

ATR Notes

$$C_k = (1 - \alpha_0) C_0 + \alpha_1 C^1 = C^0 \quad (2)$$

$$C^n = (1 - \alpha_n) C_{n+1} + \alpha_{n+1} C^{n+1}$$

$$\begin{aligned} C_k &= (1 - \alpha_0) C_0 + \alpha_0 \left((1 - \alpha_1) C_1 + \alpha_2 C^2 \right) \\ &= (1 - \alpha_0) C_0 + \alpha_0 \left((1 - \alpha_1) C_1 + \alpha_1 \left((1 - \alpha_2) C_2 + \alpha_2 C^3 \right) \right) = \\ C_0 &= 1 \end{aligned}$$

$$C_{(n \geq 1)} = 0$$

$$C_{(n \geq 1)} = \underbrace{(1 - \alpha_n) \times 0}_{0} + \underbrace{C^{n+1} \times \alpha_n}_0$$

also $n+1 \geq n \geq 1$

$$+ (1 - \alpha_{n+1}) \times 0 + C^{n+2} \times \alpha_{n+1}$$

$$C_k = \sum_{i=0}^N (1 - \alpha_i) C_i \left(\prod_{k=0}^{i-1} \alpha_k \right) \quad (7)$$

Induction

prove (7) for $N = 1$

$$(1) =$$

$$c_h = c_0 = (1 - \alpha_0) c_0 + \alpha_0 c^1$$

$$\text{let } p_n = (1 - \alpha_n) c_n$$

$$\Rightarrow c_h = \sum_{i=0}^{\infty} p_n x$$

$$(1 - \alpha_0) c_0 + (1 - \alpha_1) \alpha_0 c_1 + (1 - \alpha_2) \alpha_0 \alpha_1 c_2 + \alpha_0 \alpha_1 \alpha_2 c^3$$



