## AI1110 Assignment 1

## Dondapati Chandrahas Reddy AI21BTECH11010

ICSE Grade 10 2019 paper

## I. QUESTION 3 (A)

Question:

Simplify

$$\sin A \begin{pmatrix} \sin A & -\cos A \\ \cos A & \sin A \end{pmatrix} + \cos A \begin{pmatrix} \cos A & \sin A \\ -\sin A & \cos A \end{pmatrix}$$

Solution:

Let,

$$\mathbf{R}_{\theta} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \tag{2}$$

The matrix expression in the question can be written as

$$\left(\mathbf{R_A}^T \begin{pmatrix} \mathbf{R}_{\frac{\pi}{2}} & \mathbf{R_0} \end{pmatrix}\right) \begin{pmatrix} \sin A \\ \cos A \end{pmatrix} \tag{3}$$

Taking dot product of the vectors

$$\begin{pmatrix}
\sin^2 A & -\sin A \cos A \\
\sin A \cos A & \sin^2 A
\end{pmatrix} + \begin{pmatrix}
\cos^2 A & \cos A \sin A \\
-\cos A \sin A & \cos^2 A
\end{pmatrix} (4)$$

Adding the matrices

$$\begin{pmatrix}
\sin^2 A + \cos^2 A & -\sin A \cos A + \cos A \sin A \\
\sin A \cos A - \cos A \sin A & \sin^2 A + \cos^2 A \\
(5)
\end{pmatrix}$$

Simplifying the elements finally gives

$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \tag{6}$$