the C is moved to the LSB, and the MSB is moved to the C.



SEC LDI R20,0x15

ROL R20

ROL R20

ROL R20

ROL R20

;make C = 1 (carry is 0)

 $;R20 = 0001 \ 0101$ 

 $R20 = 0010 \ 1011 \ C = 0$ 

 $R20 = 0101 \ 0110 \ C = 0$ 

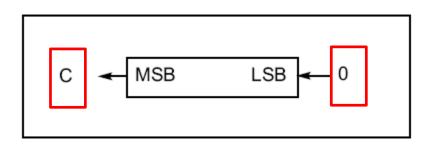
 $;R20 = 1010 \ 1100 \ C = 0$ 

 $R20 = 0101 \ 1000 \ C = 1$ 

#### LSL instruction

LSL Rd ;logical shift left

In LSL, as bits are shifted from right to left, 0 enters the LSB and the MSB exits to the carry flag. In other words, in LSL 0 is moved to the LSB, and the MSB is moved to the C.



this instruction multiplies content of the register by 2 assuming that after LSL the carry flag is not set.

In the next code you can see what happens to 00100110 after running 3 LSL instructions.

CLC ; make C = 0 (carry is 0)

LDI R20, 0x26; R20 = 0010 0110(38) c = 0

LSL R20 ;  $R20 = 0100 \ 1100(74) \ C = 0$ 

LSL R20 ;  $R20 = 1001 \ 1000(148) \ C = 0$ 

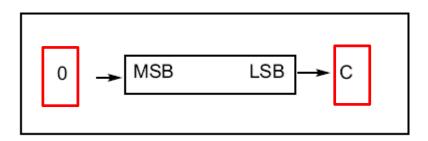
LSL R20 ;R20 = 0011 0000(98) C = 1 as C=1 and content of R20

; is not multiplied by 2

#### LSR Instruction

LSR Rd ;Rd (only flags are set)

In LSR, as bits are shifted from left to right, 0 enters the MSB and the LSB exits to the carry flag. In other words, in LSR 0 is moved to the MSB, and the LSB is moved to the C.



this instruction divides content of the register by 2 and carry flag contains the remainder of division.

In the next code you can see what happens to 0010 0110 after running 3 LSL instructions.

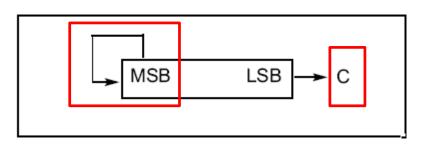
LDI R20,0x26 ;R20 = 0010 0110 (38) LSR R20 ;R20 = 0001 0011 (19) C = 0LSR R20 ;R20 = 0000 1001 (9) C = 1LSR R20 ;R20 = 0000 0100 (4) C = 1

#### ASR Instruction

ASR Rd ;Rd (only flags are set)

ASR means arithmetic shift right. ASR instruction can divide signed number by 2. In LSR, as bits are shifted from left to right, MSB is held constant and the LSB exits to the carry flag. In other words

MSB is not changed but is copied to D6, D6 is moved to D5, D5 is moved to D4 and so on.



In the next code you can see what happens to 0010 0110 after running 5 ASL instructions.

LDI	R20,0D60	$;R20 = 1101\ 0000(-48)\ c = 0$
ASR	R20	$;R20 = 1110\ 1000(-24)\ C = 0$
ASR	R20	$;R20 = 1111 \ 0100(-12) \ C = 0$
ASR	R20	$R20 = 1111 \ 1010(-6) \ C = 0$
ASR	R20	$R20 = 1111 \ 1101(-3) \ C = 0$
<b>ASR</b>	R20	$;R20 = 1111 \ 1110(-1) \ C = 1$

### Test ("socrative.com": Room = MSYS)

Hvordan kan man (hurtigt) <u>dividere R16 med 2</u>? R16 indeholder et positivt tal.

**A:** ROR R16

**B**: **ROL R16** 

**C**: LSR R16

**D**: LSL R16

**E**: DIV R16,2



### Test ("socrative.com": Room = MSYS)

Hvordan kan man (hurtigt) gange R16 med 2 ? R16 indeholder et positivt tal.

**A:** ROR R16

**B**: **ROL R16** 

**C**: LSR R16

**D**: LSL R16

**E**: ASR R16



## LAB5, del 1

<b>MSB</b> (bit 31)	<b>Tal 1:</b>	<b>LSB</b> (bit 0)	
R19	R18	R17	R16
<b>MSB</b> (bit 31)	<b>Tal 2:</b>	LSB (bit 0)	
R23	R22	R21	R20
<b>MSB</b> (bit 31)	Sum efter ad	LSB (bit 0)	
R19	R18	R17	R16

1 milliard + 2 milliarder = ?



### LAB5, del 2

- Hvis trykknap SW7 aktiveres:
   Talværdien på PORTB inkrementeres.
- Hvis trykknap SW6 aktiveres:
   Talværdien på PORTB dekrementeres.
- Hvis trykknap SW5 aktiveres:
   Værdien på [LED7,LED6,LED5,LED4] "bytter plads med" [LED3,LED2,LED1,LED0].
- Hvis trykknap SW4 aktiveres:
   Alle lysdioderne skifter tilstand (fra tændt til slukket og omvendt).
- Hvis trykknap SW3 aktiveres:
   Talværdien på PORTB divideres med 8.
- Hvis trykknap SW2 aktiveres:
   Talværdien på PORTB divideres med 7 (Hint: Se side 167 i lærebogen).
- Hvis trykknap SW1 aktiveres:
   LED7 og LED0 slukkes, mens de andre LEDs skal være uændrede.
- Hvis trykknap SW0 aktiveres:
   LED7 og LED0 tændes, mens de andre LEDs skal være uændrede.



### LAB5, del 3 (hvis tid)

```
:****** LED OFF *******
;***** Slukker en LED på PB ****
;***** Bit nr.(0-7) i R20
LED OFF:
  LDI R21,1
                      R21 = 00000000001
  CPI R20,0
  BREQ KLAR1
                      ;Hop, hvis LED nr. = 0
IGEN1:
  LSL R21
                      :Venstre-skift R21
                      ;ialt "LED nr." pladser
  DEC R20
  BRNE IGEN1
KLAR1:
  COM R21
                      ;Inverter "masken"
      R20,PINB ;Aflæs alle LEDs
  IN
  AND R20,R21 ;- lav bitvis AND
      PORTB,R20 ;- og skriv ud til LEDs igen
  OUT
  RET
:****** LED ON ********
;***** Taender en LED på PB ****
:***** Bit nr.(0-7) i R20
LED ON:
  ;<----- Skriv den manglende kode her</p>
  RET
*******************
```



# Slut på lektion 9



