

Problem 1

Using the impulse invariance method for analog to digital filter conversion, calculate the Chebyshev lowpass digital filter with parameters: passband frequency 20MHz; stopband frequency = 22MHz; passband ripple 0.5dB; stopband (out-of-band) attenuation 70dB; sampling frequency $F_s = 60\text{MHz}$.

- a) Plot the impulse response for both analog and digital systems.
- b) Plot the magnitude response for analog and digital systems in the frequency domain.

Provide code.

Problem 2

Implement a digital prototype of the analog filter with the transfer function

$$H(s) = \frac{s + 2.5}{s^2 + 2.5s + 4}$$

using the Bilinear Transformation. The sample clock frequency is $F_s = 20\text{Hz}$.

- a) Determine the Linear Difference Equation of the digital filter.
- b) Plot impulse and frequency responses for digital and analog filters.

Provide code.

Problem 3

A filter has the transfer function

$$H(z) = 3 + 4z^{-1} + 6z^{-2} + 8z^{-3}$$

Determine the impulse response of the filter with the modified frequency response

$$F(\omega) = H(\omega - 3\pi/4).$$

Problem 4

For a linear system with the transfer function

$$H(z) = \frac{z + 1}{z^3 + z^2 + 2z + 2}$$

- a) Calculate the difference equation relating the input $x[n]$ to the output $y[n]$
- b) Design block diagram realizations (Direct-Form 1 and Direct-Form 2)
- c) Plot impulse and frequency responses

Provide code.

Problem 5

Using 10-steps CORDIC algorithm, calculate

- a) $\arctan(1.5)$
- b) $\text{abs}(2.2 + 3.3j)$

Justify the approach. Compare with the actual value. Provide code.