

① funció de transferència:

$$V_o = \frac{\frac{1}{C_s}}{\frac{1}{C_s} + R_1} V_i = \frac{1}{1 + C_s R_1} V_i$$

$$H(s) = \frac{1}{1 + R_1 C_1 s} = \frac{1/R_1 C_1}{s + \frac{1}{R_1 C_1}} = \frac{1}{s + \frac{1}{10^3 \cdot 10 \cdot 10^{-9}}} = \frac{10^5}{s + 10^5}$$

$$H(s) = \frac{1}{1 + \frac{s}{10^5}}$$

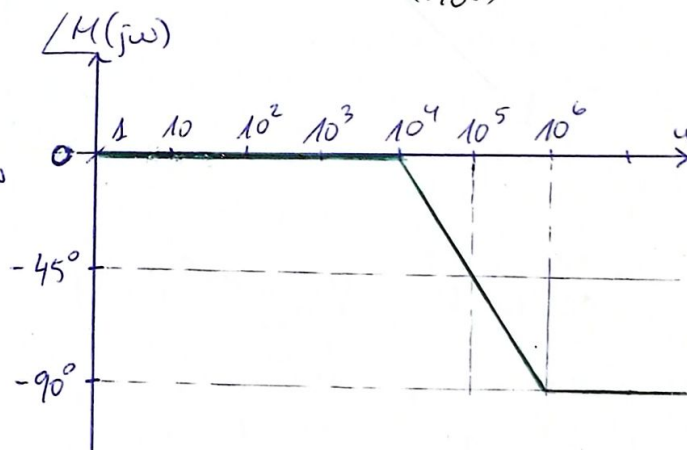
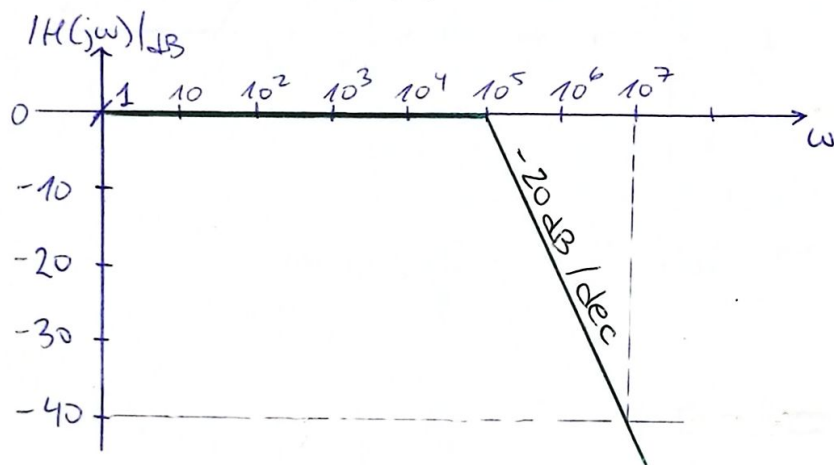
→ Filtre passa-baix.

② diagrama de Bode (mòdul i fase)

$$H(j\omega) = \frac{1}{1 + \frac{j\omega}{10^5}} \rightarrow |H(j\omega)| = \frac{1}{\sqrt{1 + \left(\frac{\omega}{10^5}\right)^2}}$$

$$\angle H(j\omega) = -\arctg\left(\frac{\omega}{10^5}\right)$$

$$|H(j\omega)|_{dB} = -20 \log\left(\sqrt{1 + \left(\frac{\omega}{10^5}\right)^2}\right)$$



③ freqüència de tall del circuit: $\omega_c = 10^5 \text{ rad/s} \rightarrow f_c = \frac{10^5}{2\pi} = 15,9 \text{ kHz}$

④ Valor de $|H(j\omega)|$ per a $f_1 = 1 \text{ kHz}$, $f_2 = 10 \text{ kHz}$, $f_3 = 100 \text{ kHz}$.

$$|H(j\omega_1)| = \frac{1}{\sqrt{1 + \left(\frac{2 \cdot 10^3 \pi}{10^5}\right)^2}} = 0,998$$

$$|H(j\omega_2)| = \frac{1}{\sqrt{1 + \left(\frac{2\pi \cdot 10^4}{10^5}\right)^2}} = 0,8467$$

$$|H(j\omega_3)| = \frac{1}{\sqrt{1 + \left(\frac{2\pi \cdot 10^5}{10^5}\right)^2}} = 0,1572$$

$$\omega_1 = 2\pi \cdot f_1 = 2\pi \cdot 10^3$$

$$\omega_2 = 2\pi \cdot f_2 = 2\pi \cdot 10^4$$

$$\omega_3 = 2\pi \cdot f_3 = 2\pi \cdot 10^5$$