

1. Mean for Philip = 19.2

Mean for Matthews = 20.4
Arithmatic mean

Median for Philip = 20] middle
n for Matthews = 25] value
after sorting

Mode for Philip = 20 → most
n for Matthews = 30 → first
value

Range = Max - Min $\approx 21 - 15 = 6$
for Philip

Range for Matthews = $35 - 0 = 35$

In order to measure consistency, we need
to calculate std for both Philip &
Matthews.

$$\begin{aligned}
 \text{Var}_P &= \frac{1}{5} \left[(15-19.2)^2 + (21-19.2)^2 + 3(20-19.2)^2 \right] \\
 &= \frac{1}{5} [17.64 + 3.24 + 1.92] \\
 &= 4.56
 \end{aligned}$$

$$\text{std}_P = \underline{2.14} (\sqrt{4.56})$$

$$\begin{aligned}
 \text{Var}_M &= \frac{1}{5} \left[(30-20.4)^2 + (25-20.4)^2 \right. \\
 &\quad \left. + (12-20.4)^2 + (35-20.4)^2 \right. \\
 &\quad \left. + (0-20.4)^2 \right]
 \end{aligned}$$

$$\begin{aligned}
 &= \frac{1}{5} \left[92.16 + 21.16 + 70.56 \right. \\
 &\quad \left. + 213.16 + 416.16 \right]
 \end{aligned}$$

$$= 162.64$$

$$\text{std}_M = \underline{\sqrt{162.64}} = 12.75$$

Seeing both the range & standard deviation, we can say that Philip is more consistent.

2.

$$65 \ 72 \ 58 \ 77 \Rightarrow 58 \ 65 \ 72 \ 77$$

Mean of first 4 matches = $\frac{65 + 72 + 58 + 77}{4}$

$$= 68$$

Median = $\frac{72 + 58}{2} = \frac{65 + 72}{2} = 68.5$

b) New mean after 5th match = $\frac{65 + 72 + 58 + 77 + 70}{5}$

$$= 68.4$$

58 65 70 72 77
new median = 70.

c) Median is increased by 1.3 runs

3. 8 6 2 4 6 8 10 8

Mode = 8

4. Q8.5 Arranging the scores in ascending order.

0 0 5.25 5.5 6 6 6.5 6.75 7 7.5 7.5
8.5 8.5 8.75 8.75 9 9.5 9.5 10 10 10 10.5 10.5 11

$$\text{spread} = \text{max} - \text{min} = 11 - 0 = 11$$

$$Q_1 = \frac{n+1}{4} \text{th} = \frac{26+1}{4} = 8.5 \text{th element}$$

~~2 3 5 6 8 10 12 14~~

$$Q_2 = 2 \left(\frac{n+1}{4} \right) \text{th} = 2 \left(\frac{26}{4} \right) = 13 \text{th element}$$

~~2 3 5 6 8 10 12 14~~

$$Q_3 = 3 \left(\frac{n+1}{4} \right) \text{th} = 3 \left(\frac{26}{4} \right) = 19.5 \text{th element}$$

~~2 3 5 6 8 10 12 14~~

5. Range₁ = max - min = 43 - 29 = 14

$$\text{range}_2 = 40 - 20 = 20$$

$$\text{range}_3 = 41 - 23 = 18$$

$$\text{range}_4 = 37 - 20 = 17$$

$$\text{range}_5 = 43 - 19 = 24$$

city 3

8

city 4

are close

$$\text{mean}_1 = 33.83$$

$$\text{mean}_2 = 31.58$$

$$\text{mean}_3 = 32.91$$

$$\text{mean}_4 = 29.75$$

$$\text{mean}_5 = 31.66$$

city 2
&
city 5
are close.

Q12

$$\text{Var} = \frac{1}{12} \left[(29 - 33.83)^2 + \right.$$

calculating standard deviation using Python
since it is a huge set.

$$s_1 = 4.15$$

$$s_2 = 6.21$$

$$s_3 = 5.66$$

$$s_4 = 5.1$$

$$s_5 = 6.76$$

city 2

&

city 3

are close

$$(6.21 - 5.66) = 0.55$$

$$\underline{s_3 - s_4 = 0.55}$$

Formula: Variance = $\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2$

Standard deviation = $\sqrt{\text{Variance}}$

$$6. \quad 82 \ 72 \ 85 \ 14, \ 66.$$

$$\text{Mean} = \frac{82 + 72 + 85 + 14 + 66}{5}$$
$$= 63.8$$

$$\text{Var} = \frac{1}{5} \left[(82 - 63.8)^2 + (72 - 63.8)^2 + (85 - 63.8)^2 + (14 - 63.8)^2 + (66 - 63.8)^2 \right]$$

$$= \frac{1}{5} \left[331.24 + 87.24 + 449.24 + 2480.04 + 4.84 \right]$$

$$= 666.52$$

$$6 = \sqrt{666.52} = 25.81$$

$$Z_1 = \frac{82 - 63.8}{25.81} = 0.70$$

$$Z_2 = \frac{72 - 63.8}{25.81} = 0.31$$

$$Z_3 = \frac{85 - 63.8}{25.81} = 0.82$$

$$Z_4 = \frac{14 - 63.8}{25.81} = -1.92$$

$$Z_5 = \frac{66 - 63.8}{25.81} = 0.08$$

f. $\mu_A = 0.7$, $\sigma_A = 0.2$

$$\mu_B = 0.4, \sigma_B = 0.1$$

$$Z_A = \frac{0.75 - 0.7}{0.2} = 0.25$$

$$Z_B = \frac{0.55 - 0.4}{0.1} = 1.5$$

B did better than his personal record