

## Report for Assignment 4: PCA and EM Algorithm

Course: CSE472 (Machine Learning Sessional)

Assignment Title: Principal Component Analysis (PCA) and Expectation-Maximization (EM) Algorithm

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### 1. How to Run the Code

1. Ensure the datasets `pca\_data.txt` and `em\_data.txt` are in the same directory as 1905028.ipynb file.
2. Install the required libraries by running the following command in your terminal:

***pip install numpy matplotlib sklearn umap-learn***

3. Open the provided Python code in Jupyter Notebook or any Python IDE that supports `.ipynb` files.
4. Run the code cell by cell. The code will:
  - Generate PCA, UMAP, and t-SNE plots.
  - Output the estimated parameters from the EM algorithm.

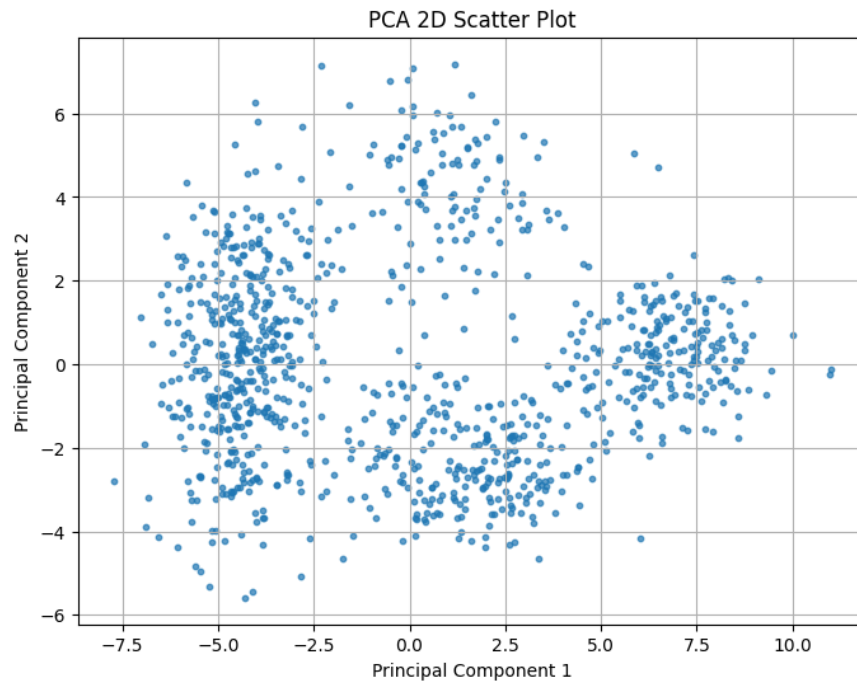
The datasets provided were:

1. `pca_data.txt` for PCA tasks (1000 samples, 500 features).
2. `em_data.txt` for EM tasks (1000 rows representing the number of children in hypothetical families).

## 2. Results

### 2.1 Principal Component Analysis (PCA)

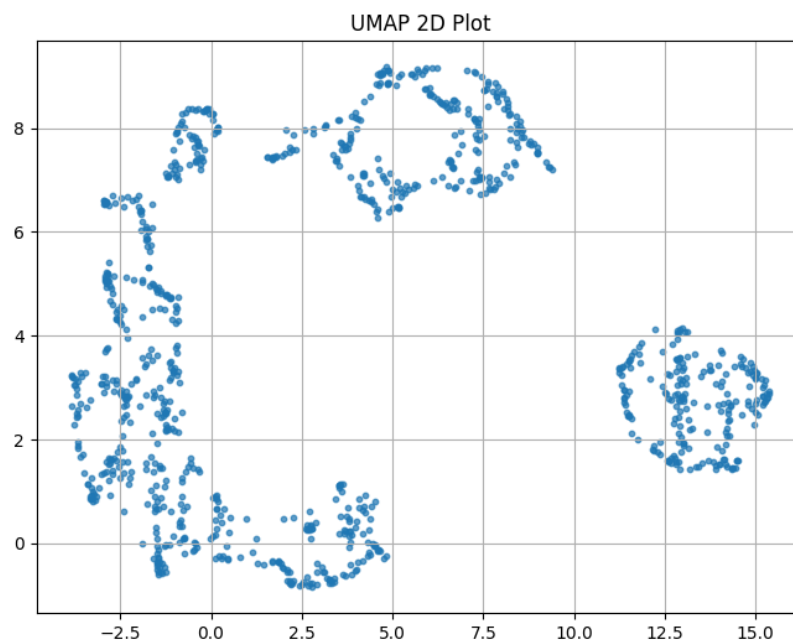
The scatter plot of the data projected onto the first two principal components is shown below.



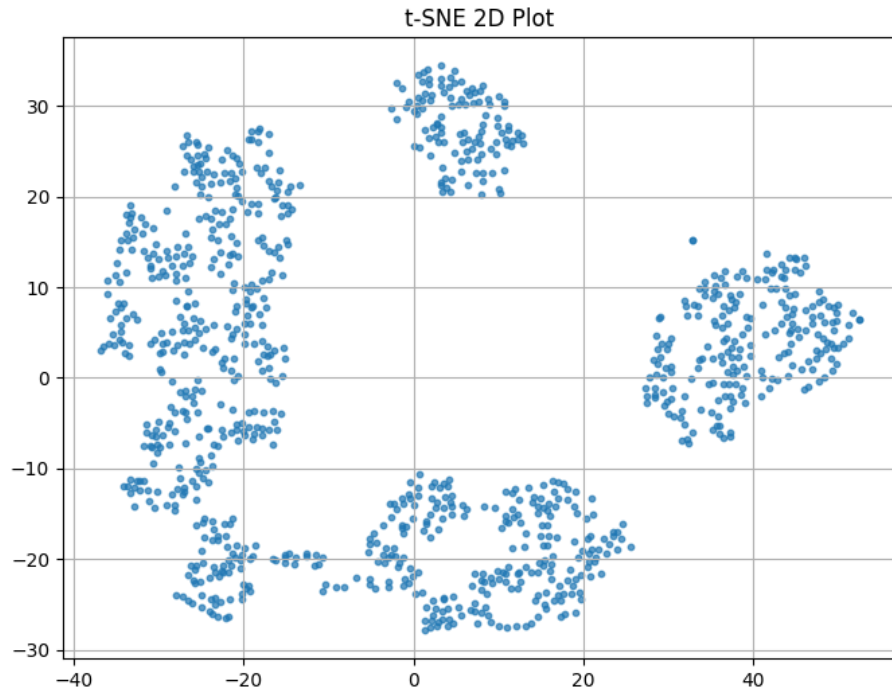
### 2.2 UMAP and t-SNE

Using library implementations, the original high-dimensional data was also visualized using UMAP and t-SNE.

- UMAP Plot:



- t-SNE Plot:



### 3. Expectation-Maximization (EM) Algorithm

After running the EM algorithm, the following parameters were estimated:

- Proportion of families with family planning ( $\pi$ ): 0.357
- Proportion of families without family planning ( $1-\pi$ ): 0.643
- Mean number of children in families with family planning ( $\lambda_1$ ): 1.785
- Mean number of children without family planning ( $\lambda_2$ ): 4.913