AI1110 Assignment 1

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I. QUESTION 3 (A)

<u>Question:</u>

Simplify

$$\sin A \begin{pmatrix} \sin A & -\cos A \\ \cos A & \sin A \end{pmatrix} + \cos A \begin{pmatrix} \cos A & \sin A \\ -\sin A & \cos A \end{pmatrix} \quad (1)$$

<u>Solution:</u>

Let,

$$\mathbf{R}_\theta = \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix} \quad (2)$$

The matrix expression in the question can be written as

$$\left(\mathbf{R_A}^T \begin{pmatrix} \mathbf{R}_{\frac{\pi}{2}} & \mathbf{R_0} \end{pmatrix}\right) \cdot \begin{pmatrix} \sin A & \cos A \end{pmatrix} \quad (3)$$

Taking dot product of the vectors

$$\begin{pmatrix} \sin^2 A & -\sin A \cos A \\ \sin A \cos A & \sin^2 A \end{pmatrix}$$
$$+ \begin{pmatrix} \cos^2 A & \cos A \sin A \\ -\cos A \sin A & \cos^2 A \end{pmatrix} \quad (4)$$

Adding the matrices

$$\begin{pmatrix} \sin^2 A + \cos^2 A & -\sin A \cos A + \cos A \sin A \\ \sin A \cos A - \cos A \sin A & \sin^2 A + \cos^2 A \end{pmatrix} \quad (5)$$

Simplifying the elements finally gives

$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \quad (6)$$