

FEDERAL STATE AUTONOMOUS EDUCATIONAL INSTITUTION
OF HIGHER EDUCATION
ITMO UNIVERSITY

Report on learning practice # 4
Stationarity of the processes

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Substantiation of chosen sampling

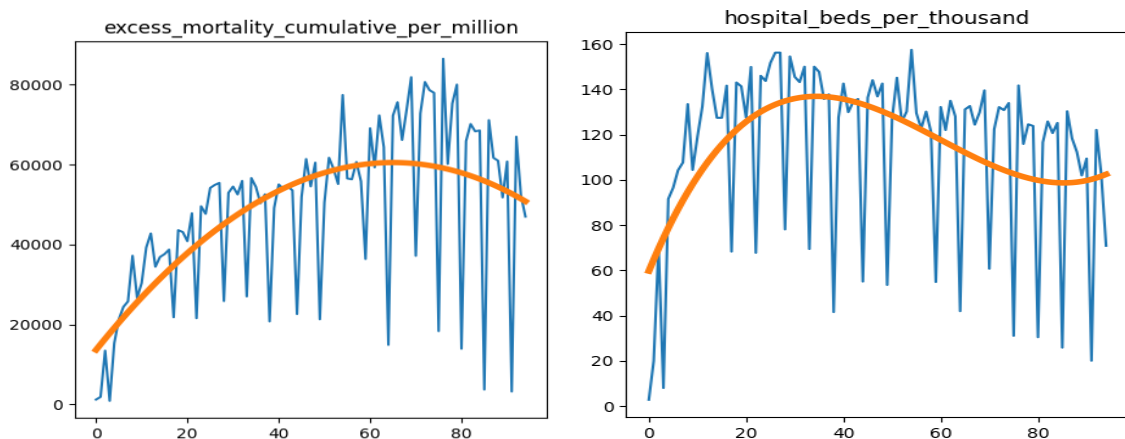
For this lab have chosen 5 variables for the analysis, 3 of them serve as predictors, and 2 - as target variables:

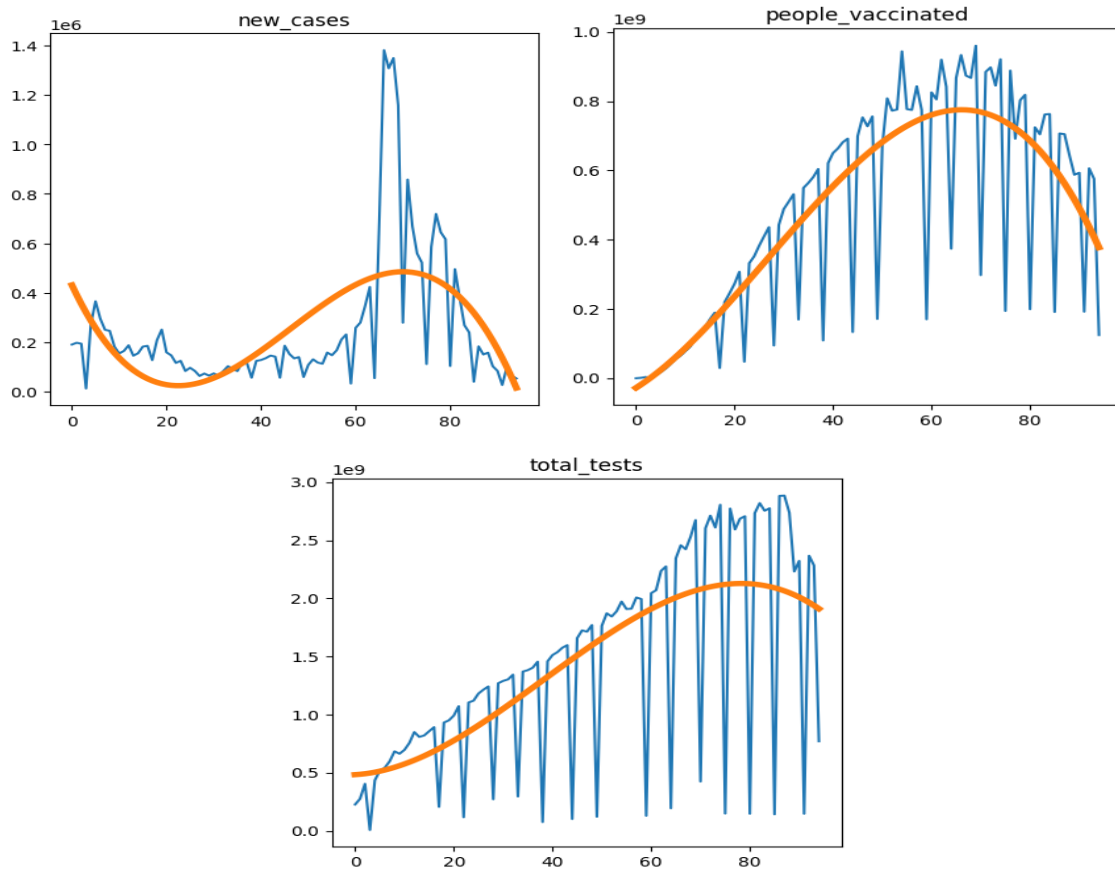
- Predictors:
 - **hospital_beds_per_thousand** - Share of the population with basic hand washing facilities on premises, most recent year available
 - **people_vaccinated** - Total number of people who received at least one vaccine dose
 - **total_tests** - New tests for COVID-19 (only calculated for consecutive days)
- Target variables:
 - **excess_mortality_cumulative_per_million** - Cumulative difference between the reported number of deaths since 1 January 2020 and the projected number of deaths for the same period based on previous years, per million people
 - **new_cases** - New confirmed cases of COVID-19

We believe that such factors as the number of tests and vaccinated people along with hospital beds are associated with the number of new cases as well as with the excess mortality

Stationary analysis

We analyzed stationarity of a process (for mathematical expectation and variance) for all chosen variables. Trend lines for each variable are presented at the graphs below





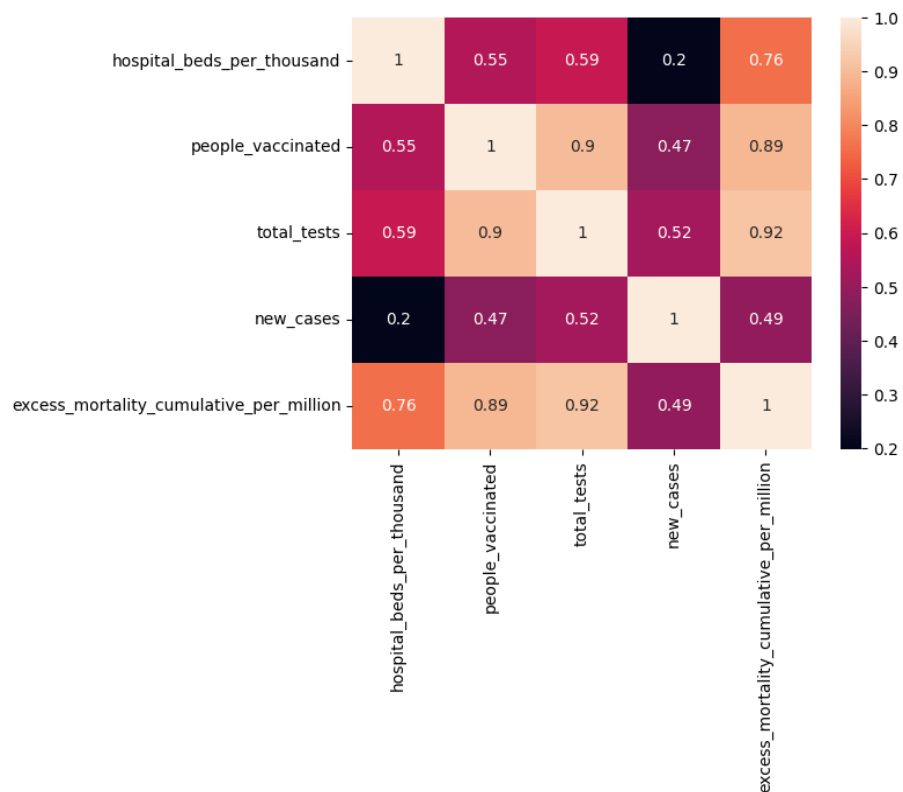
Statistical estimators as mean, standard deviation and variance for each variable are seen at the presented table:

Variable	Mean	Standard Deviation	Variance
excess_mortality_cumulative_per_million	48 444.53	20 996.3	440 844 461.65
hospital_beds_per_thousand	114.04	38.08	1450.06
new_cases	251 353.53	279 872.12	78 328 401 640.89
people_vaccinated	487 096 471.04	312 558 553.72	9.769284950126229e+16
total_tests	1 442 451 407.62	897 663 785.67	8.058002721014452e+17

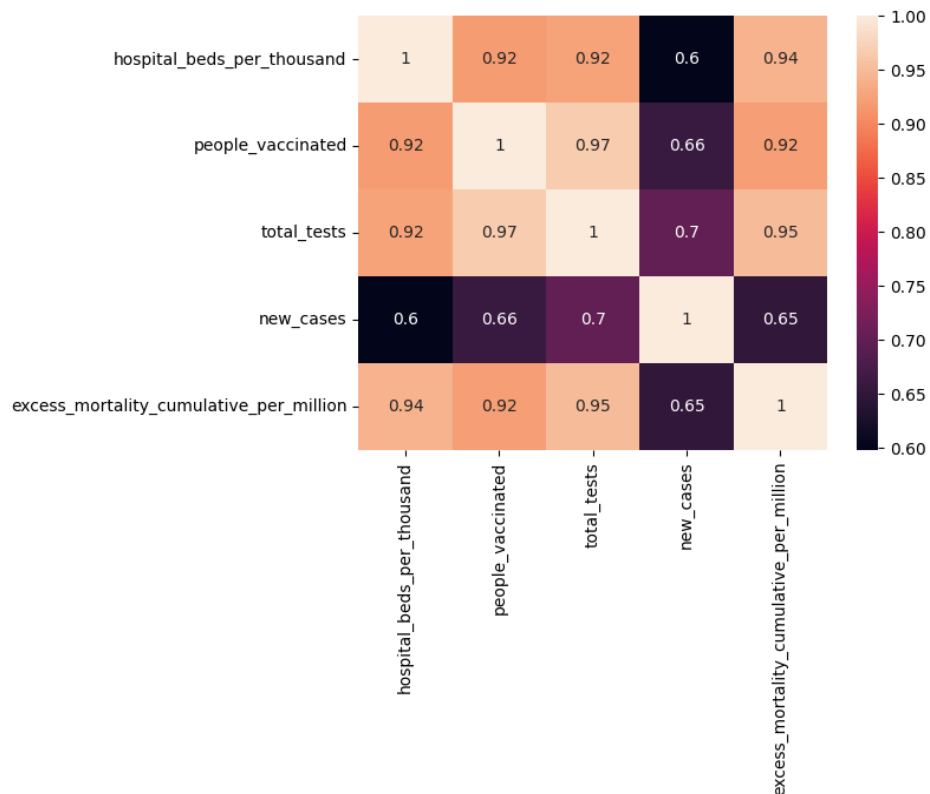
Covariance or correlation function analysis

We examined the correlation between chosen variables - all of them have statistically significant correlation with $p\text{-value} < 0.05$, the correlation coefficients are all positive and are ranged between 0.2 and 0.92

The lowest correlation (0.2) is between hospital_beds_per_thousand and new_cases and the highest (0.92) is between excess_mortality_cumulative_per_million and total_tests

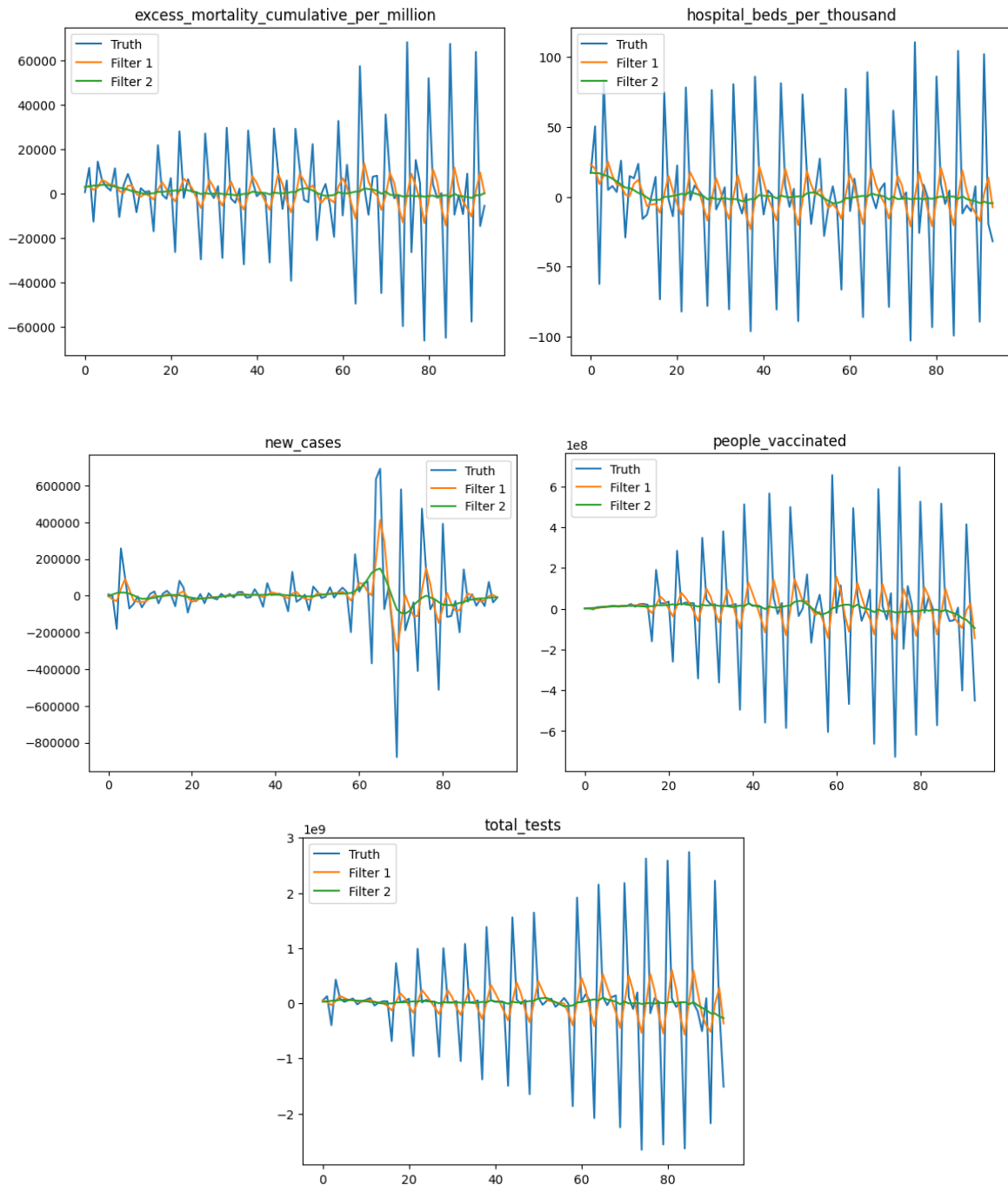


We also examined the correlation between variables on trendless data - all coefficients remained positive, but the range changed to 0.6 (hospital_beds_per_thousand and new_cases) to 0.97 (people_vaccinated and total_tests)



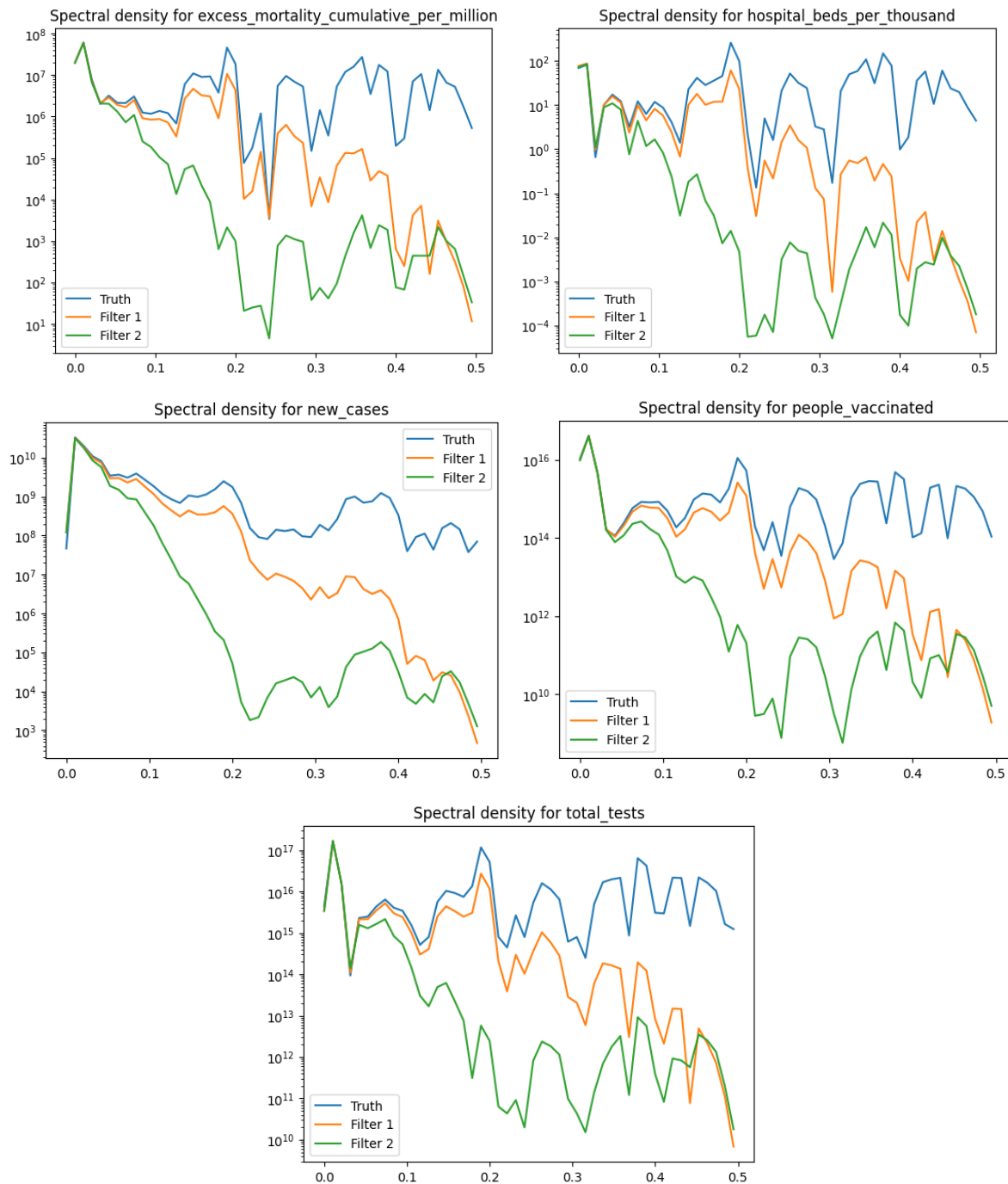
Noise filtration

We performed 2 filter types for our target variables with windows of 12 and 24 - the resulting distributions are shown on the following graphs



Estimation of spectral density function

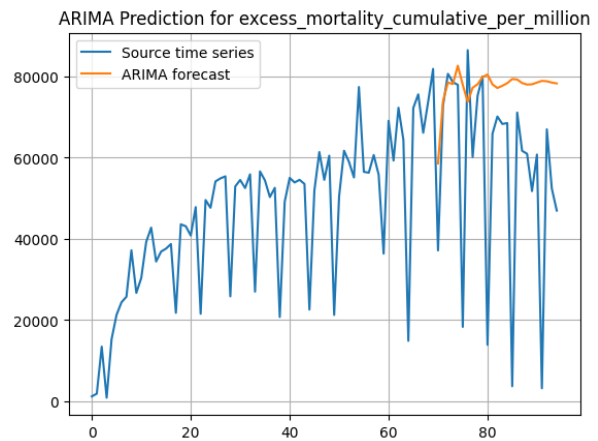
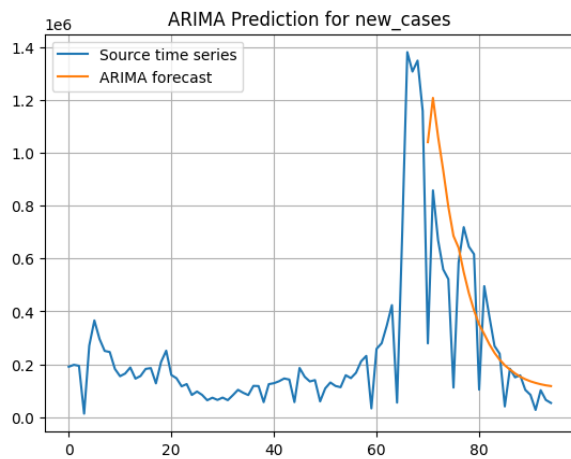
At the next step, we estimated the power spectral density of each variable, graphs of which one can see below. As it is shown in the graphs, after filtering, curves are located under the “Truth” curve, and generally Filter 2 is located below other curves



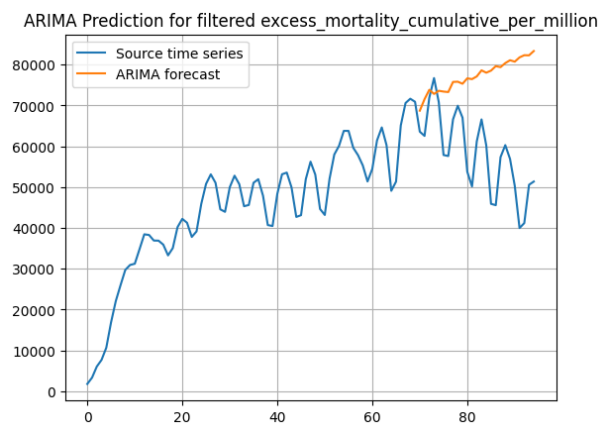
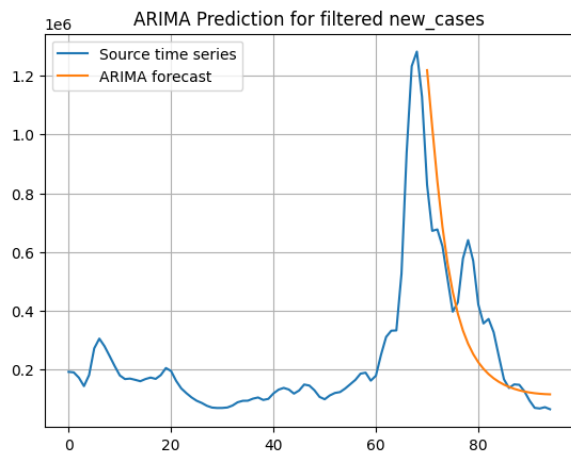
Auto-regression model

At this point, we built auto-regression model for filtered and non-filtered data. We used the ARIMA model to predict values of target variables. Obtained graphs are presented below. And as one can see from the graph the model presented quite good results for new_cases target variable, though for excess_mortality it resulted in less accurate prediction

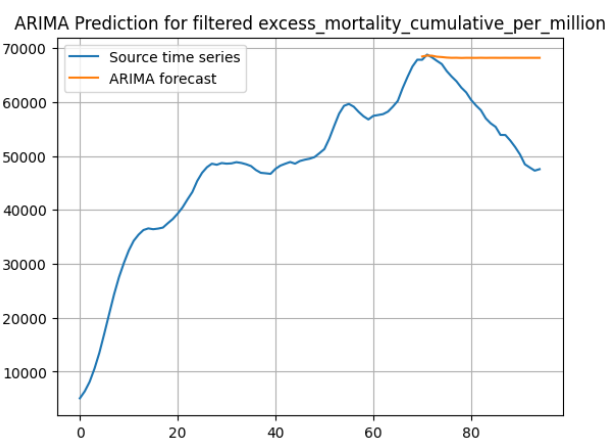
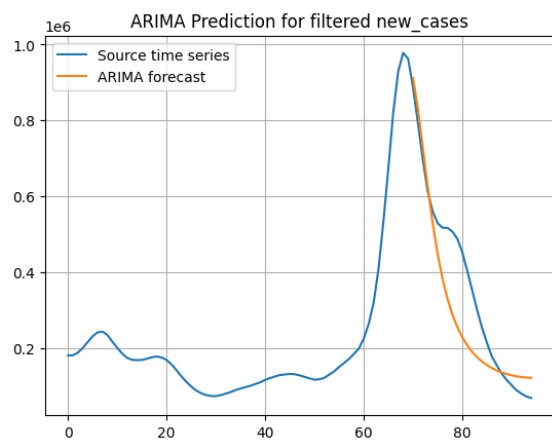
Original Data



Filter 1



Filter 2



Data Type	Target Variable	R^2	MSE	MAPE
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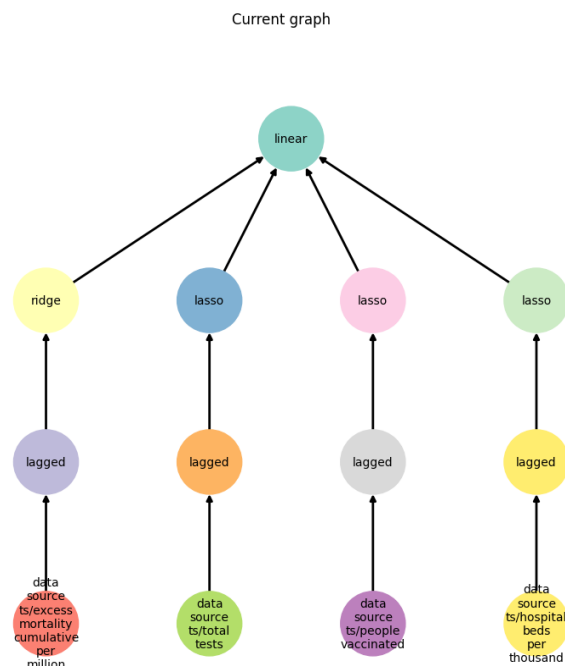
Original	new_cases	-0.044	66 430 885 780.92	100.806
	excess_mortality_cumulative_per_million	-0.737	969 402 201.428	227.517
Filter 1	new_cases	0.444	29 749 016 070.555	35.95
	excess_mortality_cumulative_per_million	-4.585	513 373 873.045	37.659
Filter 2	new_cases	0.774	12 747 671 177.288	29.681
	excess_mortality_cumulative_per_million	-1.919	147 657 374.35	18.783

Model in a form of linear dynamical system

We created two models in a form of linear dynamical systems for both of our target variables - Excess Mortality and New Cases. For both models we used all three of our chosen predictors

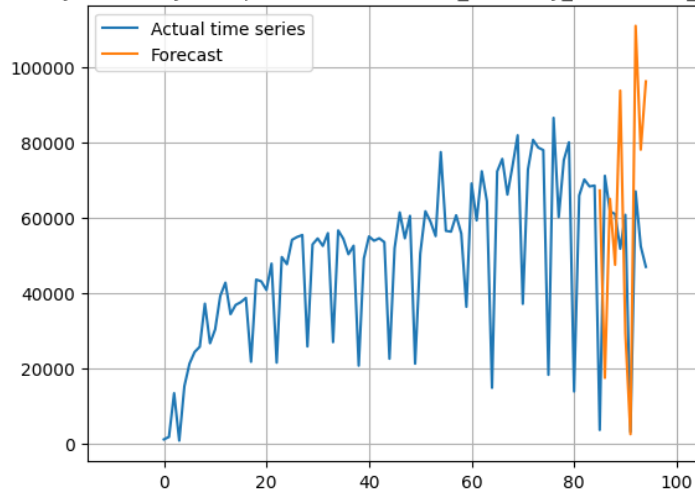
Excess Mortality

The pipeline of the linear dynamical system looks like that with three predictors for the target variable:



The forecast shows reasonable results as the correlation between predictors and the target variable is high, though the model did not catch the decreasing trend of the last observations

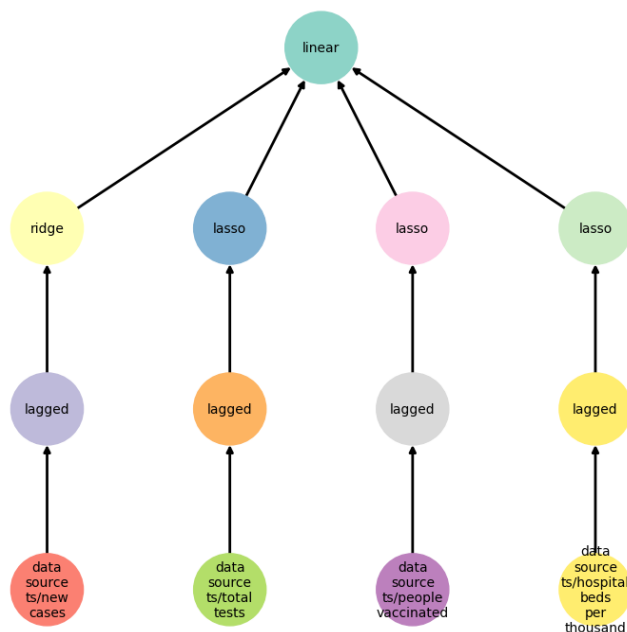
Linear dynamical system prediction for excess_mortality_cumulative_per_million



New Cases

Next, we trained the prediction model for another target variable - new_cases - with the same set of predictors. Just like in the latter case we built the following pipeline

Current graph



And as one can see from the obtained graph below the quality of the prediction model is extremely low because of the weaker correlation between the target variable and predictors compared to the case where we predicted excess mortality

