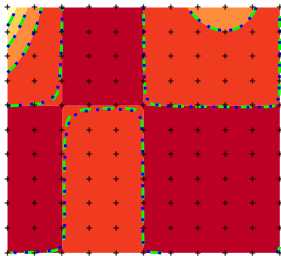


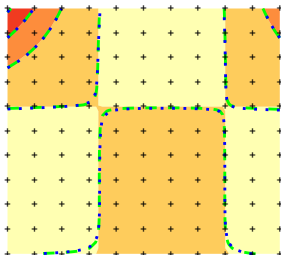
f



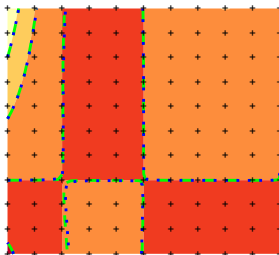
regular data grid 11 x 11  
 colors = exact values  
 dashed green = global bw  
 dotted blue = local bw  
 crosses: data points

$$\begin{aligned} f(x,y) &= x^3y^2 - 0.6x^3y + (-1.7)x^2y^2 + 1.02x^2y \\ &\quad y + 0.8x^2y^2 - 0.48x^2y + (-0.1)y^2 + 0.06y \\ f_x(x,y) &= 3x^2y^2 - 1.8x^2y + (-3.4)x^2y^2 + 2.04x^2y + 0.8y^2 - 0.48y \\ f_y(x,y) &= 2x^3y - 0.6x^3 + (-3.4)x^2y + 1.02x^2 + 1.6x^2y - 0.48x + (-0.2)y + 0.06 \\ f_{xx}(x,y) &= 6x^2y^2 - 3.6x^2y + (-3.4)y^2 + 2.04y \\ f_{yy}(x,y) &= 2x^3 - 3.4x^2 + 1.6x - 0.2 \\ f_{xy}(x,y) &= 6x^2y - 1.8x^2 + (-6.8)x^2y + 2.04x + 1.6y - 0.48 \\ f_{xxx}(x,y) &= 6y^2 - 3.6y \\ f_{yyy}(x,y) &= 0 \\ f_{xxy}(x,y) &= 12xy - 3.6x + (-6.8)y + 2.04 \\ f_{xyy}(x,y) &= 6x^2 - 6.8x + 1.6 \end{aligned}$$

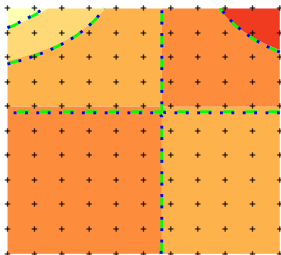
f\_x



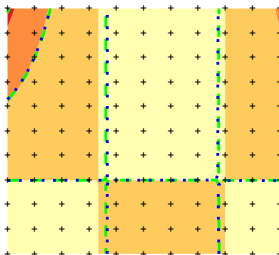
f\_x



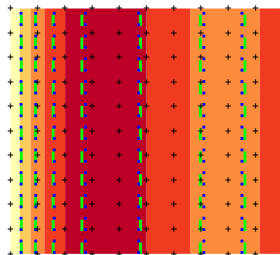
f\_xx



f\_xx

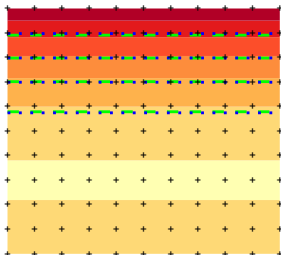


f\_yy

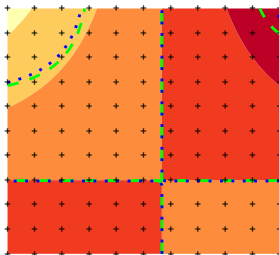


kernel: gaussian  
 global bandwidth 33 %  
 local bandwidth 11 %

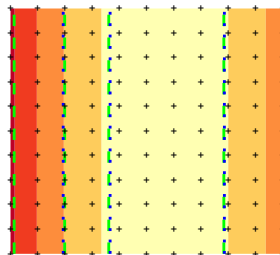
f\_xxx



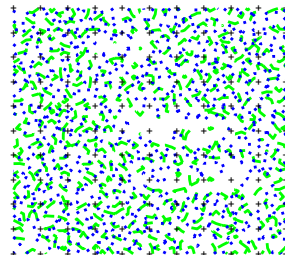
f\_xxy



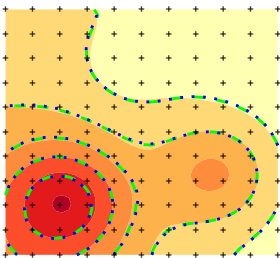
f\_xyy



f\_yyy



f



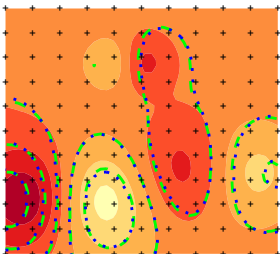
regular data grid 11 x 11  
 colors = exact values  
 dashed green = global bw  
 dotted blue = local bw  
 crosses: data points

$$f(x,y) = 0.75 \exp(-((9*x-2)^2 + (9*y-2)^2)/4) + 0.75 \exp(-((9*x+1)^2/49 + (9*y+1)/10)) + 0.5 \exp(-((9*x-7)^2 + (9*y-3)^2)/4) - 0.2 \exp(-((9*x-4)^2 + (9*y-7)^2))$$

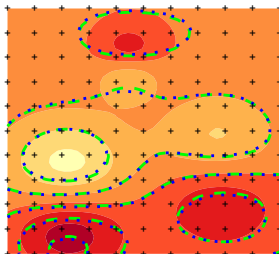
$$f_x(x,y) = ((-60.75) \exp(-((9*x-2)^2 + (9*y-2)^2)/4) * x + 13.5 \exp(-((9*x-2)^2 + (9*y-2)^2)/4) / 2 + ((-121.5) * x \exp(-((9*x+1)^2/49 + (9*y+1)/10))) / 49 + ((-40.5) * x \exp(-((9*x-7)^2 + (9*y-3)^2)/4) / 2 + 0.324e2 * x \exp(-((9*x-4)^2 + (9*y-7)^2)) + ((-13.5) \exp(-((9*x+1)^2/49 + (9*y+1)/10))) / 49 + (31.5 \exp(-((9*x-7)^2 + (9*y-3)^2)/4) / 2 - 0.144e2 \exp(-((9*x-4)^2 + (9*y-7)^2)))$$

$$f_y(x,y) = ((-60.75) \exp(-((9*x-2)^2 + (9*y-2)^2)/4) * y + 13.5 \exp(-((9*x-2)^2 + (9*y-2)^2)/4) / 2 + ((-40.5) * y \exp(-((9*x-7)^2 + (9*y-3)^2)/4) / 2 + 0.324e2 * y \exp(-((9*x-4)^2 + (9*y-7)^2)) + ((-6.75) \exp(-((9*x+1)^2/49 + (9*y+1)/10))) / 10 + (13.5 \exp(-((9*x-7)^2 + (9*y-3)^2)/4) / 2 - 0.252e2 \exp(-((9*x-4)^2 + (9*y-7)^2)))$$

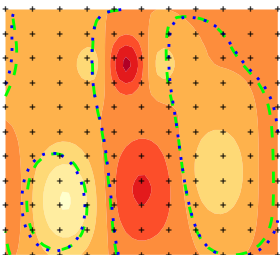
f\_x



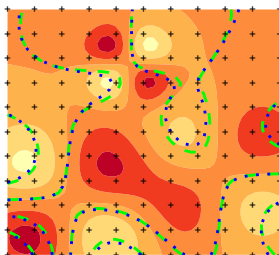
f\_x



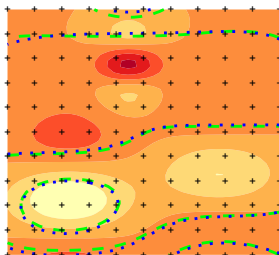
f\_xx



f\_xy

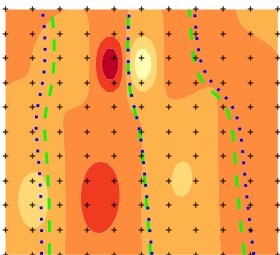


f\_yy

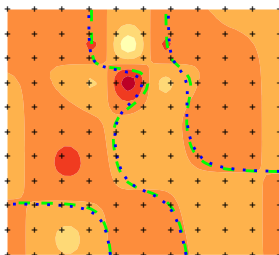


kernel: gaussian  
 global bandwidth 33 %  
 local bandwidth 11 %

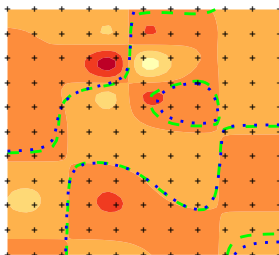
f\_xxx



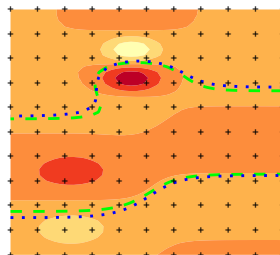
f\_xxy



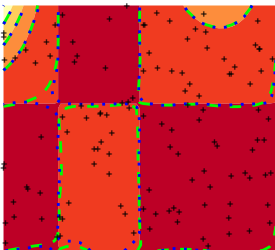
f\_xyy



f\_yyy



f



irregular data grid 121 pts

colors = exact values

dashed green = global bw

dotted blue = local bw

crosses: data points

$$f(x,y) = x^3y^2 - 0.6x^3y + (-1.7)x^2y^2 + 1.02x^2y + 0.8x^2y^2 - 0.48x^2y + (-0.1)y^2 + 0.06y$$

$$f_x(x,y) = 3x^2y^2 - 1.8x^2y + (-3.4)x^2y^2 + 2.04x^2y + 0.8y^2 - 0.48y$$

$$f_y(x,y) = 2x^3y - 0.6x^3 + (-3.4)x^2y + 1.02x^2 + 1.6x^2y - 0.48x + (-0.2)y + 0.06$$

$$f_{xx}(x,y) = 6x^2y^2 - 3.6x^2y + (-3.4)y^2 + 2.04y$$

$$f_{yy}(x,y) = 2x^3 - 3.4x^2 + 1.6x - 0.2$$

$$f_{xy}(x,y) = 6x^2y - 1.8x^2 + (-6.8)x^2y + 2.04x + 1.6y - 0.48$$

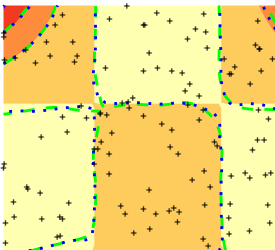
$$f_{xxx}(x,y) = 6y^2 - 3.6y$$

$$f_{yyy}(x,y) = 0$$

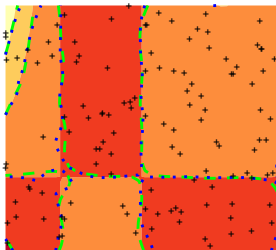
$$f_{xxy}(x,y) = 12xy - 3.6x + (-6.8)y + 2.04$$

$$f_{xyy}(x,y) = 6x^2 - 6.8x + 1.6$$

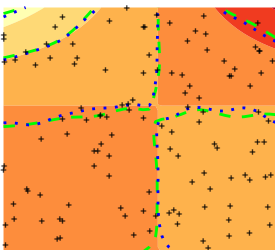
f\_x



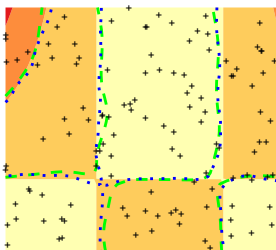
f\_x



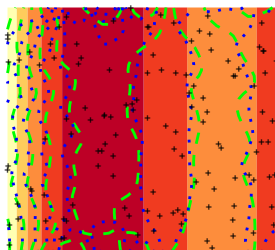
f\_xx



f\_xy

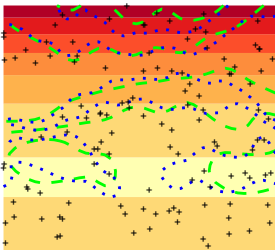


f\_yy

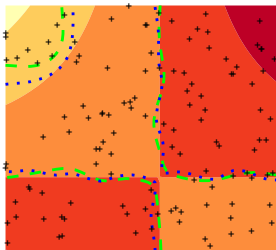


kernel: gaussian  
global bandwidth 33 %  
local bandwidth 11 %

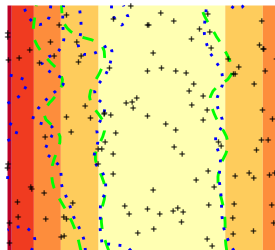
f\_xxx



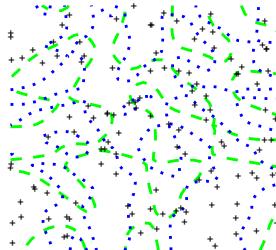
f\_xxy



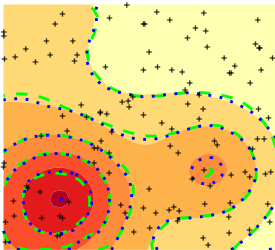
f\_xyy



f\_yyy



f



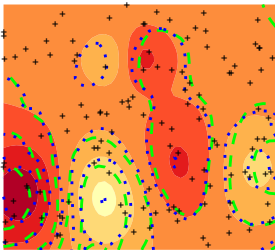
irregular data grid 121 pts  
 colors = exact values  
 dashed green = global bw  
 dotted blue = local bw  
 crosses: data points

$$f(x,y) = 0.75 \exp(-((9x-2)^2 + (9y-2)^2)/4) + 0.75 \exp(-((9x+1)^2/49 + (9y+1)/10)) + 0.5 \exp(-((9x-7)^2 + (9y-3)^2)/4) - 0.2 \exp(-((9x-4)^2 + (9y-7)^2))$$

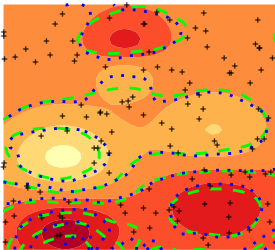
$$f_x(x,y) = ((-60.75) \exp(-((9x-2)^2 + (9y-2)^2)/4) * x + 13.5 \exp(-((9x-2)^2 + (9y-2)^2)/4) / 2 + ((-121.5) * x \exp(-((9x+1)^2/49 + (9y+1)/10))) / 4 + 9 + ((-40.5) * x \exp(-((9x-7)^2 + (9y-3)^2)/4) / 2 + 0.324e2 * x \exp(-((9x-4)^2 + (9y-7)^2)) + ((-13.5) * \exp(-((9x+1)^2/49 + (9y+1)/10))) / 49 + (31.5 \exp(-((9x-7)^2 + (9y-3)^2)/4) / 2 - 0.144e2 \exp(-((9x-4)^2 + (9y-7)^2)))$$

$$f_y(x,y) = ((-60.75) \exp(-((9x-2)^2 + (9y-2)^2)/4) * y + 13.5 \exp(-((9x-2)^2 + (9y-2)^2)/4) / 2 + ((-40.5) * y \exp(-((9x-7)^2 + (9y-3)^2)/4) / 2 + 0.324e2 * y \exp(-((9x-4)^2 + (9y-7)^2)) + ((-6.75) * \exp(-((9x+1)^2/49 + (9y+1)/10))) / 10 + (13.5 \exp(-((9x-7)^2 + (9y-3)^2)/4) / 2 - 0.252e2 \exp(-((9x-4)^2 + (9y-7)^2)))$$

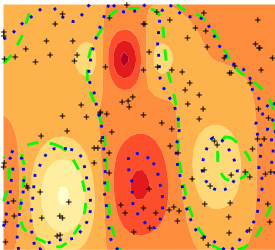
f\_x



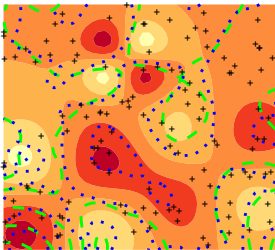
f\_x



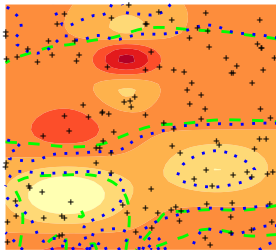
f\_xx



f\_xy

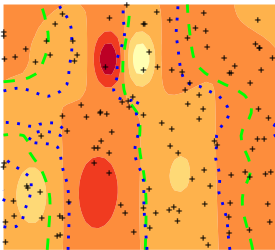


f\_yy

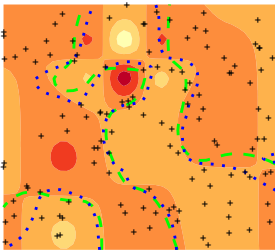


kernel: gaussian  
 global bandwidth 33 %  
 local bandwidth 11 %

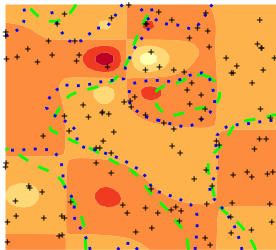
f\_xxx



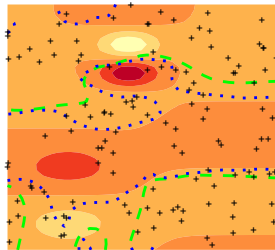
f\_xxy



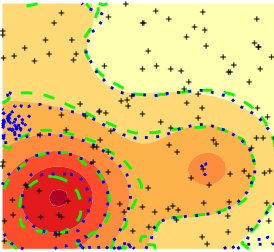
f\_xyy



f\_yyy



f



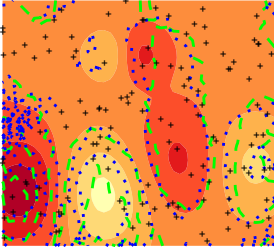
irregular data grid 121 pts  
colors = exact values  
dashed green = global bw  
dotted blue = local bw  
crosses: data points

$$f(x,y) = 0.75 \exp(-((9*x-2)^2 + (9*y-2)^2)/4) + 0.75 \exp(-((9*x+1)^2/49 + (9*y+1)/10)) + 0.5 \exp(-((9*x-7)^2 + (9*y-3)^2)/4) - 0.2 \exp(-((9*x-4)^2 + (9*y-7)^2))$$

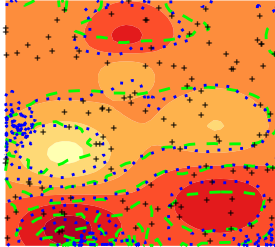
$$f_x(x,y) = ((-60.75) \exp(-((9*x-2)^2 + (9*y-2)^2)/4) * x + 13.5 \exp(-((9*x-2)^2 + (9*y-2)^2)/4) / 2 + ((-121.5) * x \exp(-((9*x+1)^2/49 + (9*y+1)/10))) / 4 + 9 + ((-40.5) * x \exp(-((9*x-7)^2 + (9*y-3)^2)/4) / 2 + 0.324e2 * x \exp(-((9*x-4)^2 + (9*y-7)^2)) + ((-13.5) \exp(-((9*x+1)^2/49 + (9*y+1)/10))) / 49 + (31.5 \exp(-((9*x-7)^2 + (9*y-3)^2)/4) / 2 - 0.144e2 \exp(-((9*x-4)^2 + (9*y-7)^2)))$$

$$f_y(x,y) = ((-60.75) \exp(-((9*x-2)^2 + (9*y-2)^2)/4) * y + 13.5 \exp(-((9*x-2)^2 + (9*y-2)^2)/4) / 2 + ((-40.5) * y \exp(-((9*x-7)^2 + (9*y-3)^2)/4) / 2 + 0.324e2 * y \exp(-((9*x-4)^2 + (9*y-7)^2)) + ((-6.75) \exp(-((9*x+1)^2/49 + (9*y+1)/10))) / 10 + (13.5 \exp(-((9*x-7)^2 + (9*y-3)^2)/4) / 2 - 0.252e2 \exp(-((9*x-4)^2 + (9*y-7)^2)))$$

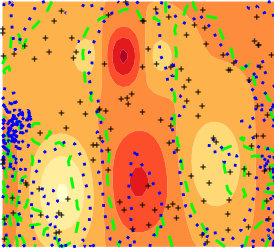
f\_x



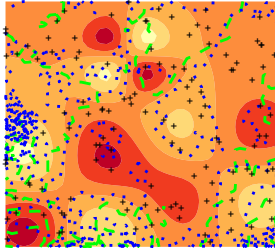
f\_x



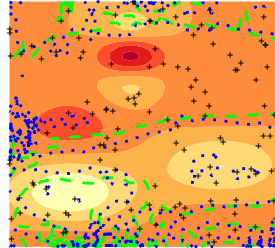
f\_xx



f\_xy

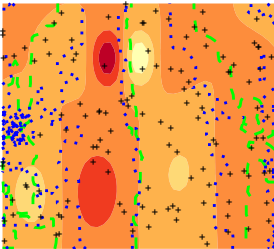


f\_yy

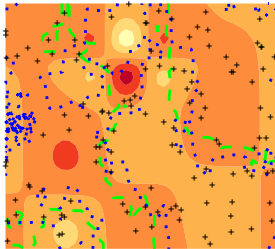


kernel: uniform  
global bandwidth 33 %  
local bandwidth 11 %

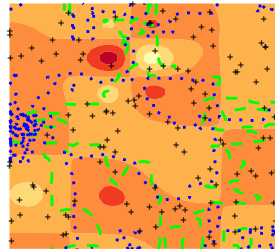
f\_xxx



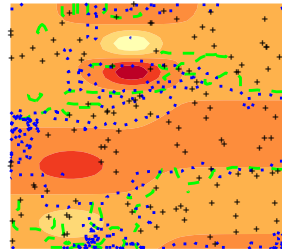
f\_xxy



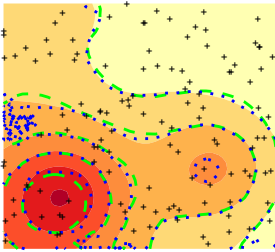
f\_xyy



f\_yyy



f



irregular data grid 121 pts  
colors = exact values  
dashed green = global bw  
dotted blue = local bw  
crosses: data points

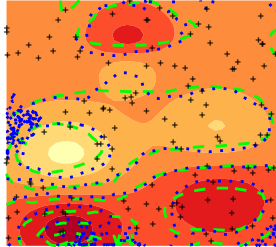
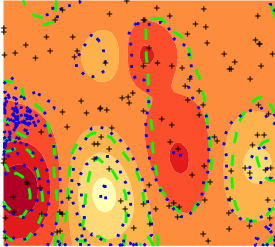
$$f(x,y) = 0.75 \exp(-((9x-2)^2 + (9y-2)^2)/4) + 0.75 \exp(-((9x+1)^2/49 + (9y+1)/10)) + 0.5 \exp(-((9x-7)^2 + (9y-3)^2)/4) - 0.2 \exp(-((9x-4)^2 + (9y-7)^2))$$

$$f_x(x,y) = ((-60.75) \exp(-((9x-2)^2 + (9y-2)^2)/4) * x + 13.5 \exp(-((9x-2)^2 + (9y-2)^2)/4) / 2 + ((-121.5) * x \exp(-((9x+1)^2/49 + (9y+1)/10))) / 4 + 9 + ((-40.5) * x \exp(-((9x-7)^2 + (9y-3)^2)/4) / 2 + 0.324e2 * x \exp(-((9x-4)^2 + (9y-7)^2)) + ((-13.5) \exp(-((9x+1)^2/49 + (9y+1)/10))) / 49 + (31.5 \exp(-((9x-7)^2 + (9y-3)^2)/4) / 2 - 0.144e2 \exp(-((9x-4)^2 + (9y-7)^2)))$$

$$f_y(x,y) = ((-60.75) \exp(-((9x-2)^2 + (9y-2)^2)/4) * y + 13.5 \exp(-((9x-2)^2 + (9y-2)^2)/4) / 2 + ((-40.5) * y \exp(-((9x-7)^2 + (9y-3)^2)/4) / 2 + 0.324e2 * y \exp(-((9x-4)^2 + (9y-7)^2)) + ((-6.75) \exp(-((9x+1)^2/49 + (9y+1)/10))) / 10 + (13.5 \exp(-((9x-7)^2 + (9y-3)^2)/4) / 2 - 0.252e2 \exp(-((9x-4)^2 + (9y-7)^2)))$$

f\_x

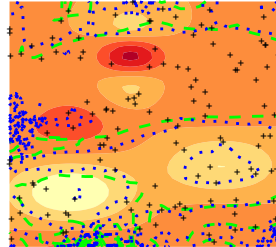
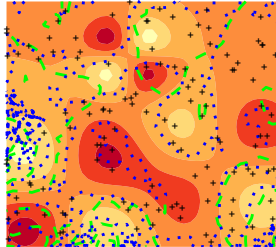
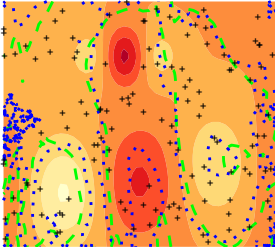
f\_x



f\_xx

f\_xy

f\_yy



kernel: epanechnikov  
global bandwidth 33 %  
local bandwidth 11 %

f\_xxx

f\_xxy

f\_xyy

f\_yyy

