FUN with Complexity: Walking through Doors is Hard, even without Staircases

Manuel Frohn

RWTH Aachen

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Theory

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Application

Socobond is PSPACE-Hard Super Mario Galaxy 2 is PSPACE-Hard Super Mario Galaxy is PSPACE-Hard Super Mario Odessy is PSPACE-Hard

PSPACE-Complexity

A given problem requires a polynomial amount of memory in relation to the input, to be solved \Leftrightarrow The problem is in PSPACE

SAT

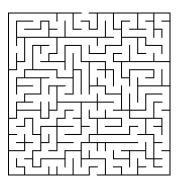
Quantified SAT

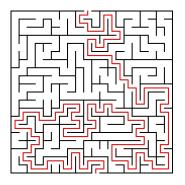
$$x_1 \wedge x_2 \vee \neg x_3$$

$$\forall x_1 \exists x_2 : x_1 \land x_2 \lor \neg x_3$$

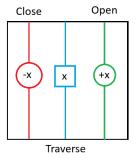
1-PlayerMotionPlaning

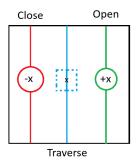
Given: Environment, Agent, Goal Question: Is the goal achivable





Basic Door Device





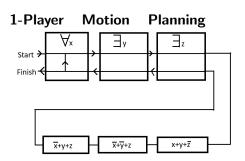
PSPACE-hardness of doors

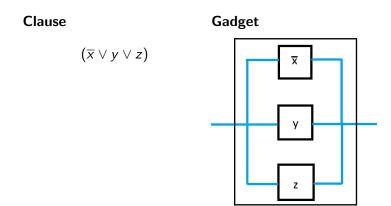
Theorem

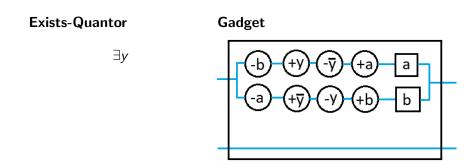
If a game features door devices which each are controlled by an open and a close preasure plate and the agent has to navigate from entrance to exit, then the game is PSPACE-hard

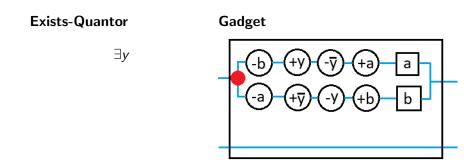
True Quantified SAT

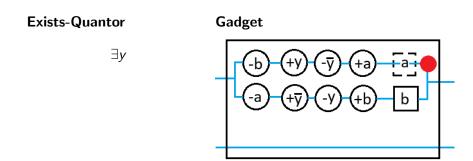
$$\forall x \exists y \exists z : (\overline{x} \lor y \lor z) \land (\overline{x} \lor \overline{y} \lor z) \land (\lor x \lor y \lor \overline{z})$$





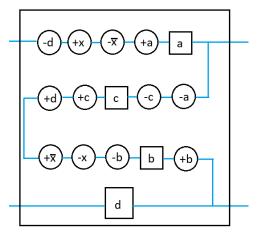






 $\forall x$

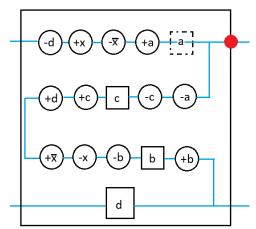
All-Quantor



All-Quantor Gadget $\forall x$

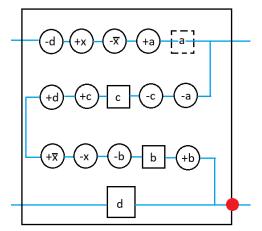
All-Quantor

 $\forall x$



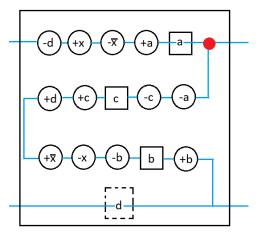
All-Quantor

 $\forall x$

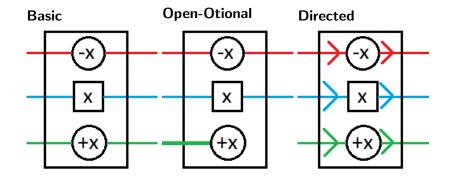


All-Quantor

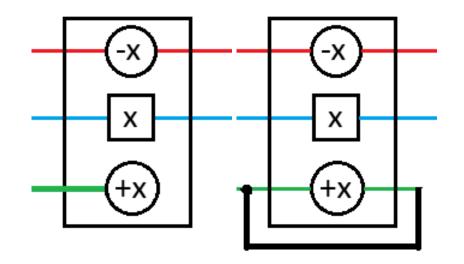
 $\forall x$



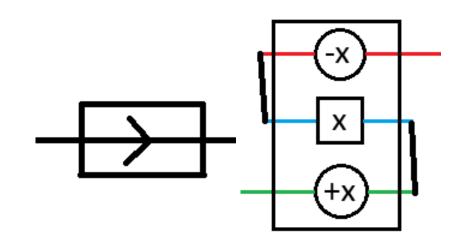
Door Device - Variants



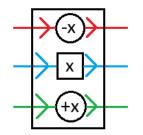
PSpace-Hardness - Open optinal door

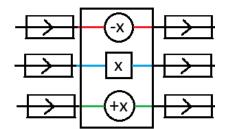


The Diode

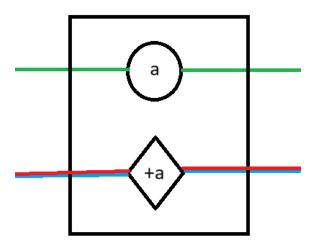


PSpace-Hardness - Directed Door

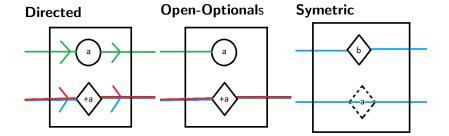




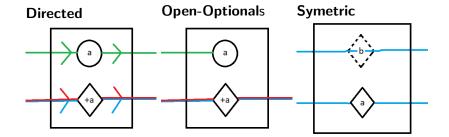
Self closing doors

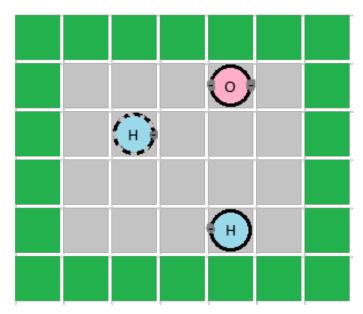


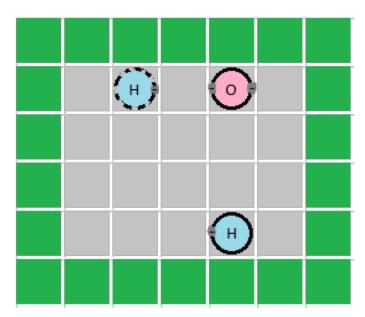
Self closing doors - Variants

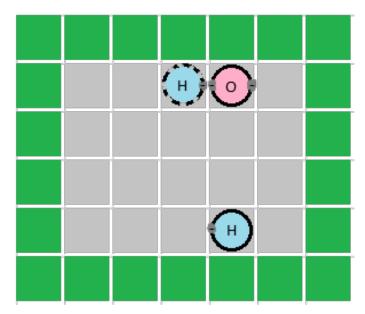


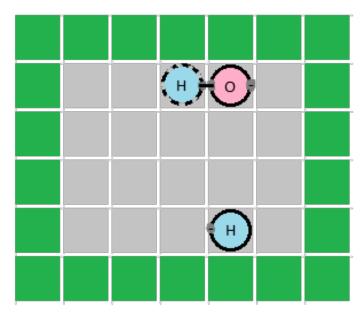
Self closing doors - Variants

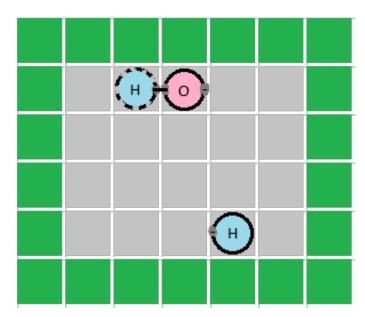


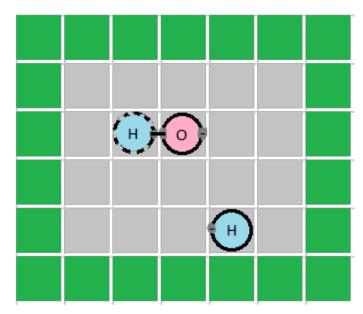


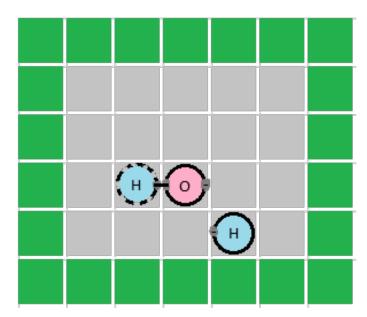


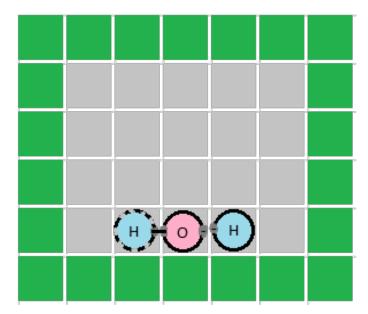


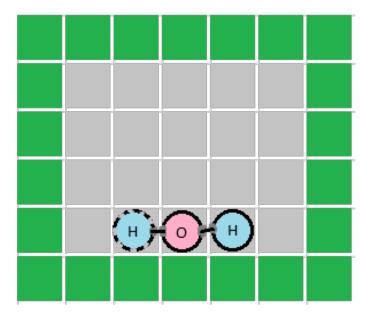


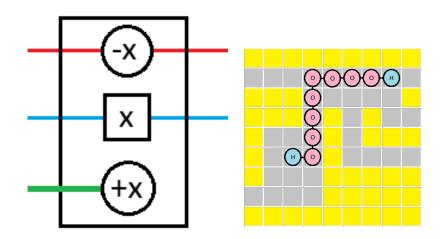


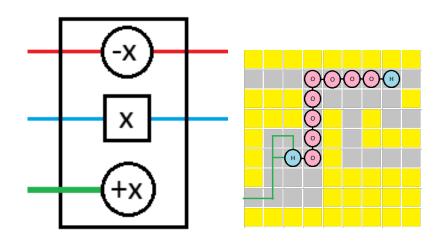


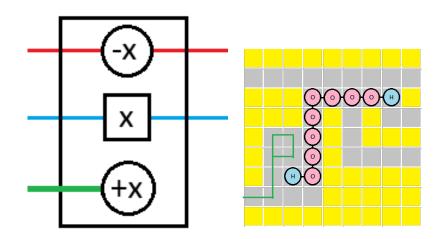


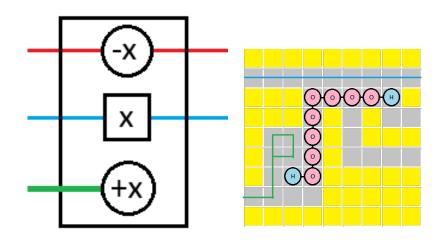


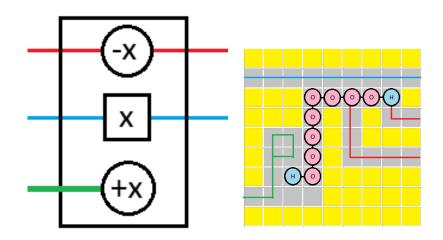


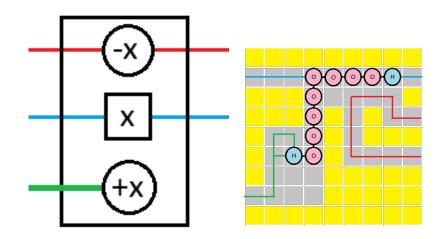




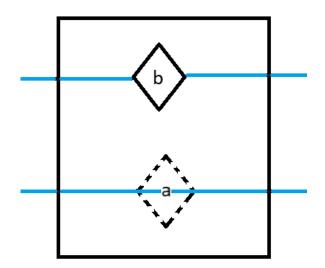




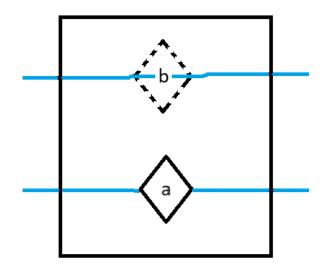




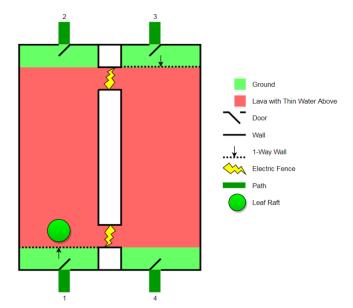
Reminder - Symetric self closing door



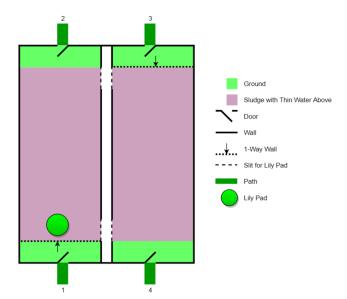
Reminder - Symetric self closing door



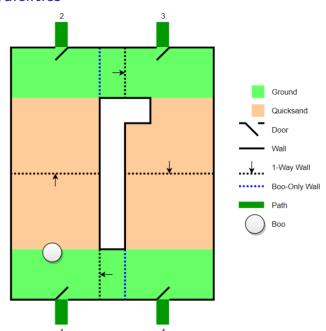
Super Mario Galaxy 2 is PSpace-hard



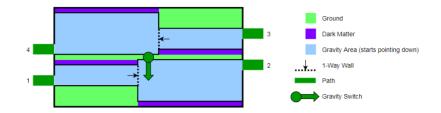
Parralelities



Parralelities



Super Mario Galaxy is PSpace-hard



Super Mario Odessy is PSpace-hard

