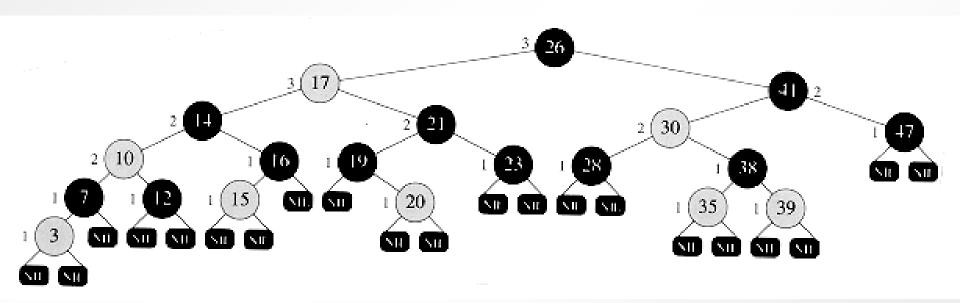
Red-black tree



Cormen

5/16/2022

Red-Black tree

- A red-black tree is a binary search tree which satisfies:
- 1. Every node is either red or black.
- 2. The root is black
- 3. Every leaf (NIL) is black.
- 4. If a node is red, then both its children are black.
- 5. Every path from a node to a descendant leaf contains the same number of black nodes.

Red-Black tree

- black-height of a node x: bh(x)
 the number of black nodes on any path from x to a leaf node
- black-height of a red-black tree: the black-height of its root.

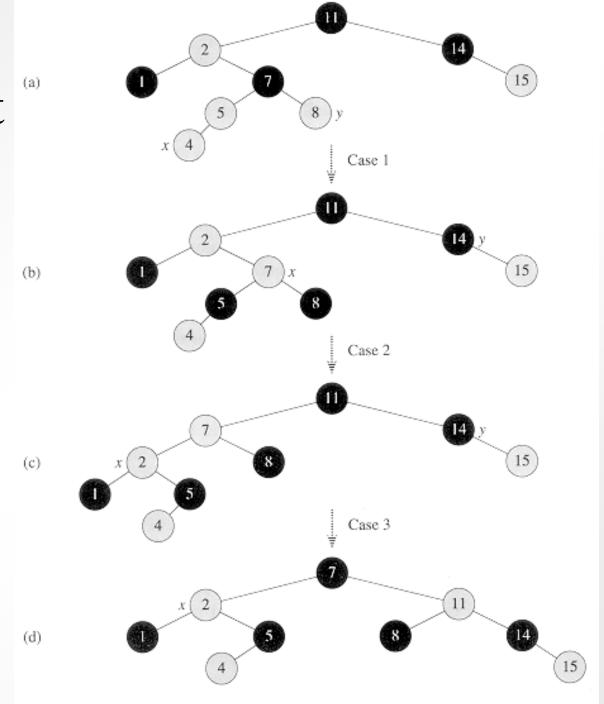
Lemma

A red-black tree with n internal nodes has height at most $2*log_2(n+1)$.

Red-black tree: operation insert

- insert in BSTree
- the new node is red
- if the parent of the new node is red fix the tree!!

Red-black tree: operation insert



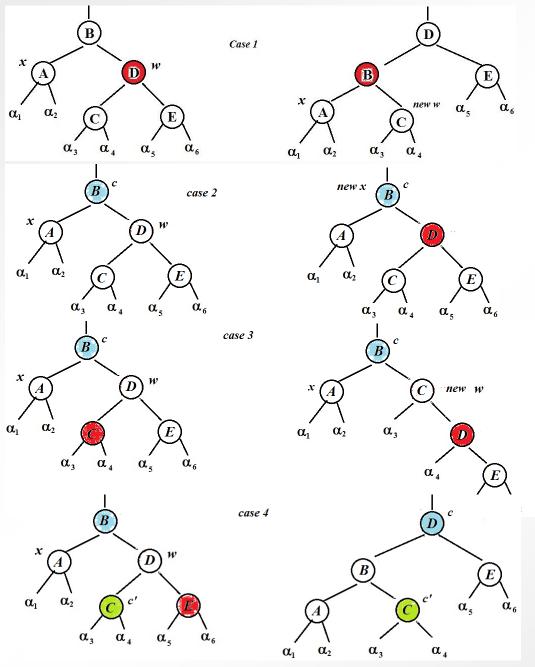
Cormen

Red-black tree: operation delete

Delete as in BSTree

If a discrepancy arises for the red-black tree, fix it!

- If the deleted node is red the tree is still a red-black tree
- If the deleted node is black:
 - if its child is red, repaint the child to black.
 - otherwise: fix the tree !!mark the child as double black: x (and fix the problem!)



5/16/2022