

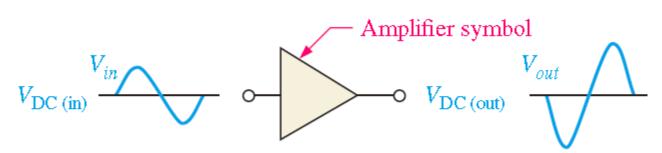
Xuewei Pan, PhD, Associate Professor

## **CHAPTER 5** Transistors Bias Circuits

- **5.1** The DC Operating Point
- **5.2 Voltage-Divider Bias**
- **5.3 Other Bias Methods**

## 5.1 The DC Operation Point DC Bias

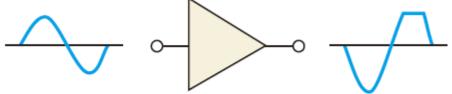
• Bias establishes the dc operating point (Q-point) for proper linear operation of an amplifier. If an amplifier is not biased with correct dc voltages on the input and output, it can go into saturation or cutoff when an input signal is applied. Figure 5–1 shows the effects of proper and improper dc biasing of an inverting



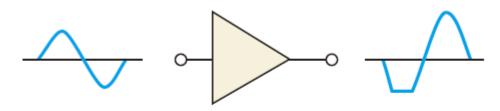
(a) Linear operation: larger output has same shape as input except that it is inverted

#### FIGURE 5-1

Examples of linear and nonlinear operation of an inverting amplifier (the triangle symbol).

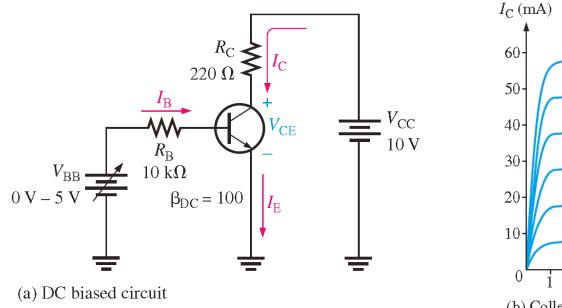


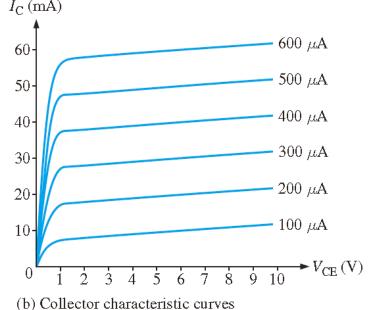
(b) Nonlinear operation: output voltage limited (clipped) by cutoff



(c) Nonlinear operation: output voltage limited (clipped) by saturation

• The transistor in Figure 5–2(a) is biased with  $V_{\rm CC}$  and  $V_{\rm BB}$  to obtain certain values of  $I_{\rm B}$ ,  $I_{\rm C}$ ,  $I_{\rm E}$ , and  $V_{\rm CE}$ . The collector characteristic curves for this particular transistor are shown in Figure 5–2(b); we will use these curves to graphically illustrate the effects of dc bias.





#### FIGURE 5-2

A dc-biased transistor circuit with variable bias voltage ( $V_{\rm BB}$ ) for generating the collector characteristic curves shown in part (b).

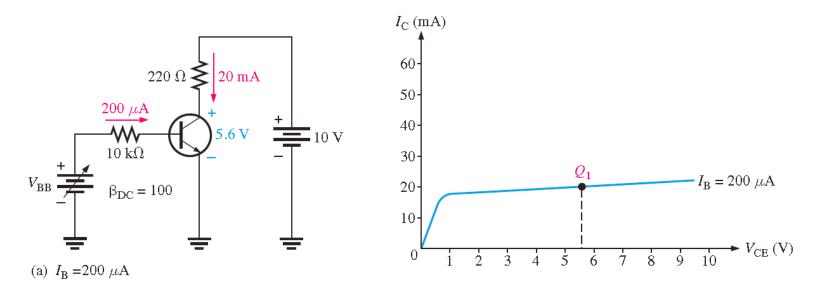


FIGURE 5-3 Illustration of Q-point adjustment.

In Figure 5–3, we assign three values to  $I_{\rm B}$  and observe what happens to  $I_{\rm C}$  and  $V_{\rm CE}$ . First,  $V_{\rm BB}$  is adjusted to produce an  $I_{\rm B}$  of 200  $\mu$ A, as shown in Figure 5–3(a). Since  $I_{\rm C} = \beta_{\rm DC} I_{\rm B}$ , the collector current is 20 mA, as indicated, and

$$V_{\rm CE} = V_{\rm CC} - I_{\rm C}R_{\rm C} = 10 \text{ V} - (20 \text{ mA})(220 \Omega) = 10 \text{ V} - 4.4 \text{ V} = 5.6 \text{ V}$$

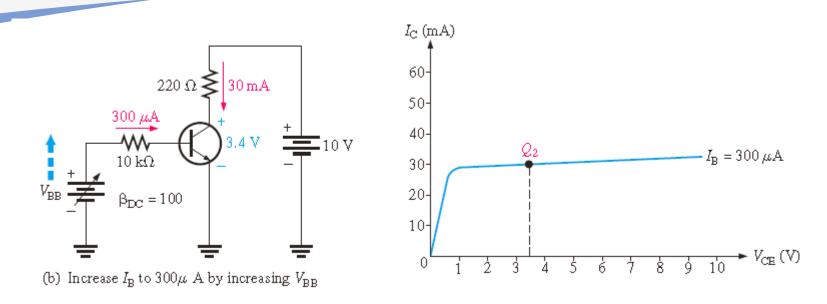


FIGURE 5-3 Illustration of Q-point adjustment.

Next, as shown in Figure 5–3(b),  $V_{\rm BB}$  is increased to produce an  $I_{\rm B}$  of 300  $\mu{\rm A}$  and an  $I_{\rm C}$  of 30 mA.

$$V_{\rm CE} = 10 \text{ V} - (30 \text{ mA})(220 \Omega) = 10 \text{ V} - 6.6 \text{ V} = 3.4 \text{ V}$$

The Q-point for this condition is indicated by  $Q_2$  on the graph.

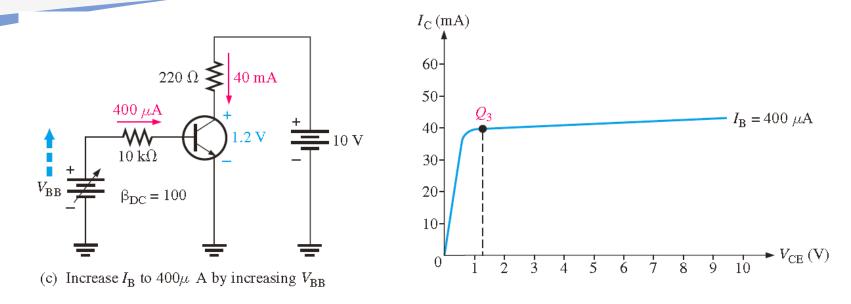


FIGURE 5-3 Illustration of Q-point adjustment.

Finally, as in Figure 5–3(c),  $V_{\rm BB}$  is increased to give an  $I_{\rm B}$  of 400  $\mu{\rm A}$  and an  $I_{\rm C}$  of 40 mA.

$$V_{\rm CE} = 10 \text{ V} - (40 \text{ mA})(220 \Omega) = 10 \text{ V} - 8.8 \text{ V} = 1.2 \text{ V}$$

 $Q_3$  is the corresponding Q-point on the graph.

### **DC Load Line**

• The dc operation of a transistor circuit can be described graphically using a dc load line. This is a straight line drawn on the characteristic curves from the saturation value where  $I_{\rm C} = I_{\rm C(sat)}$  on the y-axis to the cutoff value where  $V_{\rm CE} = V_{\rm CC}$  on the x-axis, as shown in Figure 5–4(a).

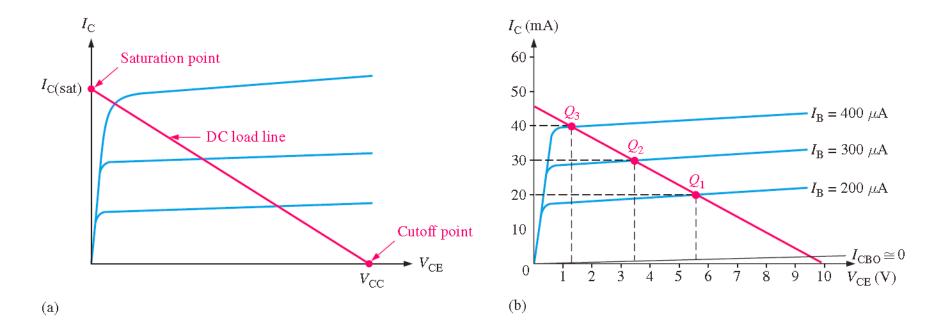
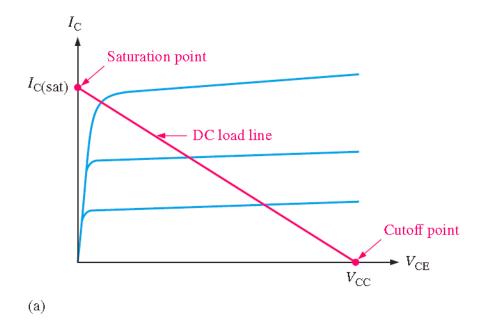


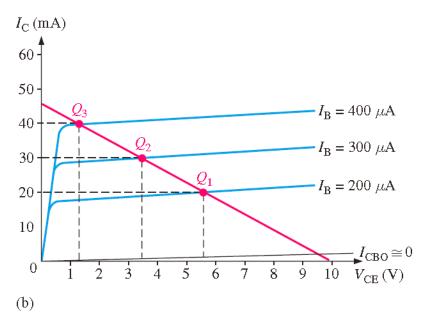
FIGURE 5-4 The dc load line.

### **DC Load Line**

• The equation for  $I_{\rm C}$  is  $I_{\rm C} = \frac{V_{\rm CC} - V_{\rm CE}}{R_{\rm C}} = \frac{V_{\rm CC}}{R_{\rm C}} - \frac{V_{\rm CE}}{R_{\rm C}} = -\frac{V_{\rm CE}}{R_{\rm C}} + \frac{V_{\rm CC}}{R_{\rm C}} = -\left(\frac{1}{R_{\rm C}}\right)V_{\rm CE} + \frac{V_{\rm CC}}{R_{\rm C}}$ 

This is the equation of a straight line with a slope of  $-1/R_{\rm C}$ , an x intercept of  $V_{\rm CE} = V_{\rm CC}$ , and a y intercept of  $V_{\rm CC}/R_{\rm C}$ , which is  $I_{\rm C(sat)}$ .





## **Linear Operation**

• The region along the load line including all points between saturation and cutoff is generally known as the linear region of the transistor's operation. As long as the transistor is operated in this region, the output voltage is a linear reproduction of the input.

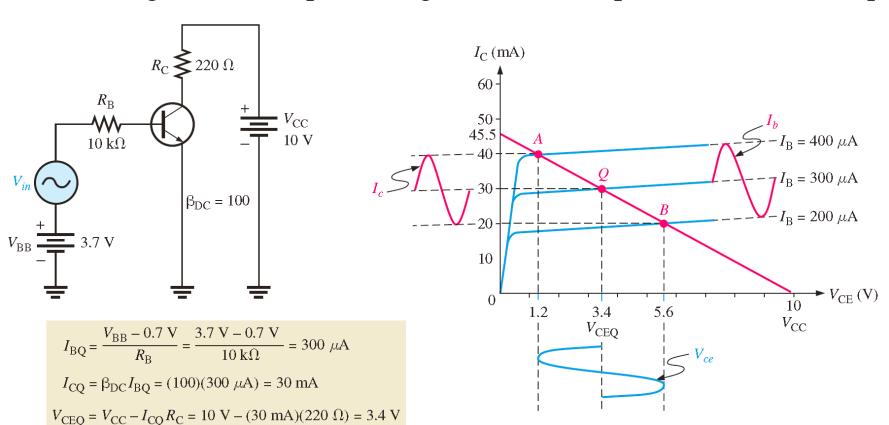
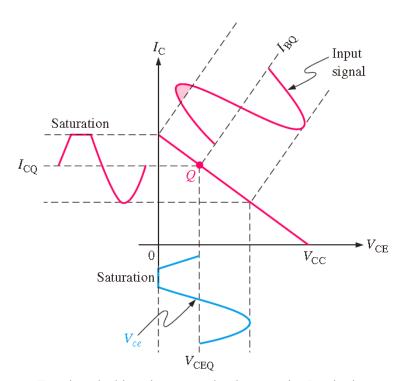


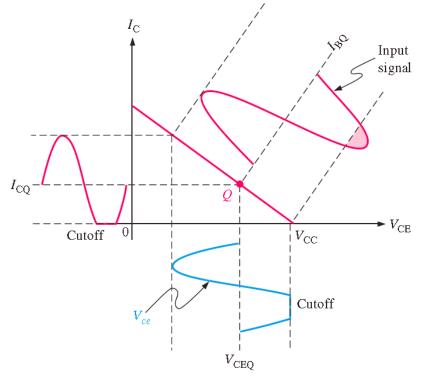
FIGURE 5-5 Variations in collector current and collector-to-emitter voltage as a result of a variation in base current.

## **Waveform Distortion**

• As previously mentioned, under certain input signal conditions the location of the Q-point on the load line can cause one peak of the  $V_{\rm ce}$  waveform to be limited or clipped, as shown in parts (a) and (b) of Figure 5–6.



(a) Transistor is driven into saturation because the Q-point is too close to saturation for the given input signal.



(b) Transistor is driven into cutoff because the Q-point is too close to cutoff for the given input signal.

## 5-2 Voltage-divider Bias

- A more practical bias method is to use  $V_{\rm CC}$  as the single bias source, as shown in Figure 5–9. To simplify the schematic, the battery symbol is omitted and replaced by a line termination circle with a voltage indicator  $(V_{\rm CC})$  as shown.
- A dc bias voltage at the base of the transistor can be developed by a resistive voltage divider that consists of  $R_1$  and  $R_2$ , as shown in Figure 5–9.  $V_{CC}$  is the dc collector supply voltage. Two current paths are between point A and ground: one through  $R_2$  and the other through the base-emitter junction of the transistor and  $R_E$ .

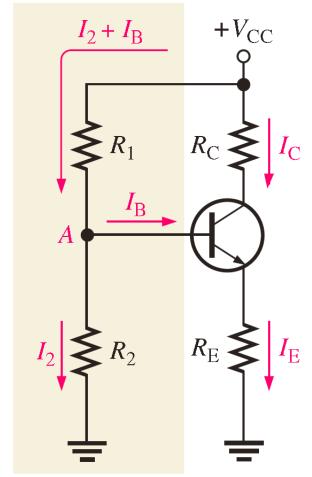


FIGURE 5-9 Voltage-divider bias.

## Voltage-divider Bias

• A voltage divider in which the base current is small compared to the current in  $R_2$  is said to be a stiff voltage divider because the base voltage is relatively independent of different transistors and temperature effects.

$$V_{\rm B} \simeq \left(\frac{R_2}{R_1 + R_2}\right) V_{\rm CC}$$
  $V_{\rm E} = V_{\rm B} - V_{\rm BE}$ 

$$I_{\rm C} \cong I_{\rm E} = \frac{V_{\rm E}}{R_{\rm E}}$$
  $V_{\rm C} = V_{\rm CC} - I_{\rm C}R_{\rm C}$ 

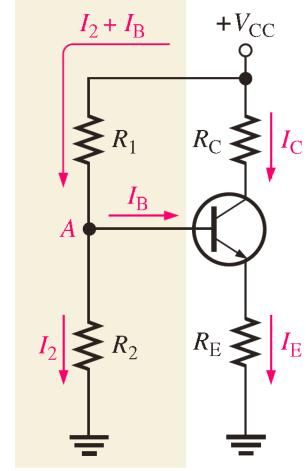
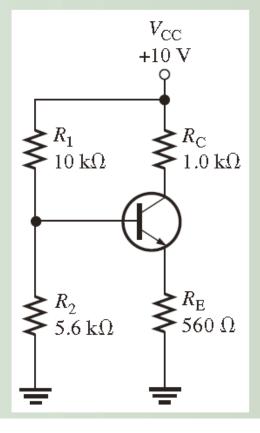


FIGURE 5-9 Voltage-divider bias.

#### EXAMPLE 5-2

Determine  $V_{\text{CE}}$  and  $I_{\text{C}}$  in the stiff voltage-divider biased transistor circuit of Figure 5–10 if  $\beta_{\text{DC}} = 100$ .

► FIGURE 5–10



### **Solution** The base voltage is

$$V_{\rm B} \simeq \left(\frac{R_2}{R_1 + R_2}\right) V_{\rm CC} = \left(\frac{5.6 \text{ k}\Omega}{15.6 \text{ k}\Omega}\right) 10 \text{ V} = 3.59 \text{ V}$$

So,

$$V_{\rm E} = V_{\rm B} - V_{\rm BE} = 3.59 \text{ V} - 0.7 \text{ V} = 2.89 \text{ V}$$

and

$$I_{\rm E} = \frac{V_{\rm E}}{R_{\rm E}} = \frac{2.89 \text{ V}}{560 \Omega} = 5.16 \text{ mA}$$

Therefore,

$$I_{\rm C} \cong I_{\rm E} = 5.16 \,\mathrm{mA}$$

and

$$V_{\rm C} = V_{\rm CC} - I_{\rm C}R_{\rm C} = 10 \text{ V} - (5.16 \text{ mA})(1.0 \text{ k}\Omega) = 4.84 \text{ V}$$
  
 $V_{\rm CE} = V_{\rm C} - V_{\rm E} = 4.84 \text{ V} - 2.89 \text{ V} = 1.95 \text{ V}$ 

## 5-3 Other Bias Methods

### **Emitter Bias**

• Emitter bias provides excellent bias stability in spite of changes in  $\beta$  or temperature. It uses both a positive and a negative supply voltage.

$$V_{\rm EE} + V_{R_{\rm B}} + V_{\rm BE} + V_{R_{\rm E}} = 0$$

Substituting, using Ohm's law,

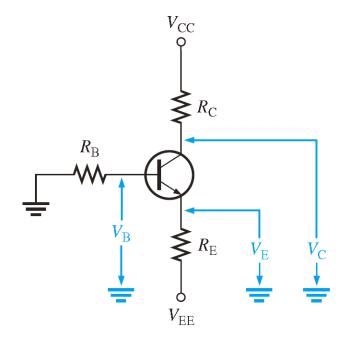
$$V_{\rm EE} + I_{\rm B}R_{\rm B} + V_{\rm BE} + I_{\rm E}R_{\rm E} = 0$$

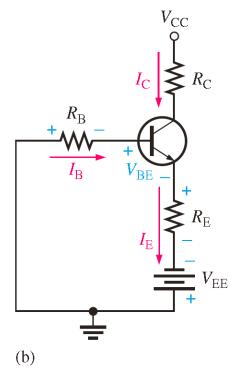
Substituting for  $I_{\rm B} \cong I_{\rm E}/\beta_{\rm DC}$  and transposing  $V_{\rm EE}$ ,

$$\left(\frac{I_{\rm E}}{\beta_{\rm DC}}\right)R_{\rm B} + I_{\rm E}R_{\rm E} + V_{\rm BE} = -V_{\rm EE}$$

Factoring out  $I_{\rm E}$  and solving for  $I_{\rm E}$ ,

$$I_{\rm E} = \frac{-V_{\rm EE} - V_{\rm BE}}{R_{\rm E} + R_{\rm B}/\beta_{\rm DC}}$$





(a)

#### **FIGURE 5-11**

An npn transistor with emitter bias. Voltages with respect to ground are indicated with a single subscript.

16

## **Emitter Bias**

Voltages with respect to ground are indicated by a single subscript. The emitter voltage with respect to ground is

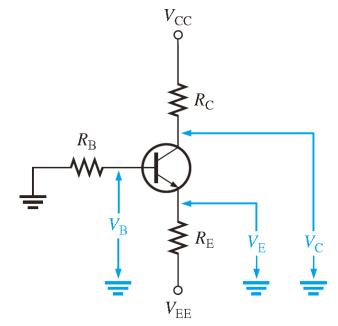
$$V_{\rm E} = V_{\rm EE} + I_{\rm E}R_{\rm E}$$

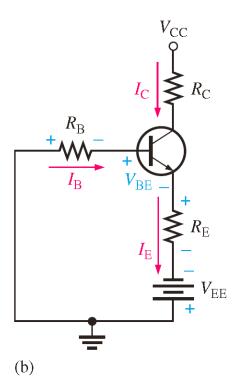
The base voltage with respect to ground is

$$V_{\rm B} = V_{\rm E} + V_{\rm BE}$$

The collector voltage with respect to ground is

$$V_{\rm C} = V_{\rm CC} - I_{\rm C} R_{\rm C}$$





#### **FIGURE 5-11**

(a)

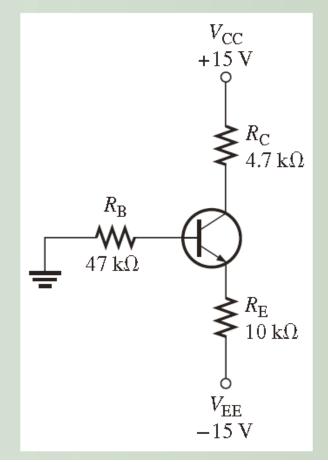
An npn transistor with emitter bias. Voltages with respect to ground are indicated with a single subscript.

17

#### EXAMPLE 5-7

Determine how much the Q-point ( $I_C$ ,  $V_{CE}$ ) for the circuit in Figure 5–18 will change if  $\beta_{DC}$  increases from 100 to 200 when one transistor is replaced by another.

#### ► FIGURE 5–18



**Solution** For  $\beta_{DC} = 100$ ,

$$I_{\text{C(1)}} \cong I_{\text{E}} = \frac{-V_{\text{EE}} - V_{\text{BE}}}{R_{\text{E}} + R_{\text{B}}/\beta_{\text{DC}}} = \frac{-(-15 \text{ V}) - 0.7 \text{ V}}{10 \text{ k}\Omega + 47 \text{ k}\Omega/100} = 1.37 \text{ mA}$$

$$V_{\text{C}} = V_{\text{CC}} - I_{\text{C(1)}}R_{\text{C}} = 15 \text{ V} - (1.37 \text{ mA})(4.7 \text{ k}\Omega) = 8.56 \text{ V}$$

$$V_{\text{E}} = V_{\text{EE}} + I_{\text{E}}R_{\text{E}} = -15 \text{ V} + (1.37 \text{ mA})(10 \text{ k}\Omega) = -1.3 \text{ V}$$

Therefore,

$$V_{\text{CE}(1)} = V_{\text{C}} - V_{\text{E}} = 8.56 \text{ V} - (-1.3 \text{ V}) = 9.83 \text{ V}$$

For  $\beta_{DC} = 200$ ,

$$I_{\text{C(2)}} \cong I_{\text{E}} = \frac{-V_{\text{EE}} - V_{\text{BE}}}{R_{\text{E}} + R_{\text{B}}/\beta_{\text{DC}}} = \frac{-(-15 \text{ V}) - 0.7 \text{ V}}{10 \text{ k}\Omega + 47 \text{ k}\Omega/200} = 1.38 \text{ mA}$$

$$V_{\text{C}} = V_{\text{CC}} - I_{\text{C(2)}}R_{\text{C}} = 15 \text{ V} - (1.38 \text{ mA})(4.7 \text{ k}\Omega) = 8.51 \text{ V}$$

$$V_{\text{E}} = V_{\text{EE}} + I_{\text{E}}R_{\text{E}} = -15 \text{ V} + (1.38 \text{ mA})(10 \text{ k}\Omega) = -1.2 \text{ V}$$

Therefore,

$$V_{\text{CE}(2)} = V_{\text{C}} - V_{\text{E}} = 8.51 \text{ V} - (-1.2 \text{ V}) = 9.71 \text{ V}$$

## **Base Bias**

• Base bias is common in switching circuits, and it has the advantage of simplicity because it uses only one resistor to obtain bias.

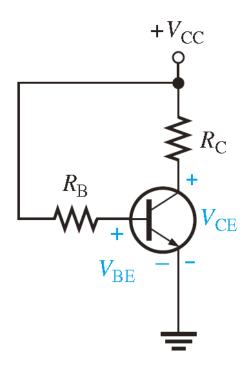
$$V_{\rm CC} - V_{R_{\rm B}} - V_{\rm BE} = 0$$

Substituting  $I_BR_B$  for  $V_{R_B}$ , you get

$$V_{\rm CC} - I_{\rm B}R_{\rm B} - V_{\rm BE} = 0$$

Then solving for  $I_{\rm B}$ ,

$$I_{\rm B} = \frac{V_{\rm CC} - V_{\rm BE}}{R_{\rm B}}$$



#### **FIGURE 5-12**

Base bias.

### **Base Bias**

Kirchhoff's voltage law applied around the collector circuit in Figure 5–19 gives the following equation:

$$V_{\rm CC} - I_{\rm C}R_{\rm C} - V_{\rm CE} = 0$$

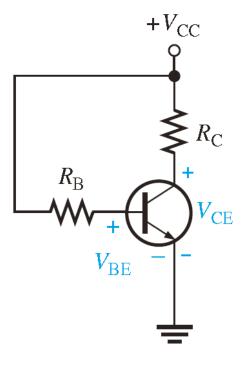
Solving for  $V_{\rm CE}$ ,

$$V_{\rm CE} = V_{\rm CC} - I_{\rm C}R_{\rm C}$$

Substituting the expression for  $I_B$  into the formula  $I_C = \beta_{DC}I_B$  yields

$$I_{\rm C} = \beta_{\rm DC} \left( \frac{V_{\rm CC} - V_{\rm BE}}{R_{\rm B}} \right)$$

*Q-Point Stability of Base Bias* Notice the above Equation shows that  $I_{\rm C}$  is dependent on  $\beta_{\rm DC}$ . The disadvantage of this is that a variation in  $\beta_{\rm DC}$  causes  $I_{\rm C}$  and, as a result,  $V_{\rm CE}$  to change, thus changing the Q-point of the transistor. This makes the base-bias circuit extremely  $\beta$ -dependent and unpredictable.



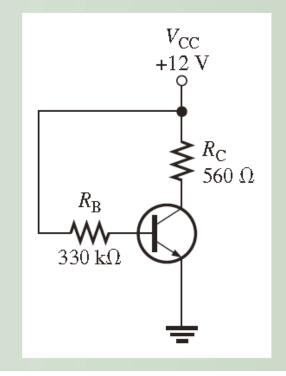
#### **FIGURE 5-12**

Base bias.

**EXAMPLE 5-8** 

Determine how much the Q-point ( $I_{\rm C}$ ,  $V_{\rm CE}$ ) for the circuit in Figure 5–20 will change over a temperature range where  $\beta_{\rm DC}$  increases from 100 to 200.

► FIGURE 5–20



**Solution** For  $\beta_{DC} = 100$ ,

$$I_{\text{C}(1)} = \beta_{\text{DC}} \left( \frac{V_{\text{CC}} - V_{\text{BE}}}{R_{\text{B}}} \right) = 100 \left( \frac{12 \text{ V} - 0.7 \text{ V}}{330 \text{ k}\Omega} \right) = 3.42 \text{ mA}$$
  
 $V_{\text{CE}(1)} = V_{\text{CC}} - I_{\text{C}(1)} R_{\text{C}} = 12 \text{ V} - (3.42 \text{ mA})(560 \Omega) = 10.1 \text{ V}$ 

For  $\beta_{DC} = 200$ ,

$$I_{\text{C(2)}} = \beta_{\text{DC}} \left( \frac{V_{\text{CC}} - V_{\text{BE}}}{R_{\text{B}}} \right) = 200 \left( \frac{12 \text{ V} - 0.7 \text{ V}}{330 \text{ k}\Omega} \right) = 6.84 \text{ mA}$$
  
 $V_{\text{CE(2)}} = V_{\text{CC}} - I_{\text{C(2)}} R_{\text{C}} = 12 \text{ V} - (6.84 \text{ mA})(560 \Omega) = 8.17 \text{ V}$ 

The percent change in  $I_{\rm C}$  as  $\beta_{\rm DC}$  changes from 100 to 200 is

$$\%\Delta I_{\rm C} = \left(\frac{I_{\rm C(2)} - I_{\rm C(1)}}{I_{\rm C(1)}}\right)100\%$$

$$= \left(\frac{6.84 \text{ mA} - 3.42 \text{ mA}}{3.42 \text{ mA}}\right)100\% = 100\% \text{ (an increase)}$$

The percent change in  $V_{\rm CR}$  is

$$\%\Delta V_{\text{CE}} = \left(\frac{V_{\text{CE}(2)} - V_{\text{CE}(1)}}{V_{\text{CE}(1)}}\right) 100\%$$
$$= \left(\frac{8.17 \text{ V} - 10.1 \text{ V}}{10.1 \text{ V}}\right) 100\% = -19.1\% \text{ (a decrease)}$$