

1.
 - a. $9 \bmod 4 = [1]_4$
 - b. $29 \bmod 5 = [4]_5$
 - c. $24 \bmod 9 = [6]_9$
2.
 - a. $49 \equiv 7k \bmod 7 \forall k \in \mathbb{Z}$
 - b. $80 \equiv 15k + 5 \bmod 15 \forall k \in \mathbb{Z}$
 - c. $43 \equiv 7k + 1 \bmod 7 \forall k \in \mathbb{Z}$
3.
 - a. $-18 \bmod 7 \equiv \text{undefined}$
 - b. $63 \equiv \text{undefined} \bmod 5$
 - c. $-12 \bmod 14 = 2$

2.
 - $195 \equiv 6 \bmod 10$ is false
 - $195 \equiv 5 \bmod 10'$ is true
 - $195 \equiv -6 \bmod 10$ is false

- $(195 \bmod 10) = 5$ is true
- $(195 \bmod 10) = -5$ is false
- $(195 \bmod 10) = -5$ is true

3.
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$$\begin{aligned}
 \text{maxint} + 1 \bmod K &= \left(\frac{K}{2} - 1\right) + 1 \bmod K \\
 &= \frac{K}{2} \bmod K \\
 &= -\frac{K}{2} \\
 &= \text{minint}
 \end{aligned}$$

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$$\begin{aligned}
 -\text{minint} \bmod K &= -\left(-\frac{K}{2}\right) \bmod K \\
 &= \frac{K}{2} \bmod K \\
 &= -\frac{K}{2} \\
 &= \text{minint}
 \end{aligned}$$

4.
 - a. $[1100111] = -25$
 - b. $[011110] = 30$
 - c. $[11111111111111111011110110] = -266$

- 5.

$$\langle a \rangle - \langle b \rangle = \langle a \rangle + \langle \bar{b} \rangle + 1$$

If we try to subtract $\langle 0010 \rangle$ from $\langle 0100 \rangle$ with the given formula, we get

$$\begin{aligned}
 \langle 0100 \rangle - \langle 0010 \rangle &= \langle 0100 \rangle + \langle \overline{0010} \rangle + 1 \\
 &= \langle 0100 \rangle + \langle 1101 \rangle + 1 \\
 &= \langle 0100 \rangle + \langle 1110 \rangle = \langle 10010 \rangle \implies \\
 &4 - 2 = 18
 \end{aligned}$$

which clearly, is not true, therefore the above equation is not true for all $a, b \in \mathbb{B}^n$.

6. a.

$$\begin{aligned}
\langle 1001101 \rangle - \langle 0111101 \rangle &= \langle 1001101 \rangle + \langle \overline{0111101} \rangle + 1 \pmod{2^7} \\
&= \langle 1001101 \rangle + \langle 1000010 \rangle + 1 \\
&= \langle 1001101 \rangle + \langle 1000011 \rangle \\
&= \langle 0010000 \rangle = 16_{10}
\end{aligned}$$

b.

$$\begin{aligned}
\langle 101111 \rangle - \langle 110 \rangle &= \langle 101111 \rangle - \langle 000110 \rangle \\
&= \langle 101111 \rangle + \langle \overline{000110} \rangle + 1 \pmod{2^6} \\
&= \langle 101111 \rangle + \langle 111001 \rangle + 1 \\
&= \langle 101111 \rangle + \langle 111010 \rangle \\
&= \langle 101001 \rangle = 41_{10}
\end{aligned}$$

c.

$$\begin{aligned}
\langle 110011 \rangle - \langle 01111 \rangle &= \langle 110011 \rangle - \langle 001111 \rangle \\
&= \langle 110011 \rangle + \langle \overline{001111} \rangle + 1 \pmod{2^6} \\
&= \langle 110011 \rangle + \langle 110000 \rangle + 1 \\
&= \langle 110011 \rangle + \langle 110001 \rangle \\
&= \langle 100100 \rangle = 36_{10}
\end{aligned}$$

7. $7 \cdot 3$