

I2I-2 Functional Verification Example Exercises

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1 Treecount

The following OCaml functions are given:

```
1 type node = Leaf of int | Inner of node * node
2
3 let rec count_leaves t = match t with
4   | Leaf _ -> 1
5   | Inner (l, r) -> count_leaves l + count_leaves r
6
7 let rec count_inner t = match t with
8   | Leaf _ -> 0
9   | Inner (l, r) -> 1 + count_inner l + count_inner r
10
11
12 (* count_leaves t = count_inner t + 1 *)
```

Prove that the equality

```
1 count_leaves t = count_inner t + 1
```

holds.

2 Dacentrili

The following OCaml functions are given:

```
1 let rec damcentravi a lst = match lst with
2   | [] -> a
3   | h::t -> damcentravi (h::(List.rev a)) t
4
5 let rec get_nth n lst = match lst with
6   | [] -> 0
7   | h::t -> if n = 0 then h else get_nth (n-1) t
8
9 let pick_middle lst = get_nth ((List.length lst) / 2) lst;;
```

Prove that the equality

```
1 a = pick_middle (damcentravi [] (a::b))
```

holds.

3 Even list

The following OCaml functions are given:

```
1 let rec el a lst = match lst with
2   | h::_::t -> el (h::a) t
3   | [h] -> el (h::a) []
4   | [] -> a
5
6 let rec de i a lst = match lst with
7   | h::t -> de (i+1) (if i mod 2 = 0 then h::a else a) t
8   | [] -> a
```

Prove that the equality

```
1 de 0 [] 1 = el [] 1
```

holds.

4 Bigotree

The following OCaml functions are given:

```
1 type node = Empty | Inner of node * int * node
2
3 let rec insertintree v t = match t with
4   | Empty -> Inner (Empty, v, Empty)
5   | Inner (l, u, r) -> if v > u then
6       Inner (l, u, insertintree v r)
7   else
8       Inner (insertintree v l, u, r)
9
10 let rec totree a lst = match lst with
11   | [] -> a
12   | h::t -> insertintree h (totree a t)
13
14 let rec tolist t = match t with
15   | Empty -> []
16   | Inner (l, v, r) -> tolist l @ [v] @ tolist r
17
18 let rec insert n lst = match lst with
19   | [] -> [n]
20   | h::t -> if n > h then
21       h::(insert n t)
22   else
23       n::h::t
24
25 let rec sort lst = match lst with
26   | [] -> []
27   | h::t -> insert h (sort t)
```

Prove that the equality

```
1 tolist (totree Empty l) = sort l
```

holds.