# Unbounded Scene Modeling

Lingjie Liu

Sept 23, 2024

#### Announcements for Next Week's Classes



Jiahui Lei (Senior PhD at Penn) Sept 30 (Monday) 3:30-5PM



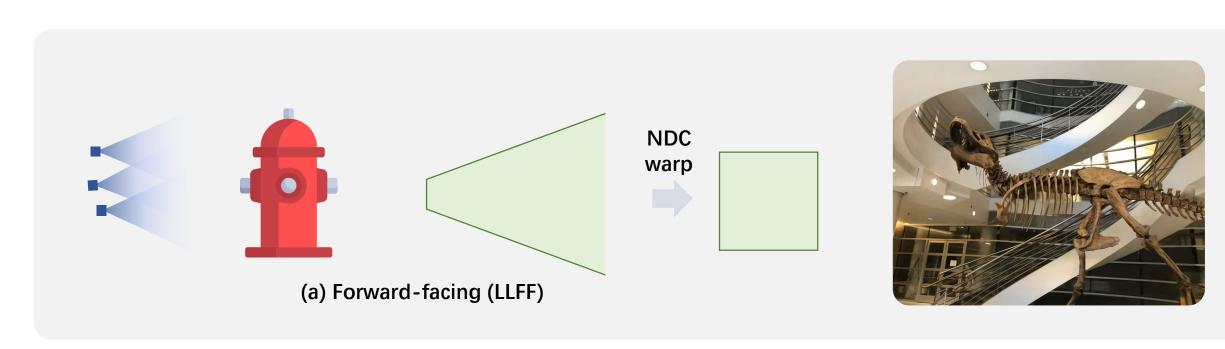
Oct 2 (Wed) 3:30-5PM

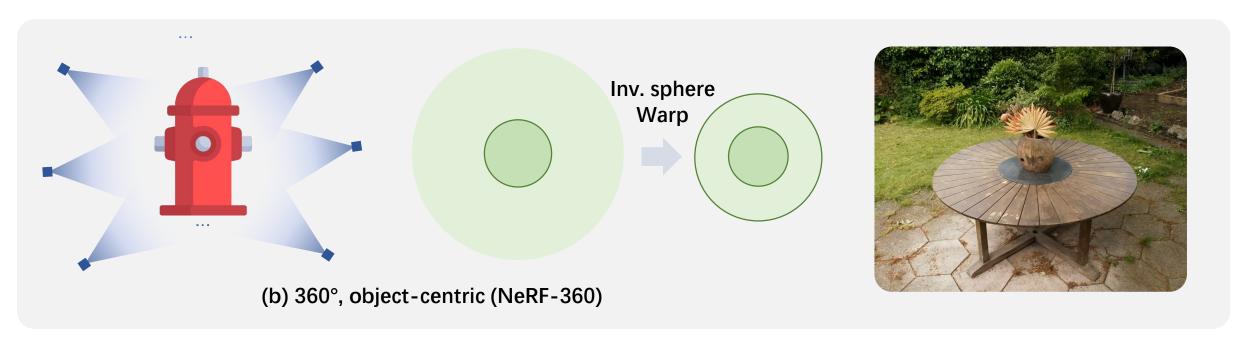
### Background: NeRF rendering of unbounded scene/open scene



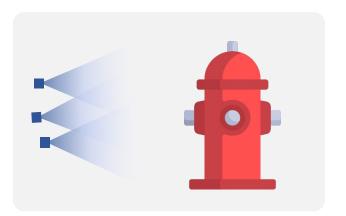


Bounded Unbounded

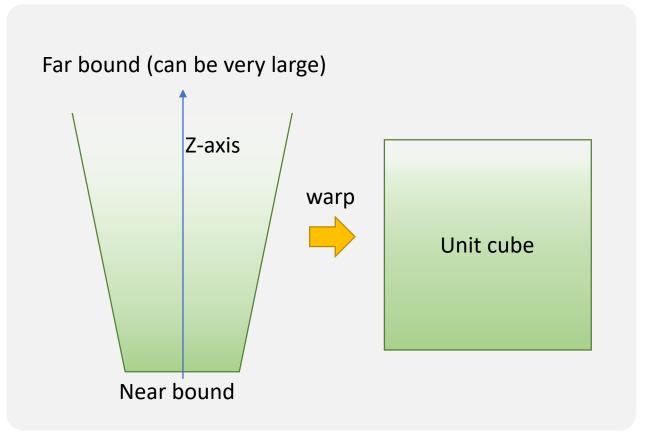




# NDC space warping



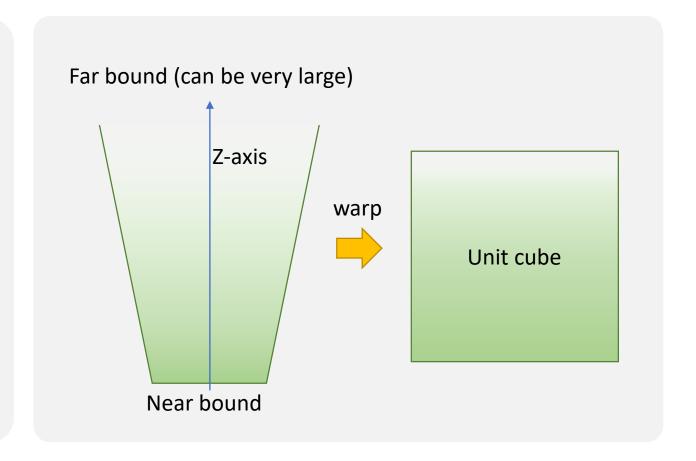




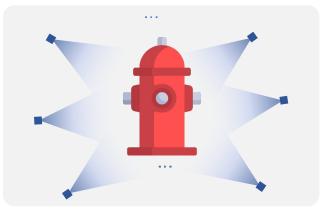
### NDC space warping

$$\begin{pmatrix} \frac{n}{r} & 0 & 0 & 0 \\ 0 & \frac{n}{t} & 0 & 0 \\ 0 & 0 & \frac{-(f+n)}{f-n} & \frac{-2fn}{f-n} \\ 0 & 0 & -1 & 0 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \\ 1 \end{pmatrix} = \begin{pmatrix} \frac{n}{r}x \\ \frac{n}{t}y \\ \frac{-(f+n)}{f-n}z - \frac{-2fn}{f-n} \\ -z \end{pmatrix}$$

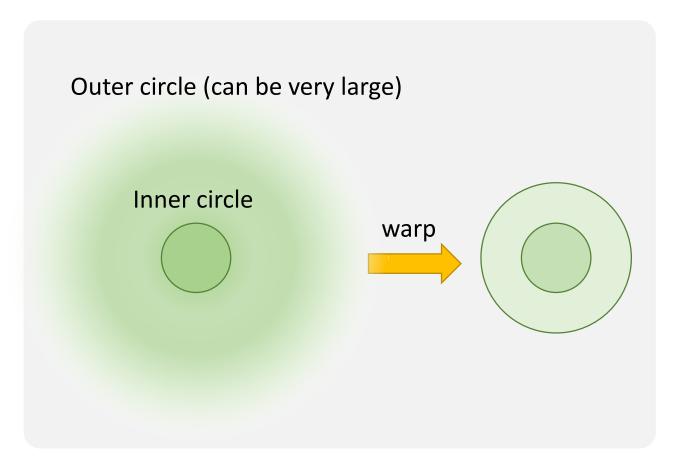
$$\text{project} \to \begin{pmatrix} \frac{n}{r} \frac{x}{r-z} \\ \frac{n}{t} \frac{y}{r-z} \\ \frac{n}{t-z} \\ \frac{(f+n)}{f-n} - \frac{2fn}{f-n} \frac{1}{-z} \end{pmatrix}$$



# Inverse sphere space warping

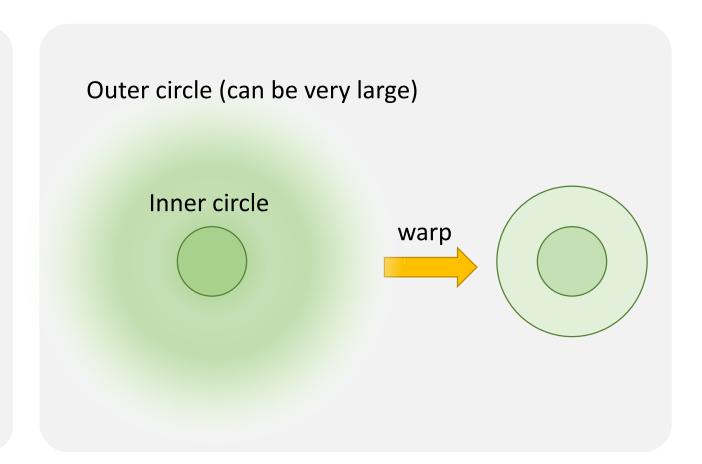






# Inverse sphere space warping (contraction)

contract(
$$\mathbf{x}$$
) = 
$$\begin{cases} \mathbf{x} & \|\mathbf{x}\| \le 1 \\ \left(2 - \frac{1}{\|\mathbf{x}\|}\right) \left(\frac{\mathbf{x}}{\|\mathbf{x}\|}\right) & \|\mathbf{x}\| > 1 \end{cases}$$





# F<sup>2</sup>-NeRF: Fast Neural Radiance Field Training with Free Camera Trajectories

Peng Wang<sup>1,2\*</sup>, Yuan Liu<sup>1\*</sup>, Zhaoxi Chen<sup>2</sup>, Lingjie Liu<sup>3</sup>, Ziwei Liu<sup>2</sup>, Taku Komura<sup>1</sup>, Christian Theobalt<sup>3</sup>, Wenping Wang<sup>4</sup>

<sup>1</sup>The University of Hong Kong

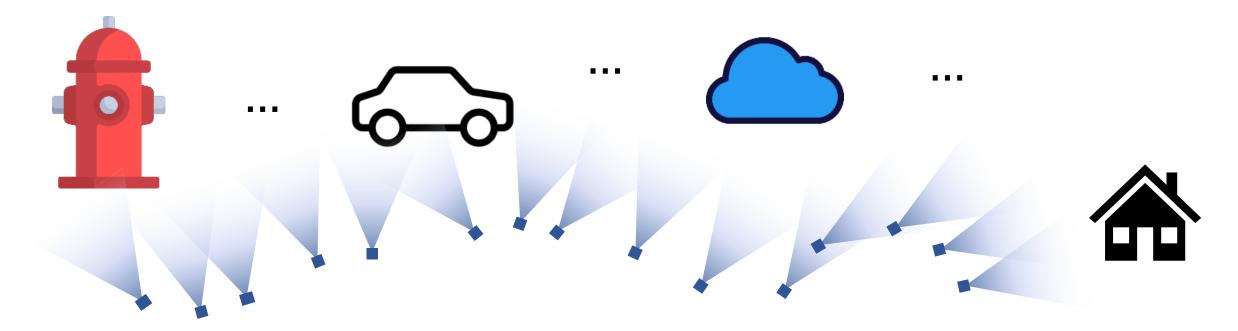
<sup>3</sup>MPI Informatics, Saarland Informatics Campus

<sup>2</sup>S-Lab, Nanyang Technological University

<sup>4</sup>Texas A&M University

### Problem

What if the input camera trajectory is very irregular?



#### What if the input camera trajectory is very irregular? – We call that a "free" trajectory



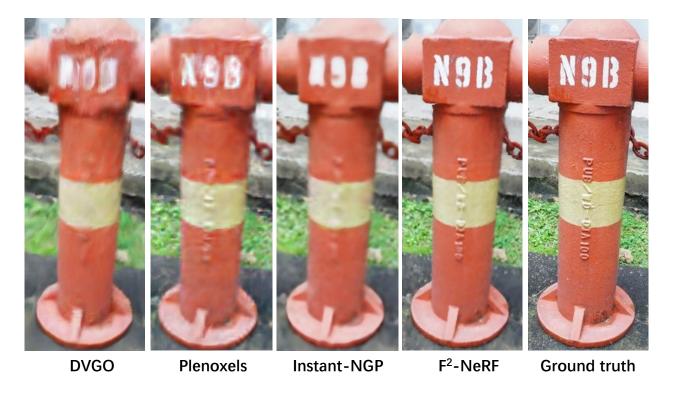






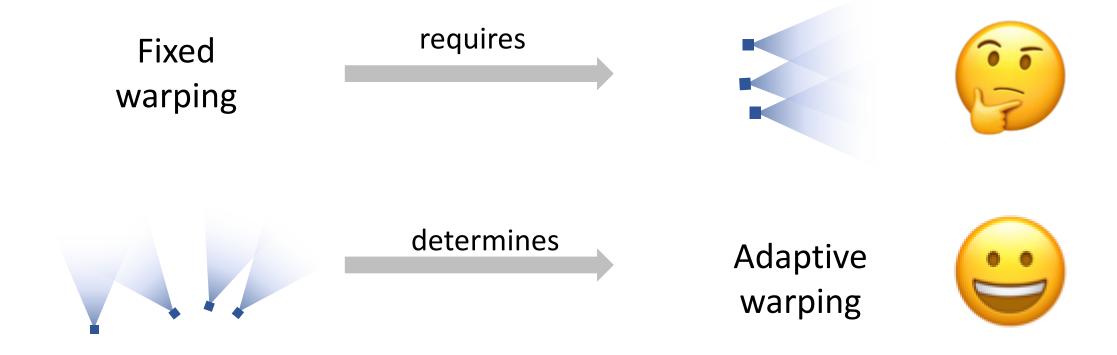
# When the trajectory is irregular...





#### Our idea

Adaptive warping method from input trajectories



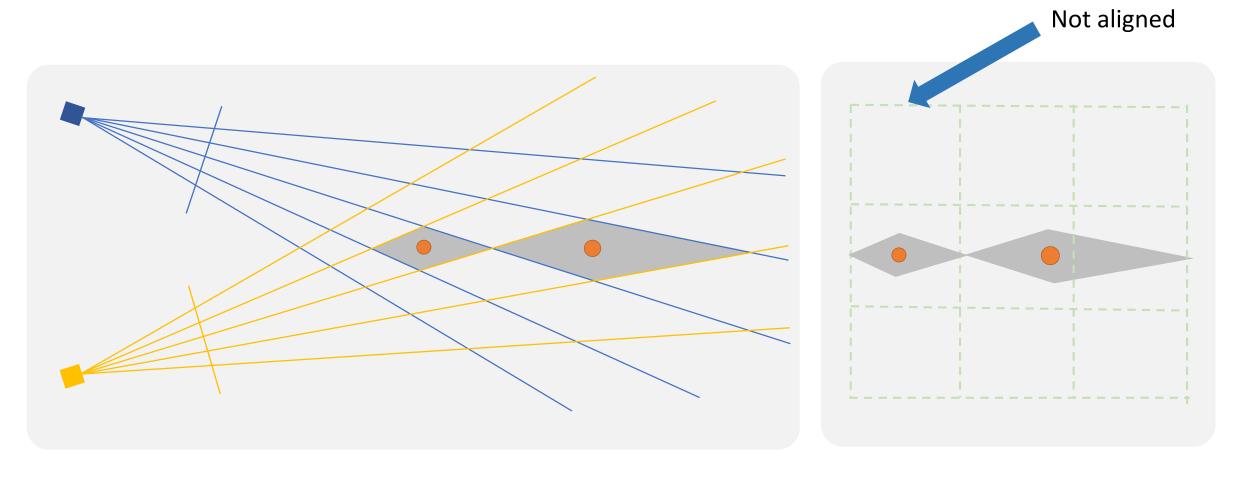
# Why space warping

Very far region

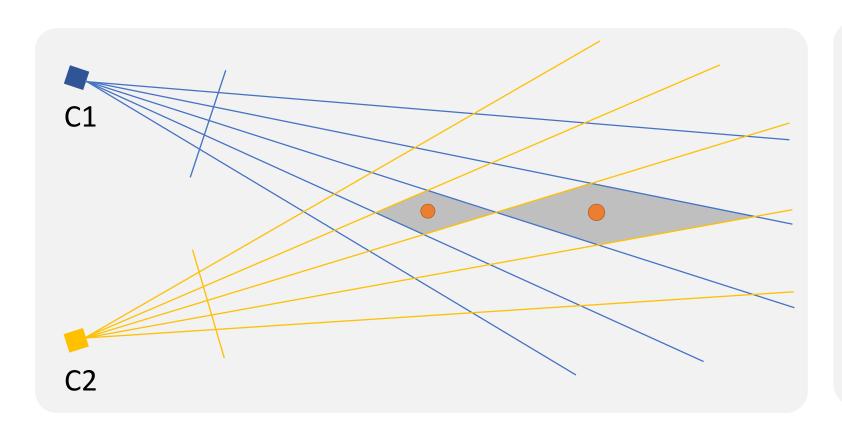
The "resolution" of the scene is spatial-variant

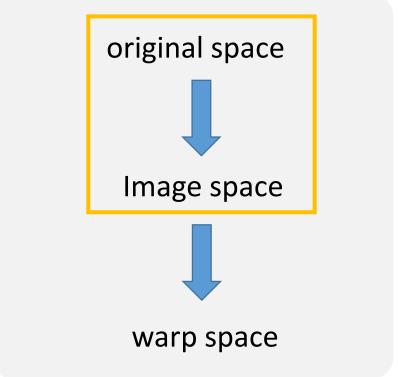


# Why space warping



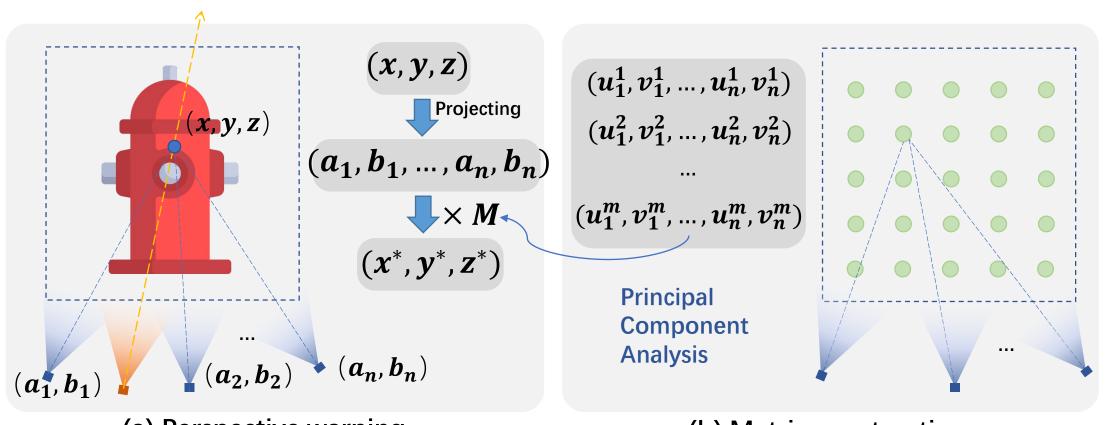
# Key idea: Perspective warping (2D)





$$F(\mathbf{x}) = (C_1(\mathbf{x}), C_2(\mathbf{x}))$$

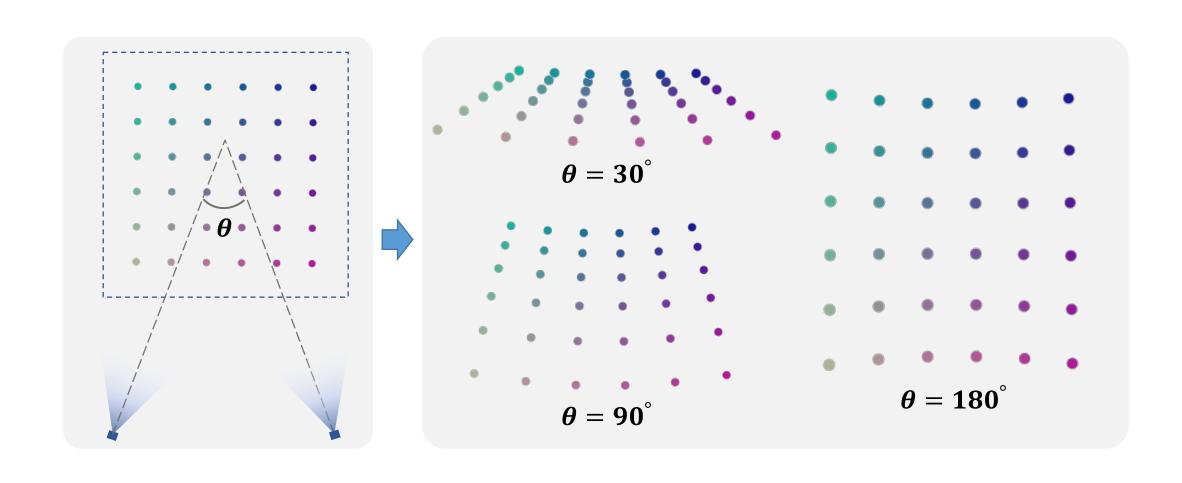
# Key idea: Perspective warping (3D)



(a) Perspective warping

(b) Matrix construction

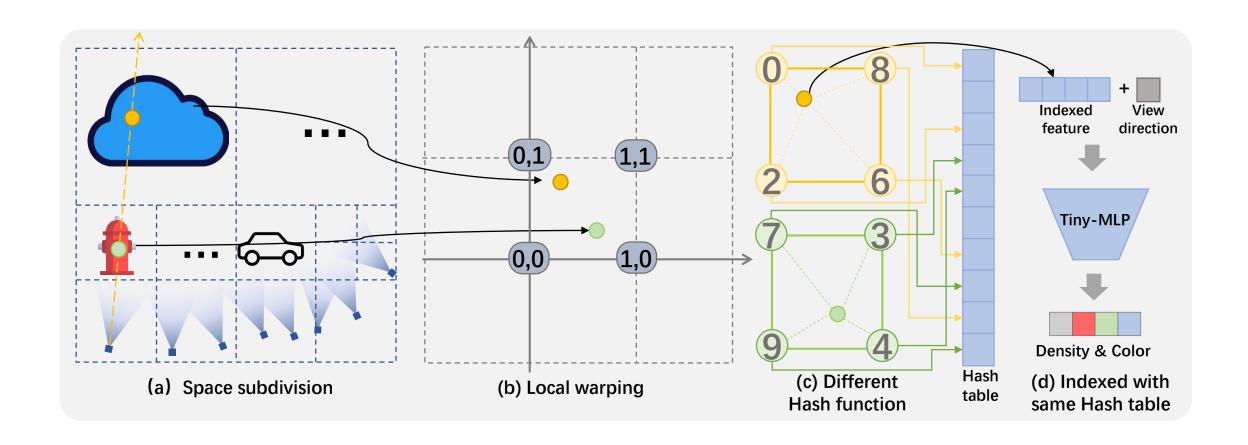
# Visualization of perspective warping



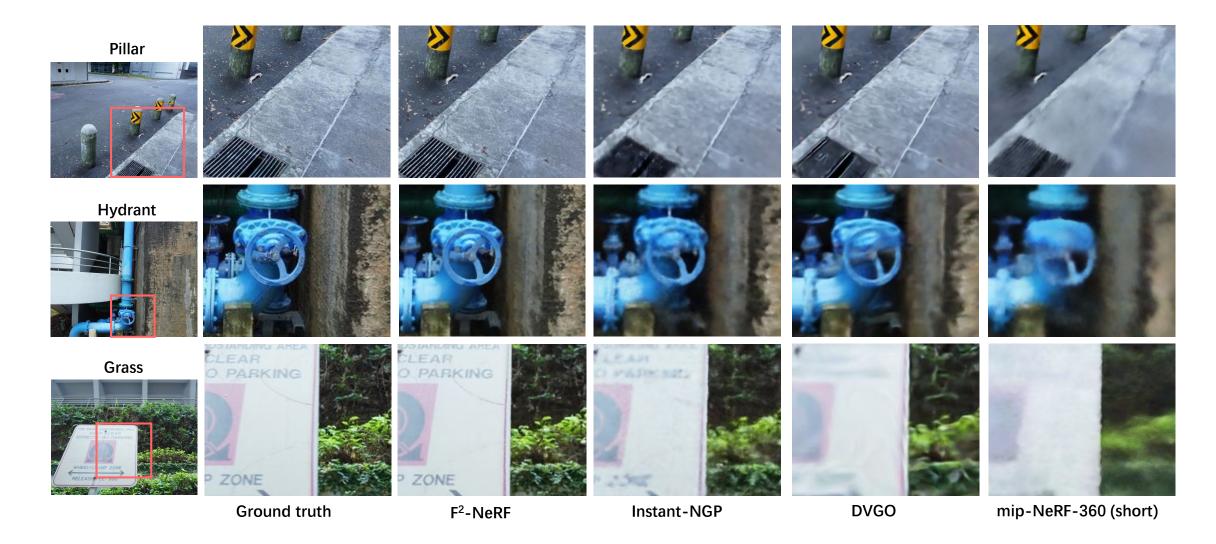
# Pipeline



# Pipeline



# Visual comparisons





**Hydrant** 





Instant-NGP





F<sup>2</sup>-NeRF



Pillar



Mip-NeRF-360 (short)



Instant-NGP



DVGO



F<sup>2</sup>-NeRF

### Quantitative results

Method	Tr. time	PSNR↑	SSIM↑	LPIPS(VGG)↓
NeRF++ [62]	hours	23.47	0.603	0.499
mip-NeRF-360 [3]	hours	27.01	0.766	0.295
mip-NeRF-360 <sub>short</sub>	30m	22.04	0.537	0.586
Plenoxels [58]	25m	19.13	0.507	0.543
DVGO [39]	21m	23.90	0.651	0.455
Instant-NGP [26]	6m	24.43	0.677	0.413
F <sup>2</sup> -NeRF	12m	26.32	0.779	0.276

Table 1. Results on the Free dataset. In mip-NeRF- $360_{\rm short}$ , we early stop the training to make them finished in 30 minutes. Training times are evaluated on a 2080ti GPU.

Method	Tr. time	PSNR↑	SSIM↑	LPIPS(VGG)↓
NeRF++ [62]	hours	26.21	0.729	0.348
mip-NeRF-360 [2]	hours	28.94	0.837	0.208
Plenoxels [58]	22m	23.35	0.651	0.471
DVGO [39]	16m	25.42	0.695	0.429
Instant-NGP [26]	6m	26.24	0.716	0.404
F <sup>2</sup> -NeRF	14m	26.39	0.746	0.361

Table 2. Results on the NeRF-360-V2 dataset.

Method	Tr. time	PSNR↑	SSIM↑	LPIPS(VGG)
NeRF [25]	hours	26.50	0.811	0.250
mip-NeRF [2]	hours	26.60	0.814	0.246
Plenoxels [58]	17m	26.29	0.839	0.210
DVGO [39]	11m	26.34	0.838	0.197
TensoRF [6]	48m	26.73	0.839	0.204
Instant-NGP [26]	6m	25.09	0.758	0.267
F <sup>2</sup> -NeRF	13m	26.54	0.844	0.189

Table 3. Results on the LLFF dataset.

#### Conclusion

- A complete pipeline for novel view synthesis with arbitrary camera trajectories
- An adaptive warping method for space compression of general scenes
- Fast to train with anchored neural hash grids

#### Limitations:

- Discontinuity on borders of sub-regions
- Aliasing
- Extremely large (>1k images) training data?

# Aliasing



# Thanks

Project page: http://totoro97.github.io/projects/f2-nerf

