



TMSCA MIDDLE SCHOOL MATHEMATICS

TEST #9 ©

JANUARY 30, 2021

GENERAL DIRECTIONS

- About this test:
 - You will be given 40 minutes to take this test.
 - There are 50 problems on this test.
- All answers must be written on the answer sheet/Scantron form/Chatsworth card provided. If you are using an answer sheet be sure to use **BLOCK CAPITAL LETTERS**. Clean erasures are necessary for accurate grading on Scantrons and Chatsworth cards.
- If you are using a Chatsworth or Scantron card, please follow the specific instructions given at your particular meet.
- You may write anywhere on the test itself. You must write only answers on the answer sheet.
- You may use additional scratch paper provided by the contest director.
- All problems have **ONE** and **ONLY ONE** correct [BEST] answer. There is a penalty for all incorrect answers.
- Calculators **MAY NOT** be used on this test.
- All problems answered correctly are worth **FIVE** points. **TWO** points will be deducted for all problems answered incorrectly. No points will be added or subtracted for problems not answered.
- In case of ties, percent accuracy will be used as a tie breaker.

[illegible]

1. $\frac{3}{4} + \frac{7}{2} + \frac{3}{5} =$ _____

- A. $4\frac{17}{20}$ B. $4\frac{3}{4}$ C. $4\frac{11}{20}$ D. $4\frac{7}{20}$ E. $4\frac{7}{10}$

2. $9,442 - 1,718 =$ _____ (nearest hundred)

- A. 7,600 B. 7,800 C. 8,000 D. 7,900 E. 7,700

3. $992 \times 999 =$ _____

- A. 991,108 B. 991,080 C. 991,008 D. 991,118 E. 991,800

4. $428 \div \frac{2}{3} =$ _____

- A. 652 B. 676 C. 628 D. 662 E. 642

5. If $A = 237$, $B = 112$, and $C = 42$, then $A + B - C =$ _____ (Roman numeral)

- A. CCCXII B. CCCIX C. CCCVII D. CCXCVII E. CDVII

6. 3.7 hours = _____ minutes

- A. 262 B. 222 C. 234 D. 212 E. 266

7. 112 is 16% of what number?

- A. 710 B. 720 C. 700 D. 680 E. 780

8. Simplify: $(8 - w) - (4 - w)$

- A. $4 - w$ B. $4 + w$ C. $12 + w$ D. $4 + 2w$ E. 4

9. Evaluate $\frac{3}{4}a + \frac{1}{2}b - \frac{5}{6}c$ for $a = 36$, $b = -28$ and $c = 48$.

- A. -27 B. -18 C. 12 D. -9 E. -45

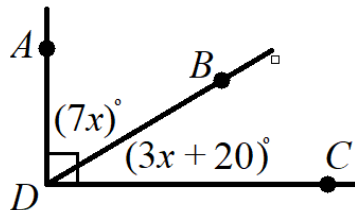
10. $\sqrt{3750}$ lies between which two integers?

- A. 58 and 59 B. 59 and 60 C. 60 and 61 D. 61 and 62 E. 62 and 63

11. How many numbers are there between 11 and 103, inclusive?

- A. 92 B. 91 C. 90 D. 93 E. 94

12. What is the measure of $\angle BDC$ in the picture below?



- A. 16° B. 32° C. 49° D. 68° E. 41°

13. $5^2 - 4^2 + 3^2 - 2^2 + 1^2 =$ _____

- A. 17 B. 15 C. 13 D. 11 E. 19

14. 3.5 quarts = _____ pints

- A. 14 B. 7 C. 28 D. 1.75 E. 17.5

15. What is the sum of all the reciprocals of the factors of 14?

- A. $\frac{5}{7}$ B. $1\frac{2}{7}$ C. $1\frac{5}{7}$ D. $1\frac{2}{5}$ E. $1\frac{5}{24}$

16. Express the ratio $\frac{1}{5}$ to 2 as a common fraction.

- A. $\frac{1}{2}$ B. $\frac{1}{4}$ C. $\frac{2}{5}$ D. $\frac{1}{25}$ E. $\frac{1}{10}$

17. It is exactly 10:55 am on a 12-hour clock. What time will it be in exactly 3 hours 22 minutes?

- A. 2:23 pm B. 2:13 pm C. 2:17 pm D. 2:27 pm E. 1:57 pm

18. What is the sum of the digits of the sum of $1,782 + 836 + 3,929$?

- A. 22 B. 21 C. 25 D. 23 E. 24

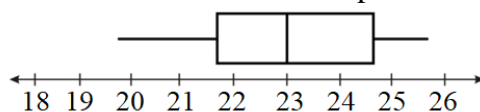
19. What is the probability of rolling a pair of dice and getting a sum of 10 facing up?

- A. $\frac{1}{6}$ B. $\frac{1}{18}$ C. $\frac{1}{9}$ D. $\frac{1}{12}$ E. $\frac{1}{4}$

20. The angles in a triangle are in a ratio of 2:4:9. What is the measure of the largest angle?

- A. 126° B. 128° C. 118° D. 106° E. 108°

21. What is twice the value of the median in the box and whisker plot?



- A. 49.5 B. 46 C. 43.6 D. 50 E. 44

22. Simplify: $19 + (-89) - 55 - (-36)$

- A. -89 B. -87 C. 17 D. -161 E. 51

23. What is the 16th term of the arithmetic sequence $-17, -9, -1, \dots$?

- A. 91 B. 97 C. 103 D. 105 E. 107

24. A human heart can beat $1\frac{1}{3}$ beats per second. How many beats can a human heart beat in one hour?

Answer in scientific notation.

- A. 8×10^1 B. 8×10^3 C. 4.8×10^6 D. 4.8×10^3 E. 1.92×10^3

25. An employee's salary increased by \$7,560, which represents an 18% raise. What is the employee's new salary?

- A. \$49,280 B. \$49,140 C. \$49,320 D. \$49,560 E. \$49,720

26. Merina walked by 12 equally spaced fence posts at her ranch. It took her 3 seconds to walk from the first post to the second, 4 seconds to walk from the second post to the third, and so on, with each time increasing by 1 second as she slowed down. How long did it take Merina to walk from the first post to the last?

- A. 1 min 18 sec B. 1 min 28 sec C. 1 min 32 sec D. 1 min 42 sec E. 1 min 39 sec

27. What value makes the equation $\frac{3}{4}(8x - 1) = \frac{3}{2}(4 - 2x)$ true?

- A. 0.75 B. 0.25 C. 0.5 D. 0.125 E. 0.375

28. 176 ft/sec = _____ mi/hr

- A. 150 B. 120 C. 90 D. 140 E. 135

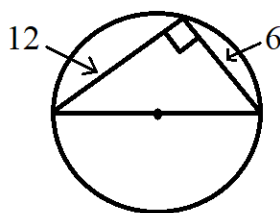
29. Point C is the midpoint of \overline{AB} , with A having coordinates $(18, 34)$ and B having coordinates $(-14, 24)$. If \overline{AB} is extended to point D with coordinates $(50, 44)$, what are the coordinates of the midpoint of \overline{CD} ?

- A. $(24, 33.5)$ B. $(34, 39)$ C. $(28, 34.5)$ D. $(34, 33.5)$ E. $(26, 36.5)$

30. $134_{14} =$ _____ (base 10)

- A. 236 B. 234 C. 232 D. 240 E. 242

31. What is the radius of the circle below?



- A. $3\sqrt{5}$ B. $8\sqrt{5}$ C. $4\sqrt{5}$ D. $6\sqrt{5}$ E. $2\sqrt{5}$

32. If $f(x) = 4x^2 - 7x$, then what is the value of $f(-3)$?

- A. 45 B. 15 C. 57 D. 148 E. -15

33. $9^{\frac{3}{2}} =$ _____

- A. 13.5 B. 81 C. 18 D. 27 E. $3^3\sqrt{3}$

34. What is the axis of symmetry for the graph of the quadratic equation $y = -2x^2 + 4 - 8x$?

- A. $x = -2$ B. $x = -1$ C. $x = 1$ D. $x = \frac{1}{2}$ E. $x = -\frac{1}{2}$

35. Line A passes through the points $(14, 16)$ and $(2, 8)$. Line B passes through the points $(5, 11)$ and $(x, 3)$. If lines A and B are parallel, what is the value of x ?

- A. 9 B. -3 C. 13 D. -9 E. -7

36. Find the value of $8 \otimes -5$, if $x \otimes y = \frac{1}{x} - \frac{2}{y}$.

- A. 0.475 B. 0.525 C. 0.575 D. 0.450 E. 0.625

37. A regular polygon has an exterior angle measure of 72° . How many sides does the polygon have?

- A. 6 B. 8 C. 7 D. 12 E. 5

38. How many permutations can be made from seven objects taken four at a time?

- A. 840 B. 35 C. 70 D. 910 E. 210

39. If 3 widgets are equal to 7 betas and 1 beta is equal to 8 cons, how many widgets are equal to 112 cons?

- A. 14 B. 12 C. 4 D. 6 E. 8

40. On a number line, the distance from point A to point B is 37 units. Point A has the coordinate of -14 . What is the sum of all possible value of B ?

- A. 51 B. 23 C. -28 D. -23 E. -16

41. The geometric mean of a and b is $8\sqrt{3}$. If $a = 8$, what is the value of b ?

- A. $\sqrt{3}$ B. 24 C. $16\sqrt{3} - 8$ D. 32 E. 48

42. If $\begin{bmatrix} -9 & 7 \\ -1 & 4 \end{bmatrix} \cdot \begin{bmatrix} 6 & -3 \\ 10 & 2 \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$, then what is the value of $(c + d) - (a + b)$?

- A. 34 B. -12 C. -2 D. 73 E. -52

43. What is the area of a triangle with vertices located at $(-5, 5)$, $(5, -4)$, and $(-8, -2)$?

- A. 51.5 units^2 B. 49.5 units^2 C. 50.5 units^2 D. 47.5 units^2 E. 48.5 units^2

44. $131_4 \times 20_4 = \underline{\hspace{2cm}}$ (base 10)

- A. 151 B. 143 C. 142 D. 164 E. 232

45. The two points $(12, -4)$ and $(6, -10)$ lie on the same line. Which of the following points also lies on the same line?

- A. $(-7, -23)$ B. $(-6, -24)$ C. $(20, 6)$ D. $(22, 8)$ E. $(31, 17)$

46. What is the decay rate of the exponential decay function $y = 1.6 \left(\frac{4}{5}\right)^x$?

- A. 60% B. 80% C. 20% D. 40% E. 10%

47. A square and a regular heptagon each have the same side length. If the perimeter of the heptagon is 84 units, what is the measure of the diagonal of the square?

- A. 14 units B. $14\sqrt{2}$ units C. $16\sqrt{2}$ units D. 12 units E. $12\sqrt{2}$ units

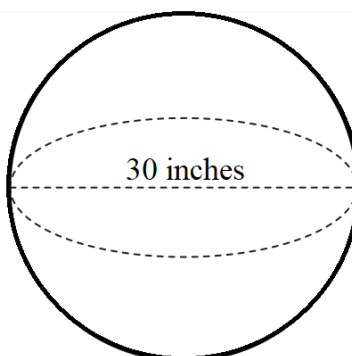
48. Rewrite $\log_4 256 = 4$ in exponential form.

- A. $4^4 = 256$ B. $4(4) = 256$ C. $2^2 = 256$ D. $4(4)^4 = 256$ E. $2(4)^2 = 256$

49. You would multiply $\frac{3}{4+\sqrt{3}}$ by which of the following to rationalize the denominator?

- A. $\frac{3\sqrt{3}}{3\sqrt{3}}$ B. $\frac{\sqrt{3}}{\sqrt{3}}$ C. $\frac{4+\sqrt{3}}{4+\sqrt{3}}$ D. $\frac{4-\sqrt{3}}{4-\sqrt{3}}$ E. $\frac{4+\sqrt{3}}{4-\sqrt{3}}$

50. If $\pi = 3$, what is the volume of the sphere below?



- A. $13,500 \text{ in}^3$ B. $2,700 \text{ in}^3$ C. $1,200 \text{ in}^3$ D. $36,000 \text{ in}^3$ E. 900 in^3

2020 – 2021 TMSCA Middle School Mathematics Test #9 Answer Key

1. A	18. A	35. E
2. E	19. D	36. B
3. C	20. E	37. E
4. E	21. B	38. A
5. C	22. A	39. D
6. B	23. C	40. C
7. C	24. D	41. B
8. E	25. D	42. B
9. A	26. B	43. E
10. D	27. A	44. E
11. D	28. B	45. A
12. E	29. E	46. C
13. B	30. E	47. E
14. B	31. A	48. A
15. C	32. C	49. D
16. E	33. D	50. A
17. C	34. A	

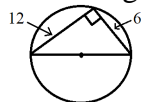
13. The alternating sum of n^2 numbers is equal to $n^2 - (n - 1)^2 + \cdots + 3^2 - 2^2 + 1^2 = 1 + 2 + 3 + \cdots + n$. Therefore, $5^2 - 4^2 + 3^2 - 2^2 + 1^2 = 1 + 2 + 3 + 4 + 5 = 15$.

22. $19 + (-89) - 55 - (-36) = 19 - 89 - 55 + 36 = -70 - 55 + 36 = -125 + 36 = -89$.

23. The formula to find the n^{th} term of an arithmetic sequence is $a_n = a_1 + (n - 1)(d)$, with $a_1 = 1^{\text{st}}$ term, n is the term we are trying to find and d is the common difference. We are given the arithmetic sequence $-17, -9, -1, \dots$, so the 16^{th} term is equal to $a_{16} = (-17) + (16 - 1)(8) = 103$.

26. From the 1^{st} fence post to the 12^{th} , there are 11 gaps, so the time is $3 + 4 + 5 + 6 + 7 + 8 + 9 + 10 + 11 + 12 + 13 = 88$ seconds. Since 60 seconds = 1 minute, 88 seconds = 1 minute 28 seconds.

31. If a right triangle is drawn inside a circle, its hypotenuse is equal to the diameter of the circle.



In the picture given, using the Pythagorean Theorem, the hypotenuse is equal to $\sqrt{12^2 + 6^2} = \sqrt{180} = 6\sqrt{5}$. The radius is half the diameter, so the radius is equal to $(\frac{1}{2})(6\sqrt{5}) = 3\sqrt{5}$.

33. Because $a^{\frac{m}{n}} = \sqrt[n]{a^m}$ or $(\sqrt[n]{a})^m$, then $9^{\frac{3}{2}} = (\sqrt[2]{9})^3 = 3^3 = 27$.

40. If point A has the coordinate of -14 , the point B could be located in the positive direction or negative direction of point A . If B is in the positive direction, then $B = -14 + 37 = 23$. If B is in the negative direction, then $B = -14 - 37 = -51$. Therefore, the sum of all possible values of B is $-51 + 23 = -28$.

41. The geometric mean of a and b is equal to \sqrt{ab} . Since $a = 8$, and the geometric mean of a and b is equal to $8\sqrt{3} = \sqrt{64 \cdot 3} = \sqrt{192}$, then b is equal to $192 \div 8 = 24$.

47. A heptagon has 7 sides, so if the perimeter is 84 units, then the side length is $84 \div 7 = 12$ units. The side length of the heptagon and square are each 12 units. The diagonal of a square is equal to $s\sqrt{2}$ units, with s equal to the side length of the square. If the side length of the square is 12 units, then its diagonal is $12\sqrt{2}$ units.

48. Since $\log_x Z = y$ can be rewritten as $x^y = Z$, then $\log_4 256 = 4$ can be rewritten as $4^4 = 256$.

49. To rationalize the denominator of $\frac{3}{4+\sqrt{3}}$, you would multiply the fraction by 1, but that contains the conjugate of the denominator. The denominator is $4 + \sqrt{3}$, so the conjugate is $4 - \sqrt{3}$. Therefore, the fraction needed to multiply $\frac{3}{4+\sqrt{3}}$ with to rationalize the denominator is $\frac{4-\sqrt{3}}{4-\sqrt{3}}$.

50. The diameter of the sphere is 30 inches, so the radius is one-half of the diameter, or $\frac{1}{2}(30) = 15$ inches. The formula for volume of a sphere is $V = \frac{4}{3}\pi r^3$. Since $r = 15$ and $\pi = 3$, the volume of the sphere is $V = \frac{4}{3} \cdot 3 \cdot 15^3 = 4 \cdot 3,375 = 13,500 \text{ in}^3$.