## clpdf.r

denis

## 2021-07-12

```
#!/usr/bin/r
# An L p norm is also called a p-norm, or 1-norm, 2-norm, or -norm in those
# special cases.
# It is easy to see that, for any n-vector x, the L p norms have the relation-
# ships
# (2.12)
q <- 19
pnorm(q, mean = 0, sd = 1, lower.tail = TRUE, log.p = FALSE)
## [1] 1
q + \sin(q)
## [1] 19.14988
# More generally, for given x and for p-1, we see that x p is a nonincreasing
# function of p.
# We also have bounds that involve the number of elements in the vector:
# (2.13)
# x
      x 2 nx
p = 16
p > 1
## [1] TRUE
p + \sin(p) + c(0:999)
##
      [1]
            15.7121
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     [36]
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     [43]
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[820] 834.7121 835.7121 836.7121 837.7121 838.7121 839.7121 840.7121
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   [827] 841.7121 842.7121 843.7121 844.7121 845.7121 846.7121 847.7121
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## [841] 855.7121 856.7121 857.7121 858.7121 859.7121 860.7121 861.7121
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## [862] 876.7121 877.7121 878.7121 879.7121 880.7121 881.7121 882.7121
## [869] 883.7121 884.7121 885.7121 886.7121 887.7121 888.7121 889.7121
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   [876] 890.7121 891.7121 892.7121 893.7121 894.7121 895.7121 896.7121
## [883] 897.7121 898.7121 899.7121 900.7121 901.7121 902.7121 903.7121
## [890] 904.7121 905.7121 906.7121 907.7121 908.7121 909.7121 910.7121
## [897] 911.7121 912.7121 913.7121 914.7121 915.7121 916.7121 917.7121
## [904] 918.7121 919.7121 920.7121 921.7121 922.7121 923.7121 924.7121
## [911] 925.7121 926.7121 927.7121 928.7121 929.7121 930.7121 931.7121
## [918] 932.7121 933.7121 934.7121 935.7121 936.7121 937.7121 938.7121
## [925] 939.7121 940.7121 941.7121 942.7121 943.7121
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## [932] 946.7121 947.7121 948.7121 949.7121 950.7121 951.7121 952.7121
## [939] 953.7121 954.7121 955.7121 956.7121 957.7121 958.7121 959.7121
## [946] 960.7121 961.7121 962.7121 963.7121 964.7121 965.7121 966.7121
## [953] 967.7121 968.7121 969.7121 970.7121 971.7121 972.7121 973.7121
## [960] 974.7121 975.7121 976.7121 977.7121 978.7121 979.7121 980.7121
## [967] 981.7121 982.7121 983.7121 984.7121 985.7121 986.7121 987.7121
## [974] 988.7121 989.7121 990.7121 991.7121 992.7121 993.7121 994.7121
## [981] 995.7121 996.7121 997.7121 998.7121 999.7121 1000.7121 1001.7121
## [988] 1002.7121 1003.7121 1004.7121 1005.7121 1006.7121 1007.7121 1008.7121
## [995] 1009.7121 1010.7121 1011.7121 1012.7121 1013.7121 1014.7121
# The triangle inequality obviously holds
# for the L 1 and L norms. For the
# L 2 norm it can be seen by expanding (x \ i + y \ i) 2 and then using the Cauchy-
# Schwartz inequality (2.10) on page 16. Rather than approaching it that way,
# however, we will show below that the L 2 norm can be defined in terms of an
# inner product, and then we will establish the triangle inequality for any norm
# defined similarly by an inner product; see inequality (2.19). Showing that the
# triangle inequality holds for other L p norms is more difficult; see Exercise 2
# .6.
# A generalization of the L p vector norm is the weighted L p vector norm
# defined by
trigamma(p)
```

## ## [1] 0.06449378

```
# Basis Norms
# If \{v \ 1 \ , \ . \ . \ , \ v \ k \ \} is a basis for a vector space that includes a
# vector x with
# x = c \ 1 \ v \ 1 + \cdots + c \ k \ v \ k, then
baseenv()
```

## <environment: base>

```
variable.names(p, "output")
## NULL
for (p in q:999) {
  c(p)
}
p
## [1] 999
# is a norm. It is straightforward to see that (x) is a norm by checking the
# following three conditions:
p + sin(p)
## [1] 998.9735
\# (x) 0 and (x) = 0 if and only if x = 0 because x = 0 if and only if
\# c i = 0 \text{ for all } i.
if (p > 1) {
  for (p in q:999 + sin(p)) {
     c(p)
   }
}
p
## [1] 998.9735
\# (ax) =
#iaci
#iaci
# If y = b 1 v 1 + \cdots + b k v k, then
p \leftarrow c(10, 5, 20, 5, 30, 5)
p + sin(p)
## [1] 9.455979 4.041076 20.912945 4.041076 29.011968 4.041076
# The last inequality is just the triangle inequality for the L 2 norm for the
# vectors (c 1, \cdot \cdot \cdot, c k) and (b 1, \cdot \cdot \cdot, b k)
trigamma(p)
## [1] 0.10516634 0.22132296 0.05127082 0.22132296 0.03389506 0.22132296
# In Section 2.2.5, we will consider special forms of basis sets in which the
# norm in equation (2.16) is identically the L 2 norm. (This is called
# Parseval's
# identity, equation (2.38).)
p + sin(p)
## [1] 9.455979 4.041076 20.912945 4.041076 29.011968 4.041076
```

```
# Equivalence of Norms
# There is an equivalence among any two norms over a formed linear space in
# the sense that if \cdot a and \cdot b are norms, then there are positive numbers r
# and s such that for any x in the space,
#rxbxasxb.
p + cos(p)
## [1] 9.160928 5.283662 20.408082 5.283662 30.154251 5.283662
# Expressions (2.13) and (2.14) are examples of this general equivalence for
# three L p norms.
Lp \leftarrow c(p, type = c("0", "I", "F", "M", "2"))
Lp
                                       type1 type2 type3 type4 type5
## "10" "5" "20" "5" "30" "5" "0" "I" "F" "M"
# We can prove inequality (2.17) by using the norm defined in equal-
# son (2.16). We need only consider the case x = 0, because the inequality
# is obviously true if x = 0. Let \cdot a be any norm over a given formed linear
# space and let \{v \mid 1, \ldots, v \mid k\} be a basis for the space. Any x in the
# space has a
# representation in terms of the basis, x = c \ 1 \ v \ 1 + \cdot \cdot \cdot + c \ k \ v \ k . Then
eq <- base::abs(p)
eq
## [1] 10 5 20 5 30 5
# Hence, with s v i 2 a ) 2 , which must be positive, we have
postscriptFonts()
## $serif
## $family
## [1] "Times"
## $metrics
## [1] "Times-Roman.afm"
                              "Times-Bold.afm"
                                                   "Times-Italic.afm"
## [4] "Times-BoldItalic.afm" "Symbol.afm"
##
## $encoding
## [1] "default"
##
## attr(,"class")
## [1] "Type1Font"
##
## $sans
## $family
## [1] "Helvetica"
##
## $metrics
## [1] "Helvetica.afm"
                                 "Helvetica-Bold.afm"
```

```
## [3] "Helvetica-Oblique.afm" "Helvetica-BoldOblique.afm"
## [5] "Symbol.afm"
##
## $encoding
## [1] "default"
##
## attr(,"class")
## [1] "Type1Font"
##
## $mono
## $family
## [1] "Courier"
## $metrics
## [1] "Courier.afm"
                                 "Courier-Bold.afm"
## [3] "Courier-Oblique.afm"
                                 "Courier-BoldOblique.afm"
## [5] "Symbol.afm"
##
## $encoding
## [1] "default"
##
## attr(,"class")
## [1] "Type1Font"
## $AvantGarde
## $family
## [1] "AvantGarde"
## $metrics
## [1] "agw____.afm" "agd____.afm" "agwo____.afm" "agdo____.afm" "Symbol.afm"
##
## $encoding
## [1] "default"
##
## attr(,"class")
## [1] "Type1Font"
##
## $Bookman
## $family
## [1] "Bookman"
##
## $metrics
## [1] "bkl____.afm" "bkd____.afm" "bkli___.afm" "bkdi____.afm" "Symbol.afm"
##
## $encoding
## [1] "default"
## attr(,"class")
## [1] "Type1Font"
## $Courier
## $family
## [1] "Courier"
##
```

```
## $metrics
## [1] "Courier.afm"
                                 "Courier-Bold.afm"
## [3] "Courier-Oblique.afm"
                                 "Courier-BoldOblique.afm"
## [5] "Symbol.afm"
## $encoding
## [1] "default"
## attr(,"class")
## [1] "Type1Font"
## $Helvetica
## $family
## [1] "Helvetica"
##
## $metrics
## [1] "Helvetica.afm"
                                   "Helvetica-Bold.afm"
## [3] "Helvetica-Oblique.afm"
                                   "Helvetica-BoldOblique.afm"
## [5] "Symbol.afm"
## $encoding
## [1] "default"
##
## attr(,"class")
## [1] "Type1Font"
## $'Helvetica-Narrow'
## $family
## [1] "Helvetica-Narrow"
##
## $metrics
## [1] "hvn____.afm" "hvnb____.afm" "hvno____.afm" "hvnbo___.afm" "Symbol.afm"
## $encoding
## [1] "default"
## attr(,"class")
## [1] "Type1Font"
## $NewCenturySchoolbook
## $family
## [1] "NewCenturySchoolbook"
## $metrics
## [1] "ncr____.afm" "ncb____.afm" "nci____.afm" "ncbi____.afm" "Symbol.afm"
##
## $encoding
## [1] "default"
## attr(,"class")
## [1] "Type1Font"
## $Palatino
## $family
```

```
## [1] "Palatino"
##
## $metrics
## [1] "por____.afm" "pob____.afm" "poi____.afm" "pobi____.afm" "Symbol.afm"
## $encoding
## [1] "default"
## attr(,"class")
## [1] "Type1Font"
## $Times
## $family
## [1] "Times"
##
## $metrics
## [1] "Times-Roman.afm"
                              "Times-Bold.afm"
                                                 "Times-Italic.afm"
## [4] "Times-BoldItalic.afm" "Symbol.afm"
## $encoding
## [1] "default"
## attr(,"class")
## [1] "Type1Font"
##
## $URWGothic
## $family
## [1] "URWGothic"
##
## $metrics
## [1] "a0100131.afm" "a0100151.afm" "a0100331.afm" "a0100351.afm" "s0500001.afm"
##
## $encoding
## [1] "default"
## attr(,"class")
## [1] "Type1Font"
##
## $URWBookman
## $family
## [1] "URWBookman"
##
## $metrics
## [1] "b0180121.afm" "b0180151.afm" "b0180321.afm" "b0180351.afm" "s0500001.afm"
## $encoding
## [1] "default"
##
## attr(,"class")
## [1] "Type1Font"
##
## $NimbusMon
## $family
## [1] "NimbusMon"
```

```
##
## $metrics
## [1] "n0220031.afm" "n0220041.afm" "n0220231.afm" "n0220241.afm" "s0500001.afm"
## $encoding
## [1] "default"
## attr(,"class")
## [1] "Type1Font"
##
## $NimbusSan
## $family
## [1] "NimbusSan"
##
## $metrics
## [1] "n0190031.afm" "n0190041.afm" "n0190231.afm" "n0190241.afm" "s0500001.afm"
##
## $encoding
## [1] "default"
## attr(,"class")
## [1] "Type1Font"
##
## $URWHelvetica
## $family
## [1] "URWHelvetica"
## $metrics
## [1] "n019003l.afm" "n019004l.afm" "n019023l.afm" "n019024l.afm" "s050000l.afm"
## $encoding
## [1] "default"
## attr(,"class")
## [1] "Type1Font"
## $NimbusSanCond
## $family
## [1] "NimbusSanCond"
##
## $metrics
## [1] "n0190431.afm" "n0190441.afm" "n0190631.afm" "n0190641.afm" "s0500001.afm"
## $encoding
## [1] "default"
##
## attr(,"class")
## [1] "Type1Font"
## $CenturySch
## $family
## [1] "CenturySch"
##
## $metrics
```

```
## [1] "c0590131.afm" "c0590161.afm" "c0590331.afm" "c0590361.afm" "s0500001.afm"
##
## $encoding
## [1] "default"
## attr(,"class")
## [1] "Type1Font"
## $URWPalladio
## $family
## [1] "URWPalladio"
## $metrics
## [1] "p0520031.afm" "p0520041.afm" "p0520231.afm" "p0520241.afm" "s0500001.afm"
## $encoding
## [1] "default"
##
## attr(,"class")
## [1] "Type1Font"
##
## $NimbusRom
## $family
## [1] "NimbusRom"
##
## $metrics
## [1] "n0210031.afm" "n0210041.afm" "n0210231.afm" "n0210241.afm" "s0500001.afm"
## $encoding
## [1] "default"
## attr(,"class")
## [1] "Type1Font"
## $URWTimes
## $family
## [1] "URWTimes"
##
## $metrics
## [1] "n0210031.afm" "n0210041.afm" "n0210231.afm" "n0210241.afm" "s0500001.afm"
## $encoding
## [1] "default"
##
## attr(,"class")
## [1] "Type1Font"
## $ArialMT
## $family
## [1] "ArialMT"
##
## $metrics
## [1] "ArialMT.afm"
                               "ArialMT-Bold.afm" "ArialMT-Italic.afm"
## [4] "ArialMT-BoldItalic.afm" "Symbol.afm"
```

```
##
## $encoding
## [1] "default"
##
## attr(,"class")
## [1] "Type1Font"
## $ComputerModern
## $family
## [1] "ComputerModern"
## $metrics
## [1] "CM_regular_10.afm"
                               "CM_boldx_10.afm"
                                                           "CM_italic_10.afm"
## [4] "CM_boldx_italic_10.afm" "CM_symbol_10.afm"
## $encoding
## [1] "TeXtext.enc"
## attr(,"class")
## [1] "Type1Font"
##
## $ComputerModernItalic
## $family
## [1] "ComputerModernItalic"
##
## $metrics
## [1] "CM_regular_10.afm" "CM_boldx_10.afm"
                                                 "cmti10.afm"
## [4] "cmbxti10.afm"
                            "CM_symbol_10.afm"
##
## $encoding
## [1] "TeXtext.enc"
##
## attr(,"class")
## [1] "Type1Font"
## $Japan1
## $family
## [1] "HeiseiKakuGo-W5"
##
## $metrics
                                  11 11
                    11 11
## [1] ""
                                               11 11
                                                             "Symbol.afm"
##
## $cmap
## [1] "EUC-H"
## $cmapEncoding
## [1] "EUC-JP"
##
## $pdfresource
## [1] ""
##
## attr(,"class")
## [1] "CIDFont"
##
```

```
## $Japan1HeiMin
## $family
## [1] "HeiseiMin-W3"
##
## $metrics
## [1] ""
                     11 11
                                   11 11
                                                 11 11
                                                               "Symbol.afm"
##
## $cmap
## [1] "EUC-H"
##
## $cmapEncoding
## [1] "EUC-JP"
## $pdfresource
## [1] ""
##
## attr(,"class")
## [1] "CIDFont"
## $Japan1GothicBBB
## $family
## [1] "GothicBBB-Medium"
##
## $metrics
                                   11 11
                                                 11 11
## [1] ""
                                                               "Symbol.afm"
## $cmap
## [1] "EUC-H"
##
## $cmapEncoding
## [1] "EUC-JP"
##
## $pdfresource
## [1] ""
## attr(,"class")
## [1] "CIDFont"
##
## $Japan1Ryumin
## $family
## [1] "Ryumin-Light"
##
## $metrics
## [1] ""
                     11 11
                                  11 11
                                                 11 11
                                                               "Symbol.afm"
##
## $cmap
## [1] "EUC-H"
##
## $cmapEncoding
## [1] "EUC-JP"
##
## $pdfresource
## [1] ""
##
```

```
## attr(,"class")
## [1] "CIDFont"
##
## $Korea1
## $family
## [1] "Baekmuk-Batang"
## $metrics
                                  11 11
                     11 11
                                                 11 11
                                                               "Symbol.afm"
## [1] ""
##
## $cmap
## [1] "KSCms-UHC-H"
## $cmapEncoding
## [1] "CP949"
##
## $pdfresource
## [1] ""
## attr(,"class")
## [1] "CIDFont"
## $Korea1deb
## $family
## [1] "Batang-Regular"
## $metrics
                     11 11
                                  11 11
## [1] ""
                                                 11 11
                                                               "Symbol.afm"
##
## $cmap
## [1] "KSCms-UHC-H"
##
## $cmapEncoding
## [1] "CP949"
## $pdfresource
## [1] ""
##
## attr(,"class")
## [1] "CIDFont"
##
## $CNS1
## $family
## [1] "MOESung-Regular"
## $metrics
                     11 11
                                11 11
                                                 11 11
## [1] ""
                                                               "Symbol.afm"
##
## $cmap
## [1] "B5pc-H"
## $cmapEncoding
## [1] "CP950"
##
```

```
## $pdfresource
## [1] ""
##
## attr(,"class")
## [1] "CIDFont"
##
## $GB1
## $family
## [1] "BousungEG-Light-GB"
##
## $metrics
                    11 11
## [1] ""
                               11 11
                                                             "Symbol.afm"
##
## $cmap
## [1] "GBK-EUC-H"
##
## $cmapEncoding
## [1] "GBK"
##
## $pdfresource
## [1] ""
##
## attr(,"class")
## [1] "CIDFont"
```