Ray - Cylinder Intersection à is normalized . We found we using the projection sormula $\|(x-c)\cdot a\| \cdot a\| = (x-c)\cdot a\|a\|$ $=(x-c)\cdot a$ because Vall=1. · Pythagora's rule for the triangle: 12+ W2 = 1x-c12 $f^2 + ((x-c) \cdot a)^2 - (x-c)^T (x-c) = 0$ replace x with the ray's equation:

 $r^2 + ((o+td-c)\cdot a)^2 - (o+td-c)^T (o+td-c) = 0$

Set
$$q=0-c$$
:
$$(2+((td+q)\cdot a)^{2}-(td+q)^{T}(td+q)=0$$

$$(2+((td+q)^{T}a)^{2}-(t^{2}d^{T}d+td^{T}q+tq^{T}d+q^{T}q)=0$$

$$(2+(td^{T}q+t^{T}q)^{2}-(t^{2}d^{T}d+td^{T}q+tq^{T}d+q^{T}q)=0$$

$$r^2 + \left(t^2 d^{T} a d^{T} a + 2t d^{T} a q^{T} a + q^{T} a q^{T} a\right) - t^2 d^{T} d - t q^{T} d - q^{T} q = 0$$

$$t^2 \left(d^{T} a d^{T} a - d^{T} d\right) + t \left(2d^{T} a q^{T} a - d^{T} q - q^{T} d\right) + \left(r^2 + q^{T} a q^{T} a - q^{T} q\right) = 0$$

$$a - d + there we solved the avadratic equation.$$

then we solved the quadratic equation.

Normal Derivations

Normal Denivation.

After solving for t in the previous section, we could express the location of intosection point using t.

In addition, we could solve for w and make use of the result to express the location of point β . (can be found in the graph in lost page).

With both location of χ and β , we could easily express the normal using formula $(\chi - \beta)$.

Point Alternation.

If one intersection point actually lands outside of the reachable distance from the center of the cylinder, we need to change to another intersection point and test of its within the height of cylinder.

We would compute w to see if it's within half if the height, if not, this means the current intersection point doesn't land on the cylinder.

We will proceed to charge to another uncheeked intersection point to make szere we don't reuse invalid intersection point.