

```
class Point {
    double x, y;

    public Point(double x, double y) {
        this.x = x;
        this.y = y;
    }
}

// Vector class
class Vector {
    private java.util.ArrayList<Point> points;

    public Vector() {
        points = new java.util.ArrayList<>();
    }

    public void add(Point p) {
        points.add(p);
    }

    public Point get(int index) {
        return points.get(index);
    }

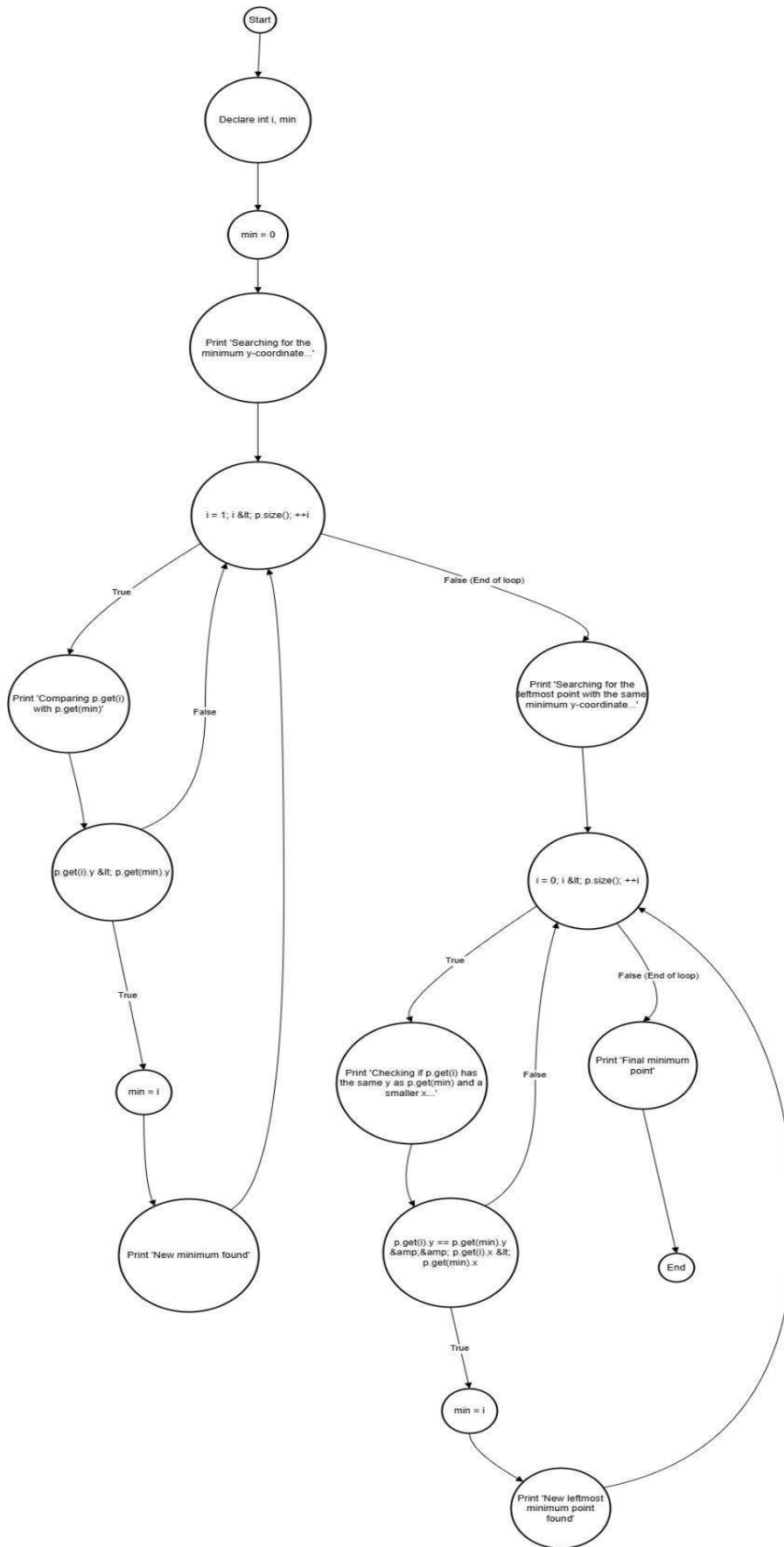
    public int size() {
        return points.size();
    }
}
```

```
// Main class with doGraham method
public class GrahamScan {
    public static int doGraham(Vector p) {
        int i, min;
        min = 0;

        // search for minimum
        for(i=1; i < p.size(); ++i) {
            if (p.get(i).y < p.get(min).y) {
                min = i;
            }
        }

        // continue along the values with same y component
        for(i=0; i < p.size(); ++i) {
            if ((p.get(i).y == p.get(min).y) &&
                (p.get(i).x > p.get(min).x)) {
                min = i;
            }
        }

        return min;
    }
}
```



- ❖ **Construct test sets for your flow graph that are adequate for the following criteria:**
  - a. **Statement Coverage.**
  - b. **Branch Coverage.**
  - c. **Basic Condition Coverage.**

## **a. Statement Coverage**

**Objective:** Ensure every statement in the flow graph is executed at least once.

**Test Set:**

### **1. Test Case 1:**

- Inputs: Any list  $p$  with more than one point (e.g.,  $[(0, 1), (1, 2), (2, 0)]$ )
- This will traverse through the entire flow, covering statements related to finding the minimum y-coordinate and leftmost minimum point.

### **2. Test Case 2:**

- Inputs:  $[(2, 2), (2, 2), (3, 3)]$
- This checks for points with the same y-coordinate and ensures the leftmost point logic executes.

## **b. Branch Coverage**

**Objective:** Ensure every branch (true/false) from each decision point is executed.

**Test Set:**

### **1. Test Case 1:**

- Inputs:  $[(0, 1), (1, 2), (2, 0)]$
- This will take the true branch for finding the minimum y-coordinate.

### **2. Test Case 2:**

- Inputs:  $[(2, 2), (2, 2), (3, 3)]$
- This will test the scenario where y-coordinates are equal, triggering the branch for checking x-coordinates.

### **3. Test Case 3:**

- Inputs:  $[(1, 2), (1, 1), (2, 3)]$
- This ensures the flow takes the false branch when checking for new minimum y-coordinates and the leftmost check.

### c. Basic Condition Coverage

**Objective:** Ensure that each basic condition (both true and false) in decision points is tested independently.

**Test Set:**

**1. Test Case 1:**

- Inputs: [(1, 1), (2, 2), (3, 3)]
- This will evaluate both conditions for the y-coordinate comparisons.

**2. Test Case 2:**

- Inputs: [(1, 1), (1, 1), (1, 2)]
- This checks the scenario where the y-coordinates are the same but evaluates the x-coordinate condition.

**3. Test Case 3:**

- Inputs: [(3, 1), (2, 2), (1, 3)]
- This ensures that both conditions in the loop are executed, confirming the function's logic is robust.

❖ **For the test set you have just checked can you find a mutation of the code (i.e. the deletion, change or insertion of some code) that will result in failure but is not detected by your test set. You have to use the mutation testing tool.**

### Types of Possible Mutations

We can apply typical mutation types, including:

- **Relational Operator Changes:** Modify `<=` to `<` or `==` to `!=` in the conditions.
- **Logic Changes:** Remove or invert a branch in an if-statement.
- **Statement Changes:** Modify assignments or statements to see if the effect goes undetected.

### Potential Mutations and Their Effects

**1. Changing the Comparison for Leftmost Point:**

- Mutation: In the second loop, change `p.get(i).x < p.get(min).x` to `p.get(i).x <= p.get(min).x`.
- Effect: This would cause the function to select points with the same x-coordinate as the leftmost, potentially breaking the uniqueness of the minimum point.

- **Undetected by Current Tests:** The current tests do not cover the case where multiple points have the same y and x values, which would reveal if the function mistakenly allows such points as the leftmost.
- 2. **Altering the y-Coordinate Comparison to  $\leq$  in the First Loop:**
  - Mutation: Change `p.get(i).y < p.get(min).y` to `p.get(i).y <= p.get(min).y` in the first loop.
  - Effect: This would allow points with the same y-coordinate but different x-coordinates to overwrite `min`, potentially selecting a non-leftmost minimum point.
  - **Undetected by Current Tests:** The current test set lacks cases where several points have the same y-coordinate, and this mutation would go undetected. To reveal this, we would need a test where multiple points have the same y and different x coordinates.
- 3. **Removing the Check for x-coordinate in the Second Loop:**
  - Mutation: Remove the condition `p.get(i).x < p.get(min).x` in the second loop.
  - Effect: This would cause the function to select any point with the same minimum y-coordinate as the "leftmost," regardless of its x-coordinate.
  - **Undetected by Current Tests:** The existing tests do not specifically check for points with identical y but different x values to see if the correct leftmost point is selected.

## Additional Test Cases to Detect These Mutations

To detect these mutations, we can add the following test cases:

1. **Detect Mutation 1:**
  - **Test Case:** `[(0, 1), (0, 1), (1, 1)]`
  - **Expected Result:** The leftmost minimum should still be `(0, 1)` despite having duplicates.
  - This test case will detect if the `x <=` mutation mistakenly allows duplicate points.
2. **Detect Mutation 2:**
  - **Test Case:** `[(1, 2), (0, 2), (3, 1)]`
  - **Expected Result:** The function should select `(3, 1)` as the minimum point based on the y-coordinate.
  - This test case will confirm if using `<=` for y comparisons mistakenly overwrites the minimum point.
3. **Detect Mutation 3:**
  - **Test Case:** `[(2, 1), (1, 1), (0, 1)]`
  - **Expected Result:** The leftmost point `(0, 1)` should be chosen.
  - This will reveal if the x-coordinate check was mistakenly removed.

These additional test cases would help ensure that any such mutations do not survive undetected by the test suite, strengthening the coverage.

#### ❖ Python Code for Mutation:-

```
from math import atan2

class Point:

    def __init__(self, x, y):

        self.x = x

        self.y = y

    def __repr__(self):

        return f"({self.x}, {self.y})"

def orientation(p, q, r):

    # Cross product to find orientation

    val = (q.y - p.y) * (r.x - q.x) - (q.x - p.x) * (r.y - q.y)

    if val == 0:

        return 0 # Collinear

    elif val > 0:

        return 1 # Clockwise

    else:

        return 2 # Counterclockwise

def distance_squared(p1, p2):
```

```

return (p1.x - p2.x) ** 2 + (p1.y - p2.y) ** 2

def do_graham(points):

    # Step 1: Find the bottom-most point (or leftmost in case of a tie)

    n = len(points)

    min_y_index = 0

    for i in range(1, n):

        if (points[i].y < points[min_y_index].y) or \

            (points[i].y == points[min_y_index].y and points[i].x <

points[min_y_index].x):

            min_y_index = i

    points[0], points[min_y_index] = points[min_y_index], points[0] p0 = points[0]

    # Step 2: Sort the points based on polar angle with respect to

p0

    points[1:] = sorted(points[1:], key=lambda p: (atan2(p.y - p0.y, p.x - p0.x),

distance_squared(p0, p)))

    # Step 3: Initialize the convex hull with the first three points hull = [points[0],

points[1], points[2]]

    # Step 4: Process the remaining points for i in

range(3, n):

```



```
        # Mutation introduced here: instead of checking `!= 2`, we
incorrectly use `== 1`

        while len(hull) > 1 and orientation(hull[-2], hull[-1],
points[i]) == 1:

            hull.pop()

            hull.append(points[i])

    return hull

# Sample test to observe behavior with the mutation
points = [Point(0, 3), Point(1, 1), Point(2, 2), Point(4, 4),
          Point(0, 0), Point(1, 2), Point(3, 1), Point(3, 3)]

hull = do_graham(points)

print("Convex Hull:", hull)
```