

Please check the examination details below before entering your candidate information

Candidate surname					Other names				
Centre Number					Candidate Number				
<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	

**Pearson Edexcel Level 3 GCE**

Time 2 hours	Paper reference	<b>8MA0/01</b>
--------------	-----------------	----------------

**Mathematics**

**Advanced Subsidiary**

**PAPER 1: Pure Mathematics**

<p><b>You must have:</b> Mathematical Formulae and Statistical Tables (Green), calculator</p>	<p>Total Marks</p>
---	--------------------

**Candidates may use any calculator allowed by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 14 questions in this question paper. The total mark for this paper is 100.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

P69201A

©2022 Pearson Education Ltd.

Q:1/1/1/1/



1. Find

$$\int \left( 8x^3 - \frac{3}{2\sqrt{x}} + 5 \right) dx$$

giving your answer in simplest form.

(4)

$$\int 8x^3 - \frac{3}{2}x^{\frac{1}{2}} + 5 \, dx$$

$$= \frac{8x^4}{4} - \frac{\frac{3}{2}x^{\frac{3}{2}}}{\frac{3}{2}} + 5x + C$$

$$= 2x^4 - x^{\frac{3}{2}} + 5x + C$$



**Question 1 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

**(Total for Question 1 is 4 marks)**

2.

$$f(x) = 2x^3 + 5x^2 + 2x + 15$$

(a) Use the factor theorem to show that  $(x + 3)$  is a factor of  $f(x)$ . (2)

(b) Find the constants  $a$ ,  $b$  and  $c$  such that

$$f(x) = (x + 3)(ax^2 + bx + c) \quad (2)$$

(c) Hence show that  $f(x) = 0$  has only one real root. (2)

(d) Write down the real root of the equation  $f(x - 5) = 0$  (1)

a)  $(x+3)$  factor  $\rightarrow n = -3$

$$0 = 2(-3)^3 + 5(-3)^2 + 2(-3) + 15$$

$$0 = 0 \quad \checkmark \checkmark$$

$$\begin{array}{r} 2x^2 \quad \quad \quad -x + 5 \\ x+3 \overline{) 2x^3 + 5x^2 + 2x + 15} \end{array}$$

$$6x^2$$

$$-x^2 + 2x$$

$$-3x$$

$$5x + 15$$

$$+ 15$$

$$(x+3)(2x^2 - x + 5)$$



Question 2 continued

$$(x+3)=0$$

$$x = -3$$



ONLY  
ONE  
ROOT



$$2x^2 - x + 5 = 0$$

$$b^2 - 4ac$$

$$= (-1)^2 - 4(2)(5)$$

$$= 1 - 40$$

$$= -39$$

$$-39 < 0$$

No real roots

$$f(2-5) = 0$$

$$x+3-5=0$$

$$x-2=0$$

$$x=2$$



**Question 2 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Question 2 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

**(Total for Question 2 is 7 marks)**

3. The triangle  $PQR$  is such that  $\vec{PQ} = 3\mathbf{i} + 5\mathbf{j}$  and  $\vec{PR} = 13\mathbf{i} - 15\mathbf{j}$

(a) Find  $\vec{QR}$

(2)

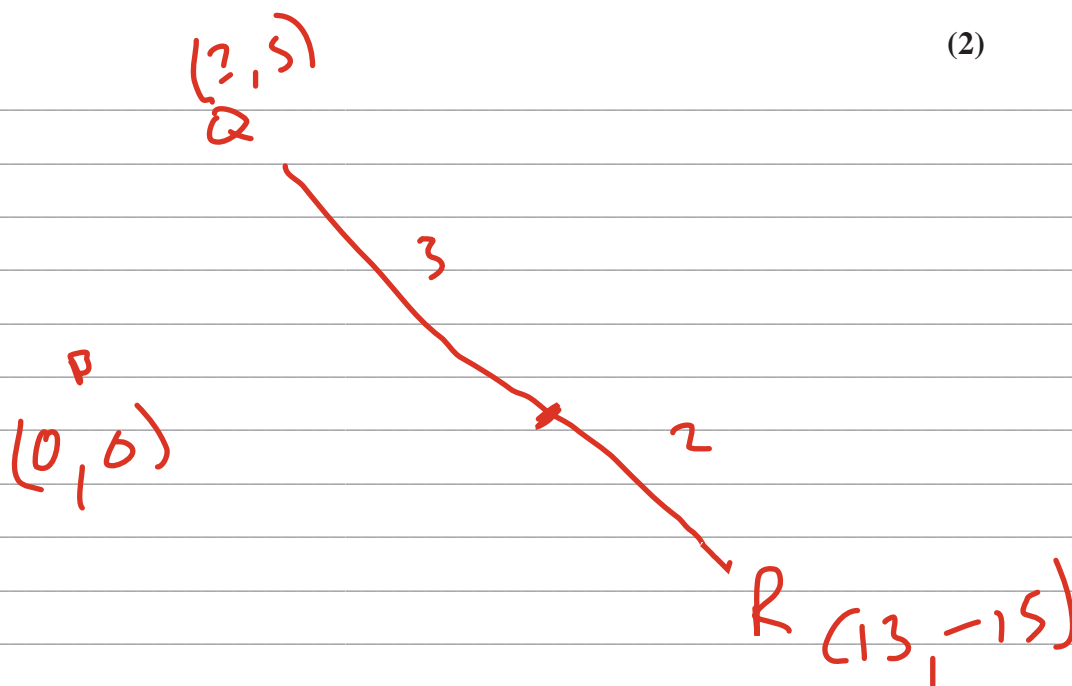
(b) Hence find  $|\vec{QR}|$  giving your answer as a simplified surd.

(2)

The point  $S$  lies on the line segment  $QR$  so that  $QS:SR = 3:2$

(c) Find  $\vec{PS}$

(2)



$$a) \vec{QR} = 10, -20 \quad \text{or} \quad 10\mathbf{i} - 20\mathbf{j}$$

$$b) |\vec{QR}| = \sqrt{10^2 + 20^2}$$

$$= \sqrt{500} \quad \text{or} \quad 5\sqrt{10}$$

$$\begin{aligned} a) \vec{PS} &= \vec{PQ} + \vec{QS} \\ &= 3\mathbf{i} + 5\mathbf{j} + \frac{3}{5}(10\mathbf{i} - 20\mathbf{j}) \\ &= 3\mathbf{i} + 6\mathbf{i} + 5\mathbf{j} - 12\mathbf{j} \\ &= 8\mathbf{i} - 6\mathbf{j} \end{aligned}$$





**Question 3 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

**(Total for Question 3 is 6 marks)**

4.

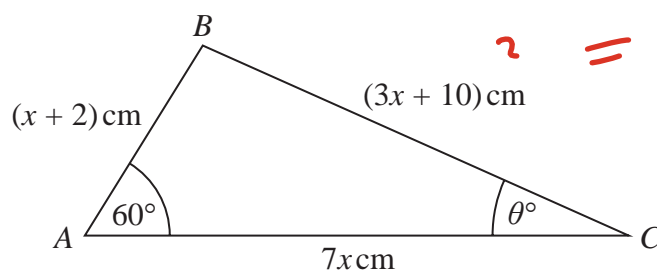


Figure 1

Figure 1 shows a sketch of triangle  $ABC$  with  $AB = (x + 2)\text{ cm}$ ,  $BC = (3x + 10)\text{ cm}$ ,  $AC = 7x\text{ cm}$ , angle  $BAC = 60^\circ$  and angle  $ACB = \theta^\circ$

(a) (i) Show that  $17x^2 - 35x - 48 = 0$

(3)

(ii) Hence find the value of  $x$ .

(1)

(b) Hence find the value of  $\theta$  giving your answer to one decimal place.

(2)

$$\text{a) i) } a^2 = b^2 + c^2 - 2bc \cos A$$

$$4x^2 + 60x + 100$$

$$= 50x^2 + 4x + 4 - (14x^2 + 28 \cos 60)$$

$$= 50x^2 + 4x + 4$$



**Question 4 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Question 4 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Question 4 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

**(Total for Question 4 is 6 marks)**

P 6 9 2 0 1 A 0 1 3 4 8

5. The mass,  $A$  kg, of algae in a small pond, is modelled by the equation

$$A = pq^t$$

where  $p$  and  $q$  are constants and  $t$  is the number of weeks after the mass of algae was first recorded.

Data recorded indicates that there is a linear relationship between  $t$  and  $\log_{10} A$  given by the equation

$$\log_{10} A = 0.03t + 0.5$$

- (a) Use this relationship to find a complete equation for the model in the form

$$A = pq^t$$

giving the value of  $p$  and the value of  $q$  each to 4 significant figures.

(4)

- (b) With reference to the model, interpret

(i) the value of the constant  $p$ ,

(ii) the value of the constant  $q$ .

(2)

- (c) Find, according to the model,

(i) the mass of algae in the pond when  $t = 8$ , giving your answer to the nearest 0.5 kg,

(ii) the number of weeks it takes for the mass of algae in the pond to reach 4 kg.

(3)

- (d) State one reason why this may not be a realistic model in the long term.

(1)

$$a) \log_{10} A = 0.03t + 0.5$$

$$10^{0.03t + 0.5} = A$$

$$(10^{0.03})^t \times \sqrt{10} = A$$

$$A = (\sqrt{10})(10^{0.03})^t$$

b) Start mass, extra mass each week of algae



## Question 5 continued

$$c) A = \sqrt{10} \times (10^{0.03})^3$$

$$A = 5.5 \text{ kg}$$

d

$$4 = \sqrt{10} \times (10^{0.03})^t$$

$$\frac{4}{\sqrt{10}} = 10^{0.03t}$$

$$1.26 = 10^{0.03t}$$

$$\log 1.26 = \log 10^{0.03t}$$

$$10^{\log 1.26} = 10^{0.03t}$$

$$t = \frac{10^{\log 1.26}}{0.03}$$

$$t = 3.4 \text{ weeks}$$



**Question 5 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA





**Question 5 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

**(Total for Question 5 is 10 marks)**

6. (a) Find the first 4 terms, in ascending powers of  $x$ , of the binomial expansion of

$$\left(3 - \frac{2x}{9}\right)^8$$

giving each term in simplest form.

(4)

$$f(x) = \left(\frac{x-1}{2x}\right)\left(3 - \frac{2x}{9}\right)^8$$

- (b) Find the coefficient of  $x^2$  in the series expansion of  $f(x)$ , giving your answer as a simplified fraction.

(2)

$$\begin{aligned} a) \quad & \binom{8}{0} (3)^8 \left(-\frac{2x}{9}\right)^0 = 6561 \\ & \binom{8}{1} (3)^7 \left(-\frac{2x}{9}\right)^1 = -3888x \\ & \binom{8}{2} (3)^6 \left(-\frac{2x}{9}\right)^2 = 1008x^2 \\ & \binom{8}{3} (3)^5 \left(-\frac{2x}{9}\right)^3 = -\frac{448}{3}x^3 \end{aligned}$$

$$\begin{aligned} b) \quad f(x) &= \left(\frac{x-1}{2x}\right) \left(3 - \frac{2x}{9}\right)^8 \\ &= \left(\frac{1}{2} - \frac{1}{2}x^{-1}\right) \left(3 - \frac{2x}{9}\right)^8 \end{aligned}$$

$$\begin{aligned} & \frac{1}{2} \times 1008x^2 - \frac{1}{2}x^{-1} \times -\frac{448}{3}x^3 \\ &= 504x^2 + \frac{224}{3}x^2 \\ &= \frac{1736}{3}x^2 \end{aligned}$$

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Question 6 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



P 6 9 2 0 1 A 0 1 9 4 8

**Question 6 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Question 6 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

**(Total for Question 6 is 6 marks)**

7. (a) Factorise completely  $9x - x^3$

(2)

The curve  $C$  has equation

$$y = 9x - x^3$$

- (b) Sketch  $C$  showing the coordinates of the points at which the curve cuts the  $x$ -axis.

(2)

The line  $l$  has equation  $y = k$  where  $k$  is a constant.

Given that  $C$  and  $l$  intersect at 3 distinct points,

- (c) find the range of values for  $k$ , writing your answer in set notation.

**Solutions relying on calculator technology are not acceptable.**

(3)

a)  $9x - x^3$   $x < 0, -3, 3$

$x(9 - x^2)$

$x(3+x)(3-x)$

b)



Question 7 continued

$$y = 9x - x^3$$

$$y = k$$

$$\frac{dy}{dx} = 9 - 3x^2$$

$$= 9 - 3x^2 = 0$$

$$3x^2 = 9$$

$$x^2 = 3$$

$$x = \pm \sqrt{3}$$

$$\begin{aligned} y &= 9(\sqrt{3}) - (\sqrt{3})^3 \\ &= 9\sqrt{3} - 3\sqrt{3} \\ &= 6\sqrt{3} \end{aligned}$$

$$\begin{aligned} y &= 9(-\sqrt{3}) - (-\sqrt{3})^3 \\ &= -9\sqrt{3} + 3\sqrt{3} \\ &= -6\sqrt{3} \end{aligned}$$

$$-6\sqrt{3} \leq k \leq 6\sqrt{3}$$

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



P 6 9 2 0 1 A 0 2 3 4 8

**Question 7 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA





**Question 7 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

**(Total for Question 7 is 7 marks)**

8.

In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

The air pressure,  $P$  kg/cm<sup>2</sup>, inside a car tyre,  $t$  minutes from the instant when the tyre developed a puncture is given by the equation

$$P = k + 1.4e^{-0.5t} \quad t \in \mathbb{R} \quad t \geq 0$$

where  $k$  is a constant.

Given that the initial air pressure inside the tyre was 2.2 kg/cm<sup>2</sup>

(a) state the value of  $k$ .

(1)

From the instant when the tyre developed the puncture,

(b) find the time taken for the air pressure to fall to 1 kg/cm<sup>2</sup>  
Give your answer in minutes to one decimal place.

(3)

(c) Find the rate at which the air pressure in the tyre is decreasing exactly 2 minutes from the instant when the tyre developed the puncture.  
Give your answer in kg/cm<sup>2</sup> per minute to 3 significant figures.

(2)

$$c) \quad 2.2 = 1.4e^0 + k$$

$$k = 0.8$$

$$b) \quad 1 = 0.8 + 1.4e^{-0.5t}$$

$$0.2 = 1.4e^{-0.5t}$$

$$e^{-0.5t} = \frac{1}{7}$$

$$\ln e^{-0.5t} = \ln \frac{1}{7}$$

$$e^{\ln \frac{1}{7}} = e^{-0.5t}$$

$$\ln \frac{1}{7} = -0.5t$$



Question 8 continued

$$t = \frac{1.17}{-0.5}$$

$$t = 3.74 \text{ minutes}$$

$$3.9 \text{ (1 dp)}$$

c)

$$P = 0.8 + 1.4e^{-0.5t}$$

$$\frac{dP}{dt} = -0.7e^{-0.5t} \quad t = 2$$

$$= -0.7e^{-0.5(2)}$$

$$= -0.258$$

decreasing at a rate

or  $-0.258 \text{ kg/cm}^3$   
per minute

(Total for Question 8 is 6 marks)



9. (a) Given that  $p = \log_3 x$ , where  $x > 0$ , find in simplest form in terms of  $p$ ,

(i)  $\log_3 \left( \frac{x}{9} \right)$

(ii)  $\log_3 (\sqrt{x})$

$$2(p-2) + 3\left(\frac{1}{2}p\right) = -11 \quad (2)$$

(b) Hence, or otherwise, solve

$$2\left(\log_3 \left(\frac{x}{9}\right)\right) + 3\log_3 (\sqrt{x}) = -11$$

giving your answer as a simplified fraction.

Solutions relying on calculator technology are not acceptable.

(4)

a)  $p = \log_3 x$

i)  $\log_3 \frac{x}{9}$

$$= \log_3 x - \log_3 9$$

$$= p - 2$$

ii)  $\log_3 \sqrt{x}$

$$= \log_3 x^{1/2}$$

$$= \frac{1}{2} \log_3 x = \frac{1}{2} p$$



## Question 9 continued

$$b) 2(p-2) + 3\left(\frac{1}{2}p\right) = -11$$

$$2p - 4 + 3\frac{1}{2}p = -11$$

$$\frac{7}{2}p = -7$$

$$p = -2$$

$$\log_3 x = p$$

$$3^p = x$$

$$x = 3^{-2}$$

$$x = \frac{1}{9}$$

(Total for Question 9 is 6 marks)



10.

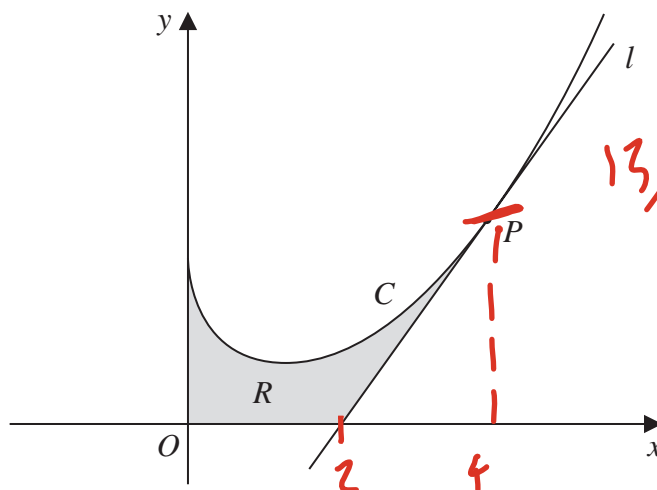


Figure 2

In this question you must show all stages of your working.

Solutions relying on calculator technology are not acceptable.

Figure 2 shows a sketch of part of the curve  $C$  with equation

$$y = \frac{1}{3}x^2 - 2\sqrt{x} + 3 \quad x \geq 0$$

The point  $P$  lies on  $C$  and has  $x$  coordinate 4

The line  $l$  is the tangent to  $C$  at  $P$ .

(a) Show that  $l$  has equation

$$13x - 6y - 26 = 0 \quad (5)$$

The region  $R$ , shown shaded in Figure 2, is bounded by the  $y$ -axis, the curve  $C$ , the line  $l$  and the  $x$ -axis.

(b) Find the exact area of  $R$ .

(5)

$$y = \frac{1}{3}x^2 - 2x^{1/2} + 3$$

$$\frac{dy}{dx} = \frac{2}{3}x - x^{-1/2}$$

$$x = 4$$

$$\frac{2}{3}(4) - \frac{1}{\sqrt{4}}$$

$$\frac{8}{3} - \frac{1}{2} = \frac{13}{6}$$



Question 10 continued

$$y = \frac{1}{3}(x)^2 - 2\sqrt{4} + 3$$

$$m = \frac{13}{6}$$

$$\frac{16}{3} - \frac{12}{3} + \frac{9}{3}$$

$$\frac{13}{3}$$

$$y - \frac{13}{3} = \frac{13}{6}(x - 4)$$

$$6y - 26 = 13x - 52$$

$$\rightarrow 13x - 6y - 26 = 0$$

$$6y = 13x - 26$$

$$y = \frac{13}{6}x - \frac{13}{3}$$

$$\frac{13}{3} = \frac{13}{6}x$$

$$\frac{13}{3} \times \frac{6}{13} = 2$$

$$x = 2$$



## Question 10 continued

$$R =$$

$$\int_0^4 \frac{1}{3}x^2 - 2x^{1/2} + 3 \quad - \quad \int_2^4 \frac{13}{6}x - \frac{13}{3}$$

$$\frac{1}{9}x^3 - \frac{2x^{3/2}}{3/2} + 3x$$

$$\left[ \frac{13}{12}x^2 - \frac{13}{3}x \right]_2^4$$

$$\left[ \frac{1}{9}x^3 - \frac{4}{3}x^{3/2} + 3x \right]_0^4$$

$$\left[ \frac{13}{12}(4)^2 - \frac{13}{3}(4) \right]$$

$$\frac{1}{9}(4)^3 - \frac{4}{3}(4)^{3/2} + 3(4)$$

$$\frac{208}{12} - \frac{52}{3}$$

$$\frac{64}{9} - \frac{32}{3} + 12$$

$$\frac{208}{12} - \frac{208}{12} = 0$$

$$\frac{64}{9} - \frac{96}{9} + \frac{108}{9}$$

$$\frac{76}{9}$$

$$\frac{13}{12}(2)^2 - \frac{13}{3}(2)$$

$$\frac{52}{12} - \frac{26}{3}$$

$$\frac{52}{12} - \frac{104}{12}$$

$$- \frac{52}{12}$$

$$\frac{304}{36} - \frac{104}{36}$$

$$\frac{148}{36} = \frac{94}{18} = \frac{33}{6} = \frac{11}{2} \text{ m/s}^2$$

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA





Question 10 continued

$$76,9 - 39,9 = 37,9 \text{ mg}^2$$

(Total for Question 10 is 10 marks)



P 6 9 2 0 1 A 0 3 3 4 8

11.

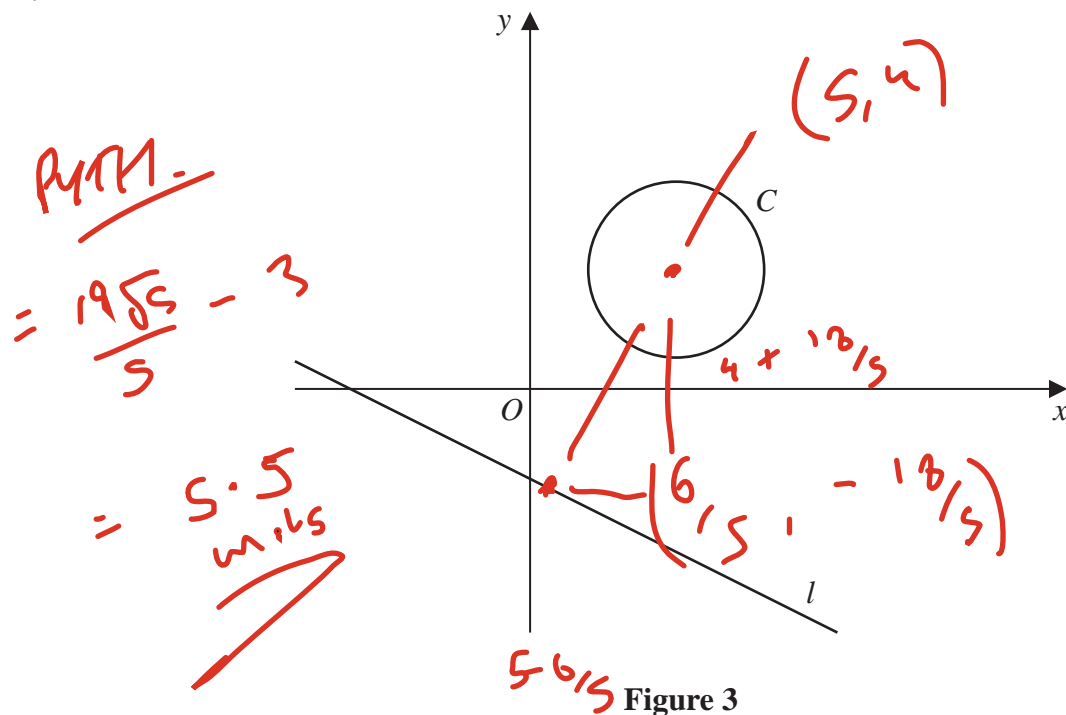


Figure 3 shows the circle  $C$  with equation

$$x^2 + y^2 - 10x - 8y + 32 = 0$$

and the line  $l$  with equation

$$2y + x + 6 = 0$$

(a) Find

- (i) the coordinates of the centre of  $C$ ,
- (ii) the radius of  $C$ .

(3)

(b) Find the shortest distance between  $C$  and  $l$ .

(5)

Q 1)  $(x-5)^2 - 25 + (y-4)^2 - 16 + 32 = 0$

$(x-5)^2 + (y-4)^2 = 9$

i) ii) Centre =  $(5, 4)$  Radius =  $\sqrt{9} = 3$



## Question 11 continued

$$b) \quad 2y = -x - 6$$

$$y = -\frac{1}{2}x - 3$$

$$\text{radius gradient} = 2$$

$$\text{radius} \rightarrow y - 7 = 2(x - 5)$$

$$y = 2x - 6$$

$$2x - 6 = -\frac{1}{2}x - 3$$

$$\frac{5}{2}x = 3$$

$$x = \frac{6}{5}$$

$$\left(\frac{6}{5}, -\frac{12}{5}\right)$$

$$\sqrt{(x-5)^2 + (y-7)^2} = 3$$

$$\sqrt{\left(\frac{6}{5}-5\right)^2 + \left(-\frac{12}{5}-7\right)^2} = 3$$

$$\sqrt{\left(\frac{6-25}{5}\right)^2 + \left(\frac{-12-35}{5}\right)^2} = 3$$

$$\sqrt{\left(\frac{-19}{5}\right)^2 + \left(\frac{-47}{5}\right)^2} = 3$$

$$\sqrt{\frac{361}{25} + \frac{2209}{25}} = 3$$

$$\sqrt{\frac{2570}{25}} = 3$$

$$\sqrt{102.8} = 3$$

$$10.14 = 3$$

$$10.14 \neq 3$$

$$(x-5)^2 + (y-7)^2 = 9$$

$$x^2 - 10x + 25 + y^2 - 14y + 49 = 9$$

$$x^2 - 10x + y^2 - 14y + 65 = 9$$

$$x^2 - 10x + y^2 - 14y + 56 = 0$$

**Question 11 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Question 11 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

**(Total for Question 11 is 8 marks)**

12. A company makes drinks containers out of metal.

The containers are modelled as closed cylinders with base radius  $r$  cm and height  $h$  cm and the capacity of each container is  $355 \text{ cm}^3$

The metal used

- for the circular base and the curved side costs  $0.04 \text{ pence/cm}^2$
- for the circular top costs  $0.09 \text{ pence/cm}^2$

Both metals used are of negligible thickness.

- (a) Show that the total cost,  $C$  pence, of the metal for one container is given by

$$C = 0.13\pi r^2 + \frac{28.4}{r} \quad (4)$$

- (b) Use calculus to find the value of  $r$  for which  $C$  is a minimum, giving your answer to 3 significant figures. (4)

- (c) Using  $\frac{d^2C}{dr^2}$  prove that the cost is minimised for the value of  $r$  found in part (b). (2)

- (d) Hence find the minimum value of  $C$ , giving your answer to the nearest integer. (2)

$$\int_1^2 3x^2 - 7x + 9$$

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Question 12 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Question 12 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA





**Question 12 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

**(Total for Question 12 is 12 marks)**

P 6 9 2 0 1 A 0 4 1 4 8

13.

In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

(a) Show that

$$\frac{1}{\cos \theta} + \tan \theta \equiv \frac{\cos \theta}{1 - \sin \theta} \quad \theta \neq (2n + 1)90^\circ \quad n \in \mathbb{Z} \quad (3)$$

Given that  $\cos 2x \neq 0$ (b) solve for  $0 < x < 90^\circ$ 

$$\frac{1}{\cos 2x} + \tan 2x = 3 \cos 2x$$

giving your answers to one decimal place.

(5)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Question 13 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Question 13 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Question 13 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

**(Total for Question 13 is 8 marks)**

14. (i) A student states

“if  $x^2$  is greater than 9 then  $x$  must be greater than 3”

Determine whether or not this statement is true, giving a reason for your answer.

(1)

(ii) Prove that for all positive integers  $n$ ,

$$n^3 + 3n^2 + 2n$$

is divisible by 6

(3)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Question 14 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



P 6 9 2 0 1 A 0 4 7 4 8

**Question 14 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

**(Total for Question 14 is 4 marks)****TOTAL FOR PAPER IS 100 MARKS**